

Superstrings on NS5 backgrounds,
deformed AdS_3 and holography

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MIDEAST meeting, Kolymbari, June 2003

Based on work with C. Kounnas and
M. Petropoulos, hep-th/0306053

OUTLINE OF THE TALK

1. Introduction and motivations
2. Decoupling limits of D1/D5
3. Partition function for $SL(2, \mathbb{R})$
4. Marginal deformations of $SL(2, \mathbb{R})$
5. Comments on holography
6. Conclusions and open problems

INTRODUCTION

1. String theory on AdS_3 backgrounds

- Exact description: WZW model $SL(2, \mathbb{R}) \Rightarrow$ simplest non-trivial spacetime in string theory
- Configuration of NS5/F1 branes in near-horizon limit \Rightarrow background $AdS_3 \times S^3 \times (T^4 \text{ or } K3)$

*Antoniadis, Bachas, Sagnotti, Phys. Lett. **B235***

Horowitz, Maldacena, Strominger, hep-th/9603109

- Starting point for other interesting string backgrounds: black holes, cosmological models...

*Witten, Phys. Rev. **D44***

Kounnas, Lüst, hep-th/9205046

- Non-unitary worldsheet CFT based on the non-compact affine algebra $\widehat{SL}(2, \mathbb{R})_L \times \widehat{SL}(2, \mathbb{R})_R$

*Balog, O'Raiifeartaigh, Forgacs, Wipf, Nucl. Phys. **B325***

- To obtain a consistent theory \Rightarrow new representations by spectral flow

Maldacena, Ooguri, hep-th/0001053

- The one loop partition function was not known up to now \Rightarrow new proposal

Israël, Kounnas, Petropoulos, hep-th/0306053

2. Holography

- D1/D5-branes theory in the decoupling limit
 $\Rightarrow AdS_3/CFT_2$ correspondence

Maldacena hep-th/9711200

- NS5-branes worldvolume theory in the decoupling limit: "Little String Theory" (LST). Conjectured holography with the near-horizon limit of the NS5-branes background: $SU(2) \times U(1)_Q$

Seiberg hep-th/9705221

Aharony, Berkooz, Kutasov, Seiberg, hep-th/9808149

- RG flow between these two theories?
 \Rightarrow exact string background:

$$\{\text{null} - \text{deformed } SL(2, \mathbb{R})\} \times SU(2) \times U(1)^4$$

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3. Marginal deformations of $SL(2, \mathbb{R})$

- WZW models can be deformed marginally with bilinears of currents of the Cartan subalgebra

Chaudhuri, Schwartz, Phys. Lett. **B219**

- In $SL(2, \mathbb{R})$, three possibilities: two inequivalent choices of Cartan subalgebra, and the *null* subalgebra.

Förste, hep-th/9407198

\Rightarrow Derivation of the spectrum for these deformations
& superconformal structure of the null deformation

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THE D1/D5 BACKGROUND

- Solution of type IIB supergravity:

$$d\tilde{s}_\sigma^2 = \frac{-dt^2 + dx^2}{\sqrt{H_1 H_5}} + \sqrt{H_1 H_5} (dr^2 + r^2 d\Omega_3^2) + \sqrt{\frac{H_1}{H_5}} \sum_{i=6}^9 (dx^i)^2$$

$$e^{2\tilde{\phi}} = g_s^2 \frac{H_1}{H_5}$$

$$\text{with } H_1 = 1 + \frac{g_s \alpha' N_1}{v r^2}, \quad H_5 = 1 + \frac{g_s \alpha' N_5}{r^2}.$$

- Standard decoupling limit: $\alpha' \rightarrow 0$, $u \equiv \alpha'/r$ fixed, v fixed

★ The geometry is $AdS_3 \times S^3 \times T^4$:

$$ds^2 = \alpha' g_s \sqrt{\frac{N_1 N_5}{v}} \left\{ \frac{du^2 + dX^2 - dT^2}{u^2} + d\Omega_3^2 \right\} + \sqrt{\frac{N_1}{v N_5}} \sum_{i=1}^6 (dx^i)^2$$

Maldacena, hep-th/9711200

- New decoupling limit: partial near-horizon geometry

$$\left\{ \begin{array}{l} \alpha' \rightarrow 0, \\ u = \alpha'/r \text{ fixed,} \\ g_s \alpha' \text{ fixed (i.e. } g_s \rightarrow \infty), \\ \alpha'^2 v \text{ fixed (i.e. } \textit{decompactification}) \end{array} \right.$$

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★ S-dual background ($\phi = -\tilde{\phi}$, $F_{[3]} \rightarrow H_{[3]}$):

$$\{\text{null - deformed } SL(2, \mathbb{R})\} \times SU(2) \times T^4$$

$$ds_\sigma^2 = \alpha' N_5 \left\{ \frac{du^2}{u^2} + \frac{dX^2 - dT^2}{u^2 + 1/M^2} + d\Omega_3^2 \right\} + \frac{1}{g_s} \sum_{i=6}^9 (dx^i)^2$$

$$e^{2\phi} = g_{max}^2 \frac{u^2}{u^2 + 1/M^2}$$

With the mass scale $M^2 = \frac{g_s N_1}{\alpha' v}$

String coupling constant bounded from above:

$$g_{max} = \sqrt{\frac{v N_5}{g_s^2 N_1}}$$

★ Asymptotic geometries:

1. $u \rightarrow 0$: linear dilaton (weakly coupled region)
2. $u \rightarrow \infty$: AdS_3 geometry (central region)

● Supersymmetry

Type IIB supergravity in partial near-horizon geometry

★ Condition for unbroken susy:

$$\delta\lambda = \delta\psi_\mu = 0.$$

\Rightarrow Preserves 1/4 of supersymmetry

- Sigma-model description

$SL(2, \mathbb{R})$ WZW model in Poincaré coordinates :

$$S = \frac{k}{2\pi} \int d^2z \left(\frac{\partial u \bar{\partial} u}{u^2} + \frac{\partial x^+ \bar{\partial} x^-}{u^2} \right).$$

The following null isometries are linearly realized :

$$J = J^1 + J^3 = \frac{\partial x^+}{u^2}, \quad \bar{J} = \bar{J}^1 + \bar{J}^3 = \frac{\bar{\partial} x^-}{u^2}.$$

★ Deform the model with truly marginal operator $J\bar{J}$:

$$S_M = \frac{k}{2\pi} \int d^2z \left(\frac{\partial u \bar{\partial} u}{u^2} + \frac{\partial x^+ \bar{\partial} x^-}{u^2 + 1/M^2} \right)$$

Affine symmetry $\widehat{SL}(2, \mathbb{R})_L \times \widehat{SL}(2, \mathbb{R})_R$ broken down to $\widehat{U}(1)_L \times \widehat{U}(1)_R$.

Förste, hep-th/9407198

★ **Alternatively:** $O(2, 2, \mathbb{R})$ transformation of the background

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THE $SL(2, \mathbb{R})$ CONFORMAL FIELD THEORY

- Algebraic description: non-compact affine $SL(2, \mathbb{R})$ algebra:

$$\begin{aligned} [J_n^3, J_m^3] &= -\frac{k}{2}n\delta_{m,-n}, \\ [J_n^3, J_m^\pm] &= \pm J_{n+m}^\pm, \\ [J_n^+, J_m^-] &= -2J_{n+m}^3 + kn\delta_{m,-n}. \end{aligned}$$

- Physical spectrum

Physical spectrum built from unitary representations of the horizontal algebra:

Principal discrete representations \mathcal{D}_j^\pm , with $m = \pm j, \pm(j+1), \dots, j \in \mathbb{R}^+$;

Principal continuous representations \mathcal{C}_j^α , with $m = \alpha, \alpha \pm 1, \dots, 0 \leq \alpha < 1, j = 1/2 + i\mathbb{R}$.

Non-unitary affine representations \Rightarrow unitary physical spectrum if : $0 < j < k/2$ (discrete representations).

Petropoulos, Phys. Lett. B236

Mohammedi, Int. J. Mod. Phys. A5

- Spectral flow: to obtain a closed and physically sensible spectrum (with an infinite tower of massive states) \Rightarrow inclusion of new sectors obtained by *spectral flow*:

$$\begin{aligned} \tilde{J}_n^3 &= J_n^3 - \frac{k}{2}w \delta_{n,0} \\ \tilde{J}_n^\pm &= J_{n\pm w}^\pm \end{aligned}$$

Maldacena, Ooguri, hep-th/0001053

★ *Partition function?* \Rightarrow divergent affine characters.

- The coset theory $SL(2, \mathbb{R})/U(1)_A$

Axial gauging of $SL(2, \mathbb{R})$: $g \rightarrow hgh$ with $h = e^{i\lambda\sigma_2/2}$
 \Rightarrow **non-compact parafermions**.

Unitary CFT with the partition function:

$$Z_A = 4\sqrt{k(k-2)}\eta\bar{\eta} \int d^2s \frac{e^{\frac{2\pi}{\tau_2}(\text{Im}(s_1\tau - s_2))^2}}{|\vartheta_1(s_1\tau - s_2|\tau)|^2} \sum_{m,w=-\infty}^{+\infty} e^{-\frac{k\pi}{\tau_2} |(s_1+w)\tau - (s_2+m)|^2}$$

Hanany, Prezas, Troost, hep-th/0202129

1. Freely acting orbifold structure
2. Obvious divergence for $s_1 = s_2 = 0$

- The $SL(2, \mathbb{R})$ partition function from the coset

1. States of the coset :

$$J_{n>0}^3 |\Phi\rangle = \bar{J}_{n>0}^3 |\Phi\rangle = 0$$

$$\text{and } J_0^3 + \bar{J}_0^3 = -wk, \quad J_0^3 - \bar{J}_0^3 = n.$$

2. No-ghost theorem for $SL(2, \mathbb{R}) \Rightarrow$ physical states obey:

$$J_{n>0}^3 |\Phi\rangle = \bar{J}_{n>0}^3 |\Phi\rangle = 0$$

3. To reconstruct the $SL(2, \mathbb{R})$ partition function \Rightarrow couple the coset theory with an appropriate lattice
4. non-compact parafermions: \mathbb{Z} symmetry
 \Rightarrow **continuous orbifold**

$$SL(2, \mathbb{R}) \sim \left(\frac{SL(2, \mathbb{R})}{U(1)} \times U(1)_t \right) / \mathbb{Z}$$

★ Partition function for $SL(2, \mathbb{R})$:

$$Z_{SL(2,R)} = 4k(k-2)^{3/2} \int d^2s d^2t \frac{e^{\frac{2\pi}{\tau_2}(\text{Im}(s_1\tau - s_2))^2}}{|\vartheta_1(s_1\tau - s_2|\tau)|^2} \times$$

$$\times \sum_{m,w} e^{-\frac{k\pi}{\tau_2} |(s_1 - t_1 + w)\tau - (s_2 - t_2 + m)|^2} \sum_{m',w'} e^{+\frac{k\pi}{\tau_2} |(t_1 + w')\tau - (t_2 + m')|^2}$$

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● Structure of the partition function

1. Structure of a $\mathbb{Z}_{twist} \times \mathbb{Z}_{shift}$ orbifold \Rightarrow modular invariant

2. Zero modes structure:

$$P_{L,R}^+ = \frac{n^+}{\sqrt{2k}} \pm \sqrt{\frac{k}{2}}(w_- - 2t_1), \quad P_{L,R}^- = \pm \sqrt{\frac{k}{2}}w_+.$$

$\Rightarrow X^-$ is compact, X^+ at “radius” zero (i.e. non-compact)

\Rightarrow “Shifted winding” $\sqrt{\frac{k}{2}}(w_- - 2t_1)$ defines a *lightcone energy*

3. Free-field representation:

$$J^3 = i\sqrt{\frac{k}{2}}\partial T, \quad J^\pm = - \left(\sqrt{\frac{k}{2}}\partial X \pm i\sqrt{\frac{k-2}{2}}\partial\rho \right) e^{\pm i\sqrt{\frac{2}{k}}(X-T)}$$

with a linear dilaton: $Q_\rho = 1/\sqrt{2(k-2)}$

★ **Structure of the zero modes:** integration over t_1, t_2

★ **Correlation with oscillators:** integration over s_1, s_2

4. Integration over the lightcone energy : after regulating the partition function and analytic continuation, one find:

$$Z_{SL(2,\mathbb{R})} = 4 \frac{(k-2)^{3/2} e^{\frac{2\pi}{\tau_2}(\text{Im}\theta)^2}}{k\sqrt{\tau_2} |\vartheta_1(\theta|\tau)|^2}.$$

Gawedzki, hep-th/91100796

Petropoulos, hep-th/9908189

- Uncovering the spectrum

Integration of the Lagrange multipliers s_1, s_2 and t_2 :

★ *Discrete representations* in the range
 $\frac{1}{2} < j < \frac{k-1}{2}$

$$L_0 = -\frac{j(j-1)}{k-2} + w_+ \left(-\tilde{m} - \frac{k}{4}w_+ \right) + N,$$

$$\bar{L}_0 = -\frac{j(j-1)}{k-2} + w_+ \left(-\tilde{m} - \frac{k}{4}w_+ \right) + \bar{N},$$

★ *Continuous representations*

$$L_0 = \frac{s^2 + 1/4}{k-2} + w_+ \left(-\tilde{m} - \frac{k}{4}w_+ \right) + N,$$

$$\bar{L}_0 = \frac{s^2 + 1/4}{k-2} + w_+ \left(-\tilde{m} - \frac{k}{4}w_+ \right) + \bar{N},$$

with $\tilde{m} + \tilde{\tilde{m}} = -k(w - t_1)$ and $\tilde{m} - \tilde{\tilde{m}} = n$.

Maldacena, Ooguri, hep-th/0001053

- Superconformal structure

The $\hat{c} = 6$ worldsheet SCFT $SL(2, \mathbb{R}) \times SU(2)$ factorizes into a first $\hat{c} = 2$, $N = 2$ superconformal algebra, with $N = 2$ R-current:

$$J_2 = \psi^3 \chi^3$$

And a “would be” N=4 algebra, with $N = 2$ R-current:

$$\begin{aligned} J_4 &= i\sqrt{2}\partial H^+ \\ &= \chi^+ \chi^- + \psi^+ \psi^- \\ &\quad + \frac{2}{k+2} \left[\underbrace{J^3 + \chi^+ \chi^-}_{\text{total } SL(2,R) \text{ } J^3 \text{ current}} - \left(\underbrace{I^3 + \psi^+ \psi^-}_{\text{total } SU(2) \text{ } I^3 \text{ current}} \right) \right] \end{aligned}$$

Cartan currents coupled to their respective coset theories $\Rightarrow H^+$ is not a free boson at self-dual radius

- Spacetime supersymmetry ?

$N = 2$ current $J = J_2 + J_4$ not appropriate to define spacetime supercharges:

1. Physical states have non-integer charges w.r.t. J
2. Target space symmetries not respected

⇒ Use directly the bosonized free fermions:

$$\Theta_\varepsilon(z) = \exp \left\{ \frac{i}{2} (\varepsilon_0 H_0 + \varepsilon_1 H_1 + \varepsilon_2 H_2 + \varepsilon_3 H_3 + \varepsilon_4 H_4) \right\}$$

physical, provided that $\varepsilon_0 \varepsilon_1 \varepsilon_2 = 1$ (i.e. choice of 6D chirality for $AdS_3 \times S^3$ fermions)

Giveon, Kutasov, Seiberg, hep-th/9806194

For type IIB: we realize instead the projection on the four-torus fermions ⇒ T^4/\mathbb{Z}_2 orbifold. The five-branes are wrapped on K3.

★ Partition function (type IIB):

$$\begin{aligned} Z_{\text{IIB}} &= \frac{\text{Im}\tau}{\eta^2 \bar{\eta}^2} Z_{SU(2)} Z_{SL(2, \mathbb{R})} \frac{1}{2} \sum_{h,g=0}^1 Z_{T^4/\mathbb{Z}_2}^{\text{twisted}} \begin{bmatrix} h \\ g \end{bmatrix} \\ &\times \frac{1}{2} \sum_{a,b=0}^1 (-)^{a+b} \vartheta^2 \begin{bmatrix} a \\ b \end{bmatrix} \vartheta \begin{bmatrix} a+h \\ b+g \end{bmatrix} \vartheta \begin{bmatrix} a-h \\ b-g \end{bmatrix} \\ &\times \frac{1}{2} \sum_{\bar{a}, \bar{b}=0}^1 (-)^{\bar{a}+\bar{b}} \bar{\vartheta}^2 \begin{bmatrix} \bar{a} \\ \bar{b} \end{bmatrix} \bar{\vartheta} \begin{bmatrix} \bar{a}+h \\ \bar{b}+g \end{bmatrix} \bar{\vartheta} \begin{bmatrix} \bar{a}-h \\ \bar{b}-g \end{bmatrix} \end{aligned}$$

MARGINAL DEFORMATIONS OF $SL(2, \mathbb{R})$

Bilinears of affine Cartan currents in WZW models \Rightarrow exactly marginal deformations \Rightarrow continuous lines of CFT's

- The $J^3 \bar{J}^3$ deformation

Standard choice : timelike Cartan generator

\Rightarrow geometry of the deformed CFT:

$$ds^2 = dr^2 + \frac{-\cosh^2 r dt^2 + \mathcal{R}^2 \sinh^2 r d\phi^2}{\mathcal{R}^2 \cosh^2 r - \sinh^2 r}$$

$$e^{2\Phi} = e^{2\Phi_0} \frac{\mathcal{R}^2 - 1}{\mathcal{R}^2 \cosh^2 r - \sinh^2 r}$$

★ **Spectrum of the theory**: change the radius of the J^3, \bar{J}^3 timelike lattice:

$$Z_{3\bar{3}}(\mathcal{R}) = 4\mathcal{R}k\sqrt{k-2} \int d^2s d^2t \frac{e^{\frac{2\pi}{\tau_2}(\text{Im}(s_1\tau-s_2))^2}}{|\vartheta_1(s_1\tau-s_2|\tau)|^2} \times$$

$$\times \sum_{m,w} e^{-\frac{k\pi}{\tau_2}|(s_1-t_1+w)\tau-(s_2-t_2+m)|^2} \sum_{m',w'} e^{\mathcal{R}^2 \frac{k\pi}{\tau_2}|(t_1+w')\tau-(t_2+m')|^2}$$

At first order (i.e. $\mathcal{R}^2 = 1 + \varepsilon$) :

$$\delta L_0 = \delta \bar{L}_0 = -\frac{\varepsilon}{k} \left(\tilde{m} + \frac{k}{2}w_+ \right) \left(\tilde{\bar{m}} + \frac{k}{2}w_+ \right)$$

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CIGAR/TRUMPET DUALITY ?

\Rightarrow Infinite deformation ($\mathcal{R} \rightarrow \infty$): *axial coset*, cigar geometry

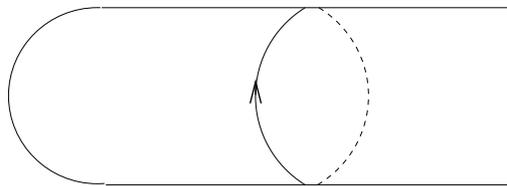
★ Spectrum: $L_0^{axial} = -\frac{j(j-1)}{k-2} + \frac{(n/2 - kw/2)^2}{k}$

\Rightarrow Opposite limit ($\mathcal{R} \rightarrow 0$): *vector coset*, trumpet geometry

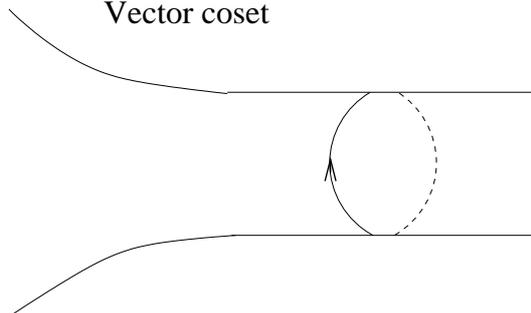
★ Spectrum: $L_0^{vector} = -\frac{j(j-1)}{k-2} + \frac{\mu^2}{k}$, with $\mu \in \mathbb{R}$.

Mismatch: choice of the *universal cover* of $SL(2, \mathbb{R})$

Axial coset



Vector coset



- The $J^2 \bar{J}^2$ deformation

Inequivalent choice of Cartan subalgebra: spacelike current J^2

\Rightarrow change the radius of the **spacelike** lattice in the partition function

Infinite deformation: *Minkowskian 2D black hole*

- Null deformation

In $SL(2, \mathbb{R})$, another inequivalent subalgebra: *null subalgebra* (currents $J = J^1 + J^3, \bar{J} = \bar{J}^1 + \bar{J}^3$)

\Rightarrow deform with the exactly marginal operator $J\bar{J}$

★ Partition function: change the radii of both lattices

\Rightarrow first order spectrum (continuous repr.):

$$L_0 = \frac{s^2 + 1/4}{k - 2} - w_+ [m + \frac{\varepsilon}{2}(m + \bar{m})] - \frac{k}{4}(1 + \varepsilon)w_+^2$$

Deformation acts on *spectral flow*

★ Infinite deformation limit: $U(1)_Q \times \mathbb{R}^{1,1}$

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- The supersymmetric null deformation

Continuous line of $N=2$ algebras interpolating between $SL(2, \mathbb{R}) \times SU(2)$ and $U(1)_Q \times \mathbb{R}^{1,1} \times SU(2)$ (parametrized by p) :

$$\begin{aligned} \sqrt{2}G^\pm &= \left[s_0(I^3 + i\partial H_2) \mp i(c \partial T + s \partial H_1) \right] e^{\pm iH_0} + s_0 I^\mp e^{\pm iH_2} \\ &\quad + i \left[c \partial X - (s_0 - s)(\partial H_1 - t \partial X^-) \mp i\partial\rho \right] e^{\pm i[H_1 - tX^-]} \\ J &= i\partial H_0 + i\partial H_2 + i\partial H_1 + ips^2 \left[\frac{1}{t}\partial T + \partial H_1 \right] - s_0^2 \mathcal{I}^3 \\ &\quad + (p-1)t i\partial X^- \end{aligned}$$

where $c = \cosh(\sigma)$, $s = \sinh(\sigma) = s_0/p$, with $s_0 = \sqrt{\frac{2}{k+2}}$ and $p \geq 1$

★ **Limit $s \rightarrow s_0$** : undeformed theory

★ **Limit $s \rightarrow 0$** : $U(1)_Q \times \mathbb{R}^{1,1} \times SU(2)$, nonstandard complex structure.

★ **New physical spin fields** (same projections) :

$$\Theta_\varepsilon^d(z) = \exp \left\{ \frac{i}{2} \left[\varepsilon_0 H_0 + \varepsilon_1 (H_1 + (p-1)t X^-) + \sum_{\ell=2}^4 \varepsilon_\ell H_\ell \right] \right\}$$

★ Locality w.r.t to the spectrum \Rightarrow **quantization of the deformation parameter**:

$$p \in 2\mathbb{Z} + 1$$

Right-moving sector: replace $\bar{X}^- \rightarrow \bar{X}^+$

\Rightarrow flip of chirality for the anti-holomorphic spin fields

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SOME COMMENTS ABOUT HOLOGRAPHY

- [AdS₃ holography](#)

Low energy limit of the D1/D5 theory ($\alpha' \rightarrow 0$)

\Rightarrow (full) near-horizon geometry: $AdS_3 \times S^3 \times T^4$ or $K3$

★ *Dual theory*: Dynamics of string-like instantons in D=6 SYM (Higgs branch) $\Rightarrow \mathcal{N} = (4, 4)$ SCFT in 2D on a deformation of the symmetric product $Sym(T^4 \text{ or } K3)^k$.

Maldacena, hep-th/9711200

- [Linear dilaton holography](#)

“Decoupling” limit of the NS5-branes: $\tilde{g}_s \rightarrow 0$, $\tilde{\alpha}'$ fixed.

\Rightarrow near-horizon limit of the NS5 background:

$$ds^2 = dx^\mu dx^\nu \eta_{\mu\nu} + \tilde{\alpha}' N_5 (d\rho^2 + d\Omega_3^2)$$

$$\Phi = \Phi_0 - \rho$$

$$H = 2\tilde{\alpha}' N_5 \epsilon(\Omega_3)$$

★ *Dual theory (type IIB)*: $\mathcal{N} = (1, 1)$ “gauge” theory in D=6. In the UV, new string-like degrees of freedom \Rightarrow

Little String Theory

★ *At low energies*: Super-Yang-Mills, gauge group $U(N_5)$.

Aharony, Berkooz, Kutasov, Seiberg, hep-th/9808149

★ *Free fixed point* in the IR (type IIB)

\Rightarrow *strong coupling problem*: distribute the five-branes on a circle or a three-sphere

Giveon, Kutasov, hep-th/9909110

Kiritsis, Kounnas, Petropoulos, Rizos, hep-th/0204201

- Null-deformed theory

From AdS_3/CFT_2 point of view : deform with (infra-red) **irrelevant** operator + decompactification limit
 \Rightarrow Best described as an **infrared regularization of LST**

★ **Worldsheet perspective**: marginal deformation of linear dilaton CFT

$$\delta S_{worldsheet} \sim M^2 \int d^2z e^{-\sqrt{\frac{2}{k+2}} \rho} \partial X^+ \bar{\partial} X^-$$

\Rightarrow Liouville potential with nontrivial $B_{\mu\nu}$, singlet of $\widehat{SU(2)}_L \times \widehat{SU(2)}_R$.

★ **D5-branes perspective**: add RR flux \Rightarrow generates imaginary “theta-like” term

$$S_{gauge} = \frac{1}{\alpha' g_s} \int \text{Tr} (F \wedge *F) - dt \wedge dx \wedge \text{Tr} (F \wedge F)$$

\Rightarrow “**instanton-like**” solutions contribute:

$$*_6 F = F \wedge dt \wedge dx$$

Infra-red fixed point: SCFT of AdS_3/CFT_2 correspondence

\Rightarrow dilaton stops running

★ **Null-deformed AdS_3** : RG flow between linear dilaton and AdS_3 holographic theories

Israel, Kounnas, Petropoulos

CONCLUSIONS

- Partition function for Minkowskian $SL(2, \mathbb{R})$, including flowed representations
- Spectra of marginal deformations of $SL(2, \mathbb{R})$: three left-right symmetric deformations \Rightarrow asymmetric ones?
- New decoupling limit of D1/D5 theory, S-dual to an exact SCFT: $\{\text{null-deformed } SL(2, \mathbb{R})\} \times SU(2) \times U(1)^4$
- Realization of worldsheet and target space supersymmetry for these theories
- Holographic interpretation: infra-red regularization of LST with “condensate” of fundamental strings
- Open problems:
 1. Other realizations of spacetime supersymmetry?
 2. Brane interpretation of other deformations?
 3. Explicit holography calculations...