

F. P. [arXiv:1204.4099](https://arxiv.org/abs/1204.4099).

See also [arXiv:0907.0765](https://arxiv.org/abs/0907.0765), etc...

Infrared-modified Universe

Federico Piazza



Outline

- Motivations (Inflation and Dark Energy unified)
- Strategy (Infrared-modified gravity)
- The basic FRW kinematics without a metric
- Extending the FRW paradigm
- Future directions: expanding metric space

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This Universe...

CDM-Big Bang theory is just great. Except that:

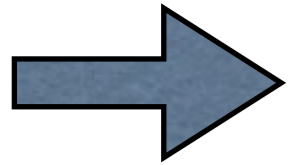
- 1) Distances($d_L(z), d_A(z)$) are not quite right at high z (“dark energy”)
- 2) We see homogeneity (and correlations!) on all angular scales (“inflation”)

Taken at face value these are both **INFRARED** problems: something going on at Hubble scales or beyond...

Why must they be unrelated phenomena in GR?

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Homogeneity and Isotropy

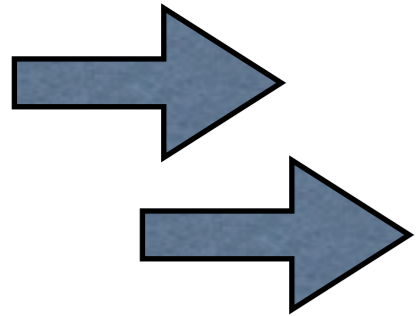


FRW metric

$$ds^2 = -dt^2 + a^2(t)dx^2$$

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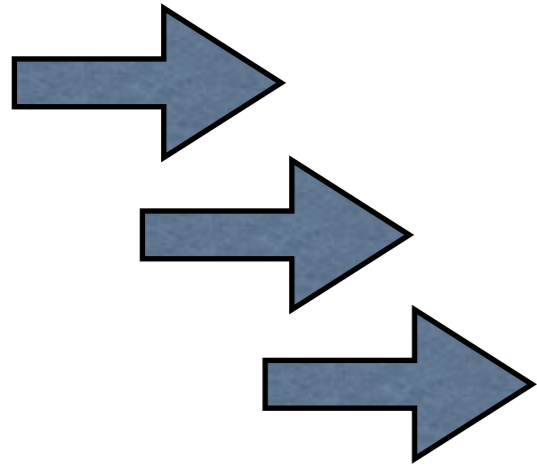


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one degree of freedom: the expansion $a(t)$

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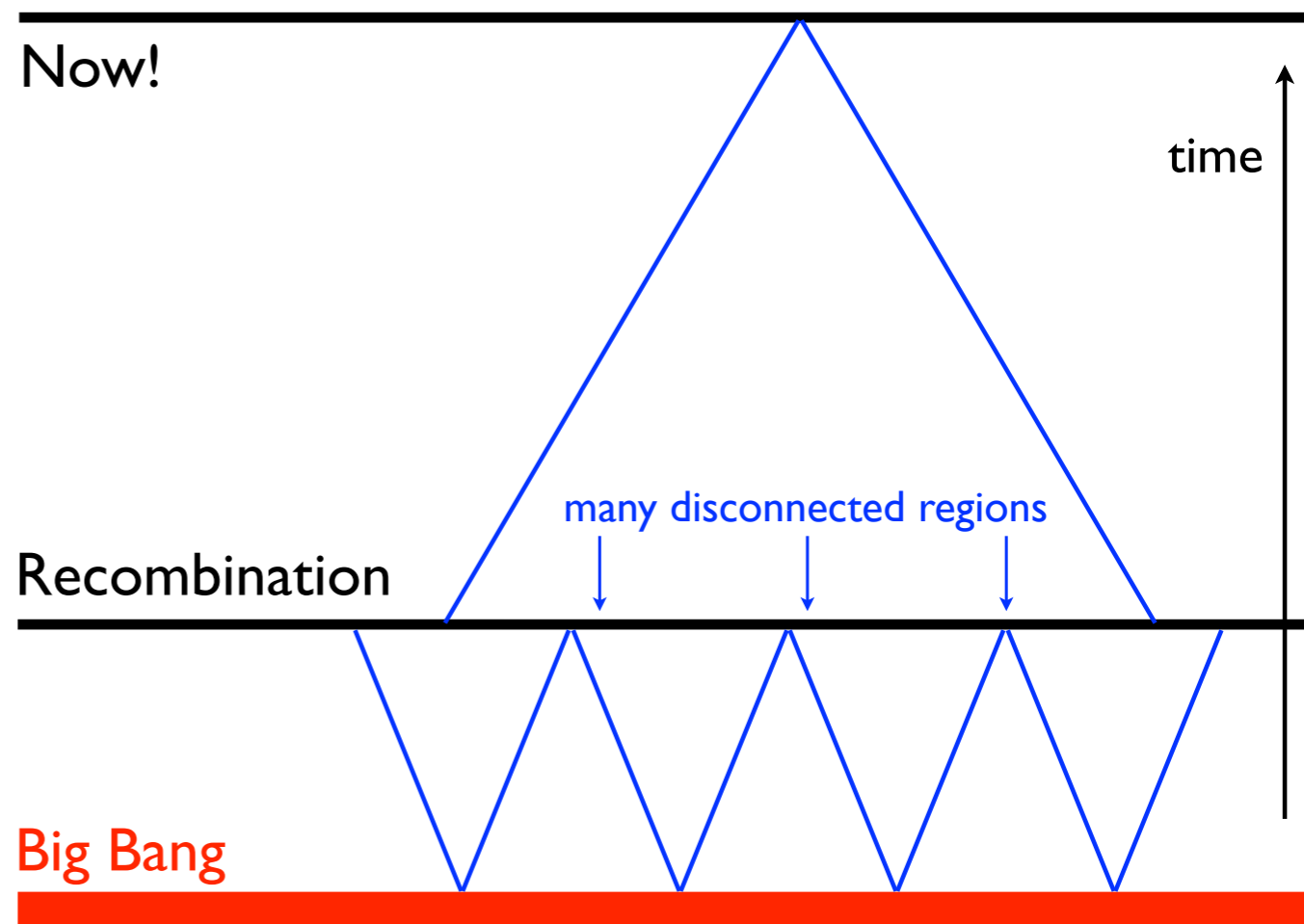
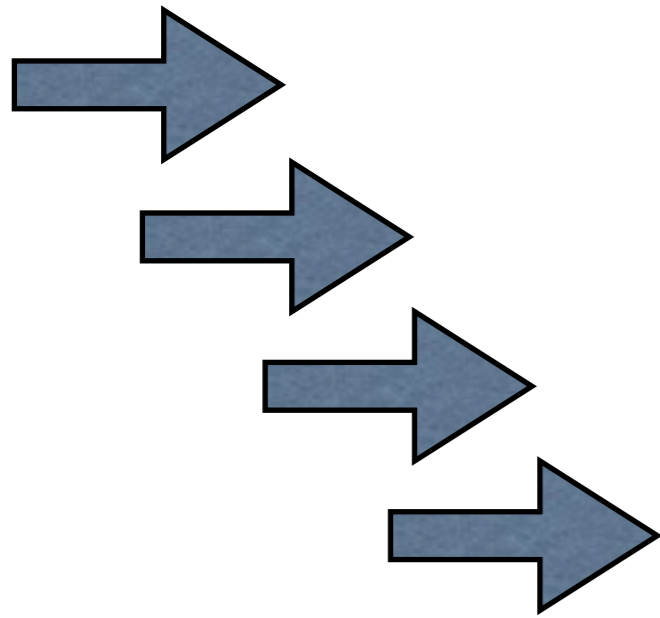
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causality follows



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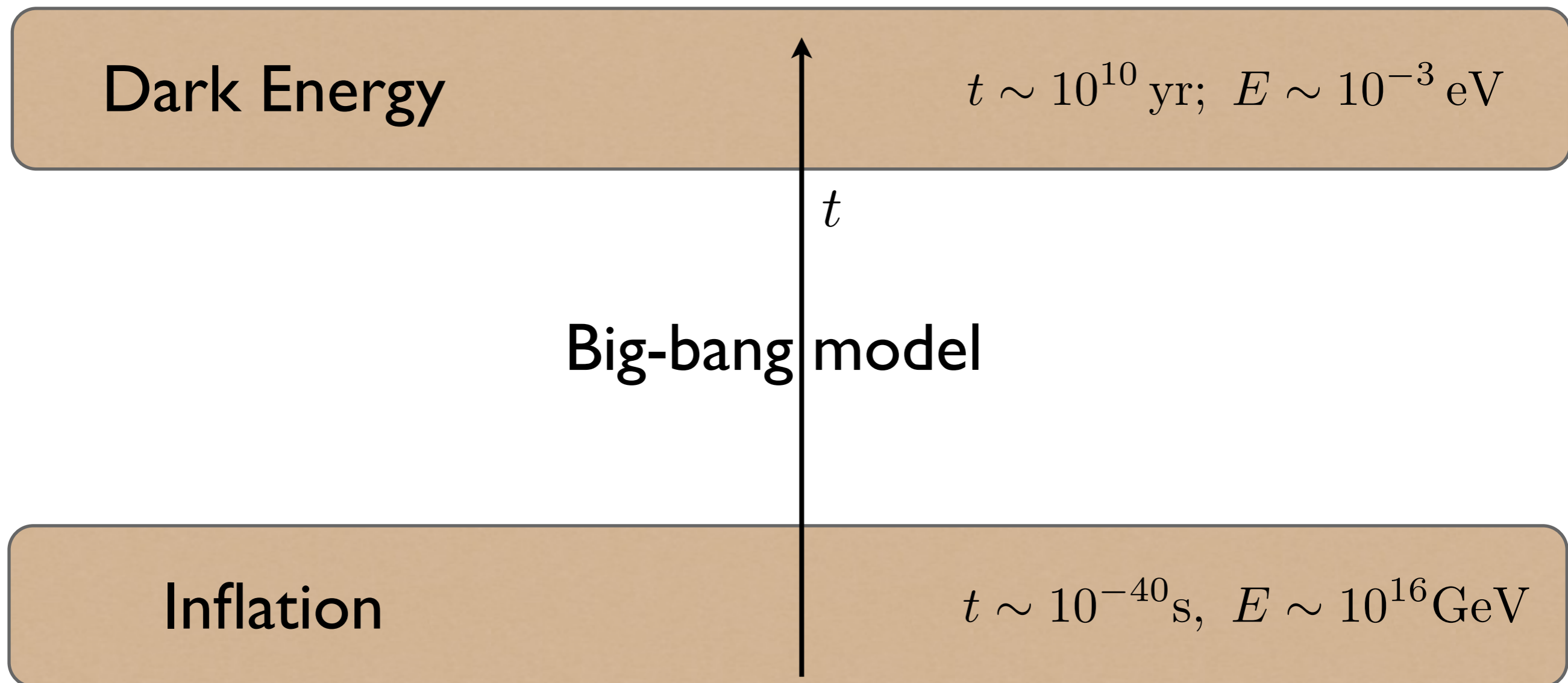
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Big-bang model

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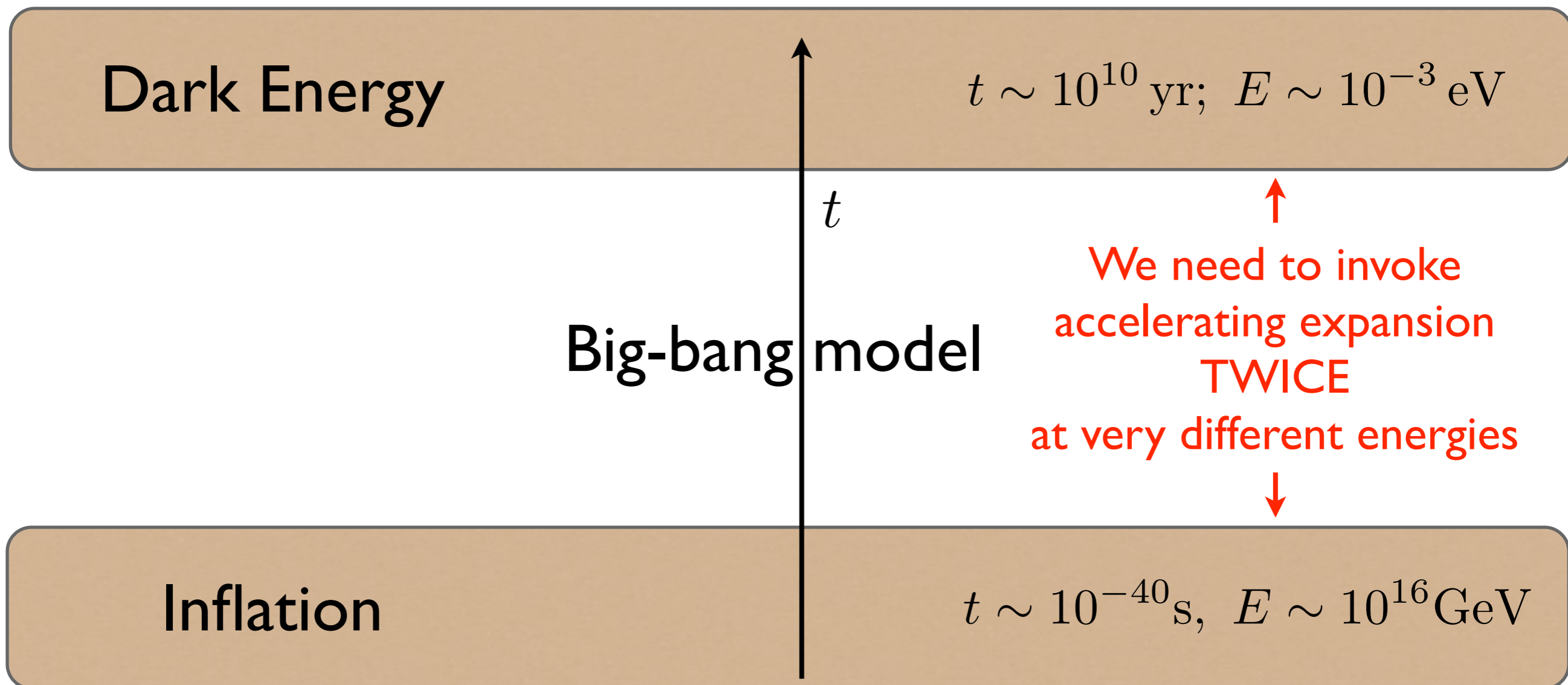
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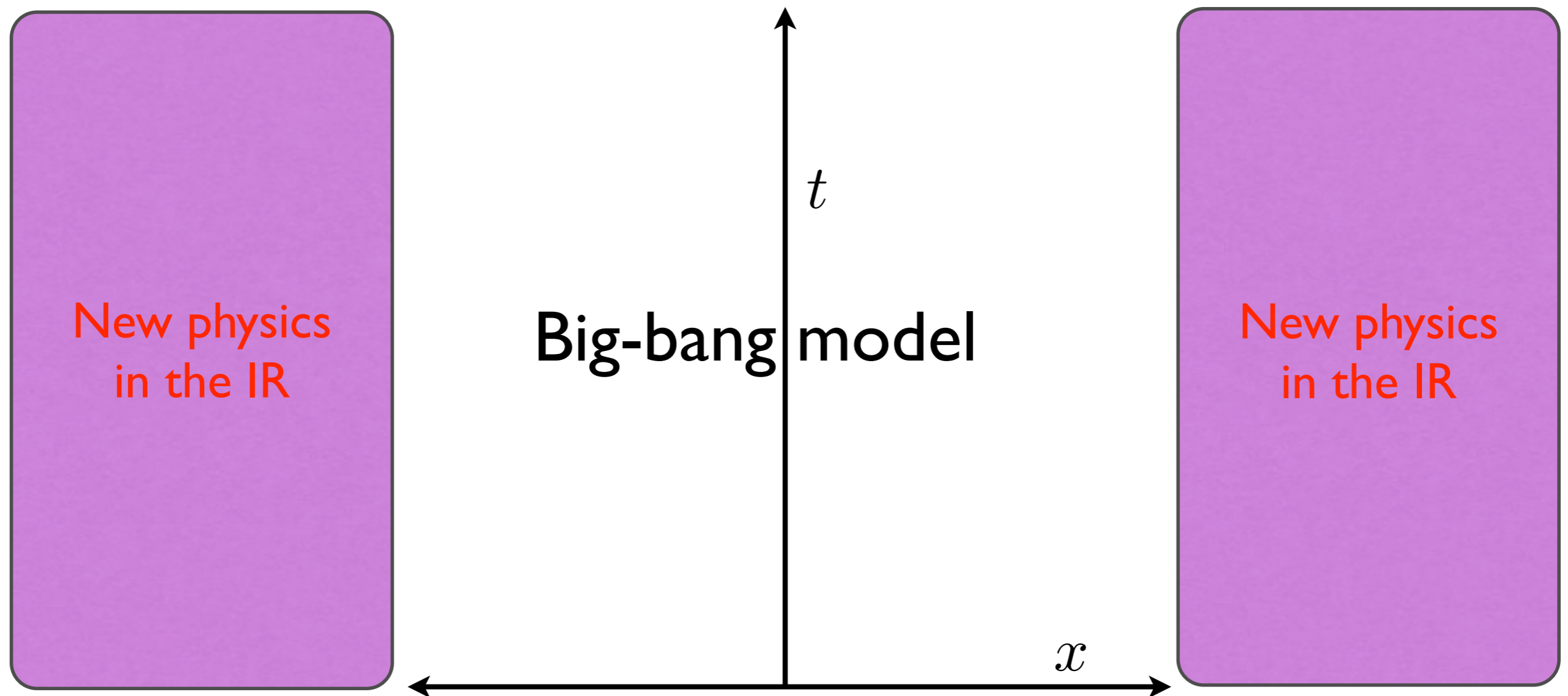


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THE IDEA

- 1) Keep the expansion as in the BB model as a **local** phenomenon
- 2) Change the GR geometrical description in the IR, i.e. at $d \sim H^{-1}$

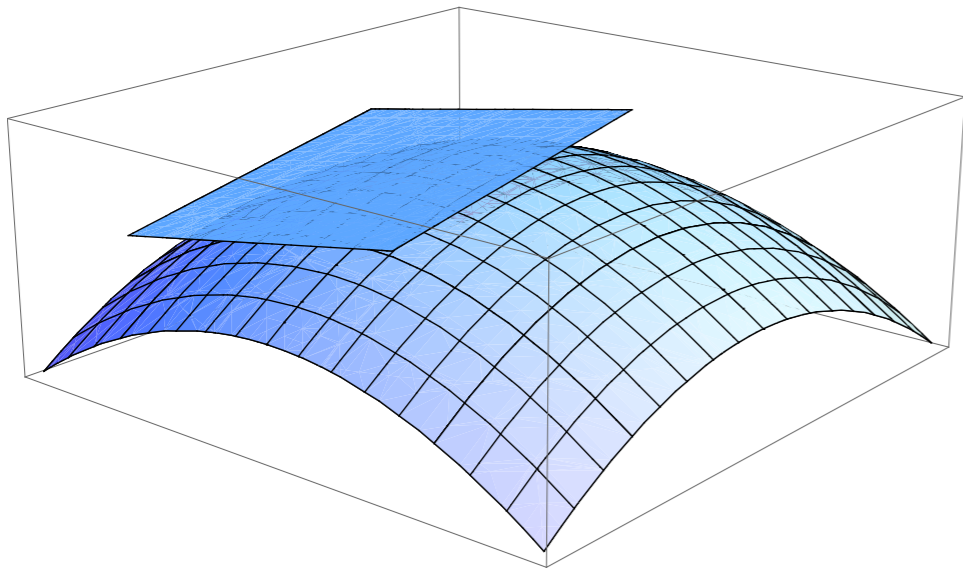


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As much as GR is an
IR modification of... flat space!

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- 5) Analogous to Tolman-Bondi models, but **homogeneous!**

connection with previous work:
The Extreme Equivalence Principle

F.P. arXiv:0907.0765, etc...

$$\langle T_0^0 \rangle_{\text{bare}} = \int d^3 k \left(k + \frac{f_{\text{quad}}(t)}{k} + \frac{f_{\text{log}}(t)}{k^3} + \dots \right)$$

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- 1) GR static spacetimes are unchanged
- 2) GR time dependent spacetimes: corrected

$$\dot{\vec{X}} = H \vec{X} (1 + g(X)) \quad g(X) \sim H^2 X^2 + \mathcal{O}(X^4)$$

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What to do without a metric: recipe

- 1) Scene: a flat, pre-relativistic (Newtonian) space
- 2) A set of privileged observers: the **comoving** ones
- 3) Consider one observer at $\vec{X} = 0$
- 4) The **Hubble velocity field** $\vec{h}(\vec{X})$: the velocity of the other comoving obs.
- 5) Give a prescription for **velocity transformations** among comoving obs.

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This will be our definition of homogeneity

Warm-up: FRW without GR

- 1) Note that velocities can be > 1
- 2) This is fine cause velocities defined somewhere else are not measurable
- 3) What needs to be at most one is the **local velocity**

$$v_{\vec{X}}(\vec{X}) \leq 1$$

- 4) A light ray is a curve $L(t)$ that has always unit local velocity:

$$\frac{d\vec{L}_{\vec{L}}(t)}{dt} = 1 \quad \longrightarrow \quad \frac{dL}{dt} = 1 + HL \quad \longrightarrow \quad \frac{dl}{d\tau} = 1$$

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IR-modified FRW (or: enforcing homogeneity)

Hubble velocity field $\vec{h}(\vec{X}) = H \vec{X} [1 + g(X; t)]$

This might happen also in a Tolman-Bondi...

Enforce homogeneity by postulating a velocity transformation

$$\vec{v}_{\vec{A}}(\vec{X}) = \left(\frac{\vec{v}(\vec{X})}{1 + g(X)} - H \vec{A} \right) \left(1 + g(|\vec{X} - \vec{A}|) \right)$$

$$\vec{h}_{\vec{A}}(\vec{X}) = \vec{h}(\vec{X} - \vec{A})$$

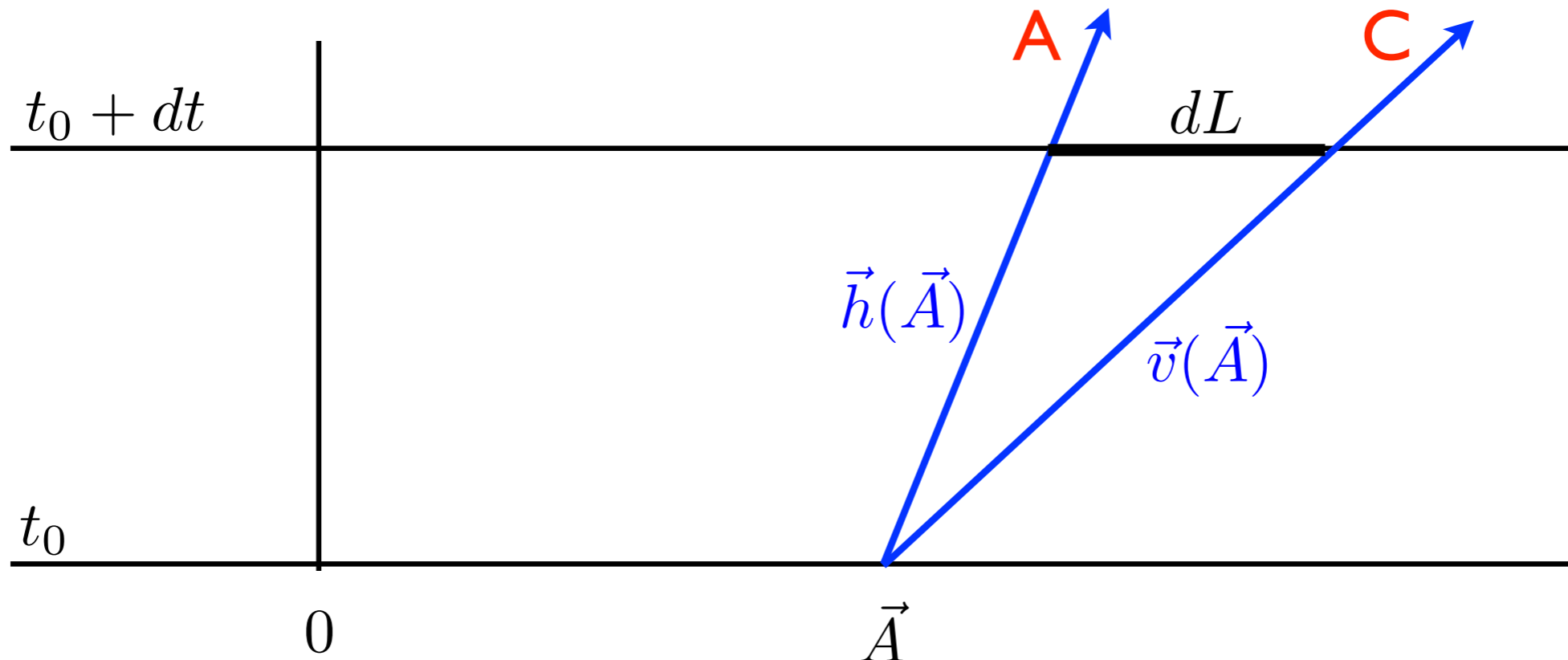
IR-modified FRW: light rays

As before, light rays have always **unit local velocity**

$$\frac{d\vec{L}_{\vec{L}}(t)}{dt} = 1 \quad \rightarrow \quad \frac{dL}{dt} = (1 + HL)(1 + g(L))$$

IR-modified FRW: the puzzle

- 1) Take a comoving observer **A** going with the Hubble flow
- 2) Take another non-comoving observer with velocity $\vec{v}(\vec{A})$ (from the origin)
- 3) They are close to each other but very far from 0

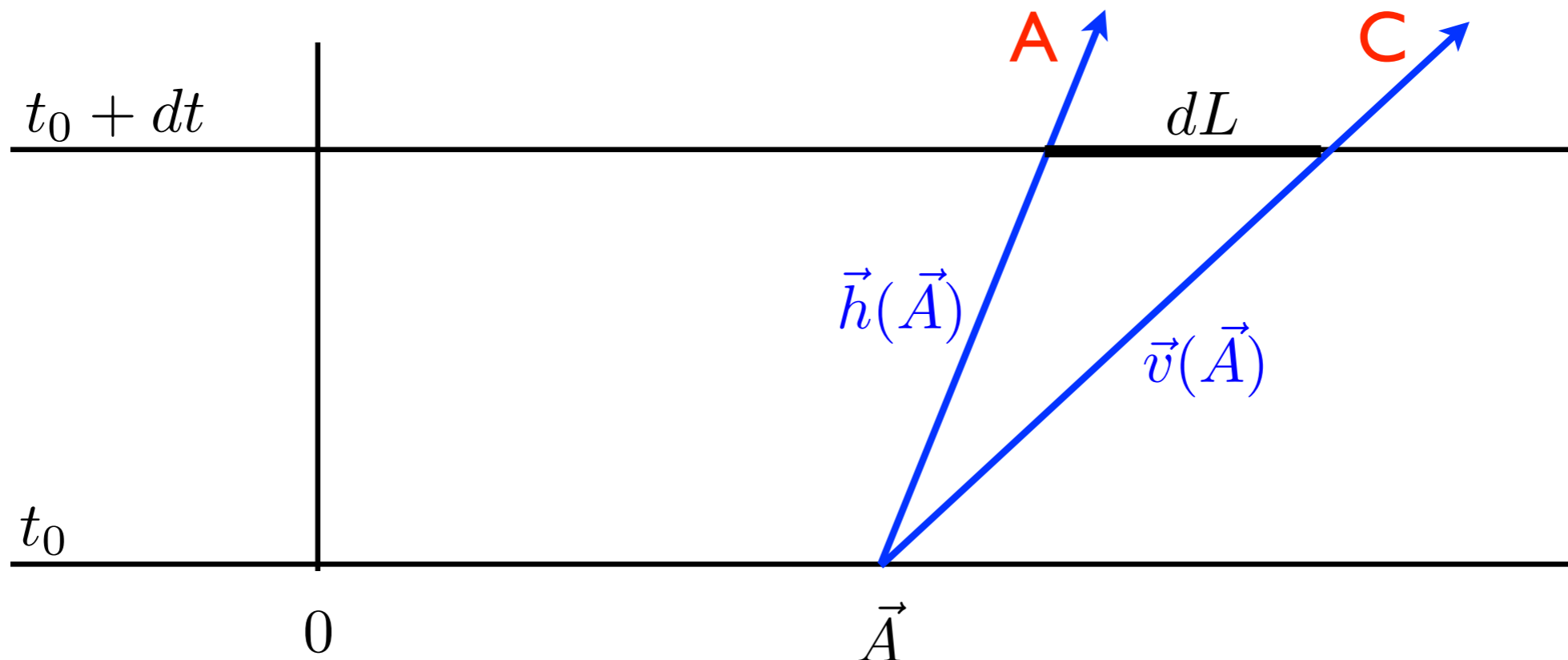


IR-modified FRW: the puzzle

After dt two different accounts of the distance dL :

locally: $d\vec{L} = \vec{v}_{\vec{A}}(\vec{A})dt$ from the distance: $d\vec{L} = (\vec{v}(\vec{A}) - \vec{h}(\vec{A}))dt$

$$d\vec{L}(\text{'seen from distance } X') = (1 + g(X))d\vec{L}$$



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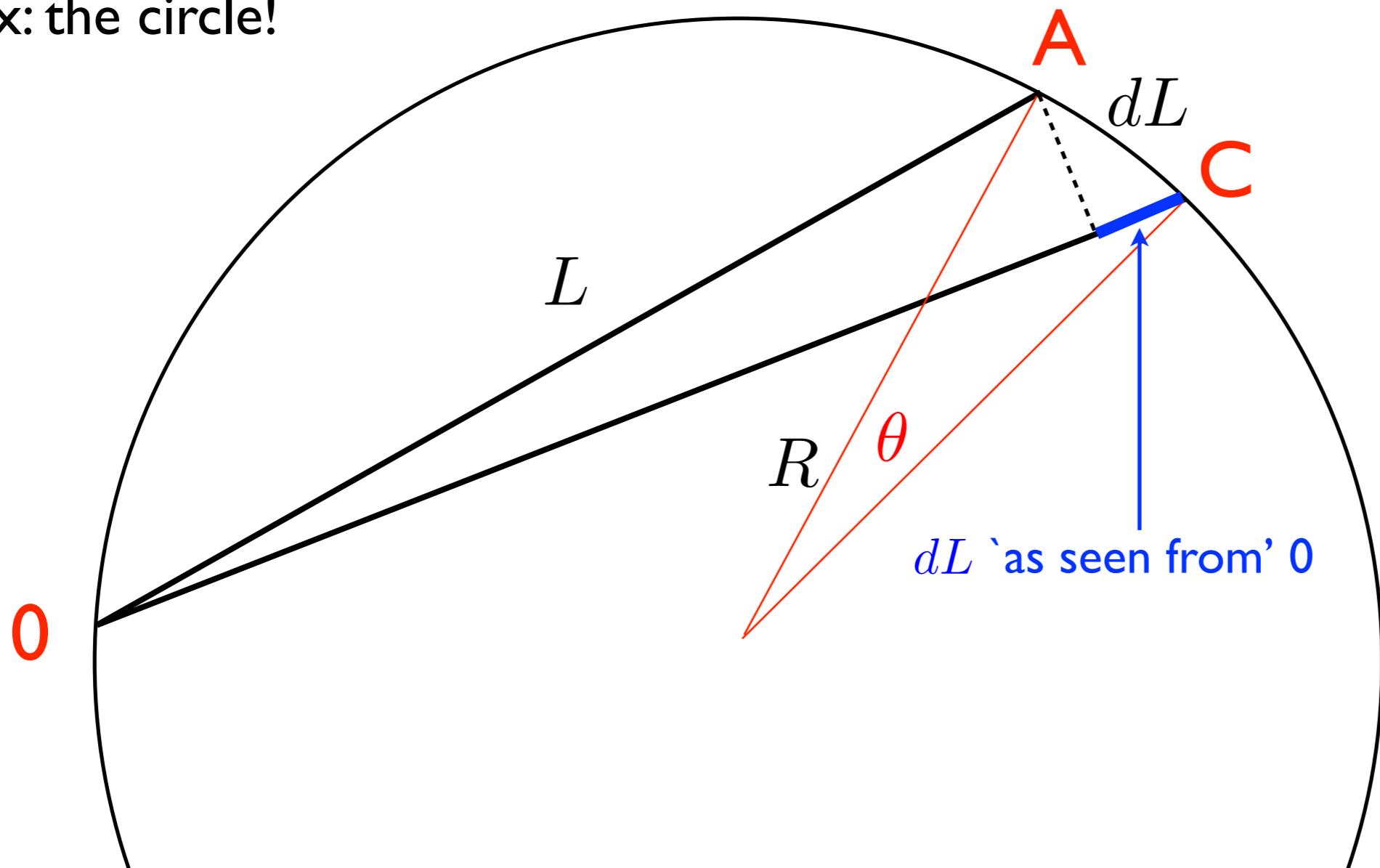
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- 1) In an expanding universe distances on $t=\text{const}$ slices do not add up
- 2) Therefore the observer 0 should not calculate d_L by a subtraction

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- 2) Therefore the observer 0 should not calculate dL by a subtraction
- 3) Ex: the circle!



IR-modified FRW: the proposal

- 1) Take the $t=\text{const}$ **metric manifold** of FRW (e.g. 3d flat space)
- 2) This is also a **metric space** at least locally (geodesic distance)
- 3) Take a **concave increasing function** of geodesic distance and define a new metric space
- 4) You can assign distances to any pair of points but not lengths to curves

Now!

time

Recombination

many disconnected regions

Big Bang

