

AdS/CONDENSED MATTER

SUPERGRAVITY HELPS CONDENSED MATTER PHYSICS.
A FIRST EXAMPLE: HOLOGRAPHIC SUPERCONDUCTORS

Francesco Aprile

Universitat de Barcelona
9 April 2013

AdS/CONDENSED MATTER

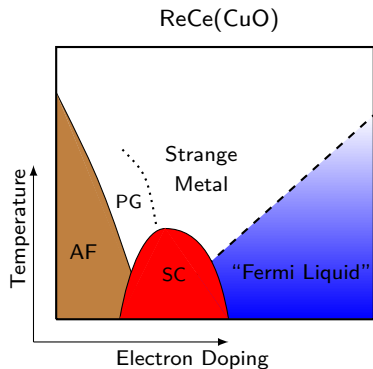
SUPERGRAVITY HELPS CONDENSED MATTER PHYSICS. A FIRST EXAMPLE: HOLOGRAPHIC SUPERCONDUCTORS

In collaboration with Jorge Russo, Diederik Roest, Andrea Borghese, Aldo Dector
Based on [1104.4473] [1206.5827] [1205.2087]

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- 1 Motivations
- 2 AdS/CFT and Hol. Superconductors: minimal structure
- 3 $\mathcal{N} = 2$ sugra coupled to $SU(2, 1)$ hypermultiplet
- 4 Probing the IR geometry: EE
- 5 Dual Field Theory and Marginal Deformations



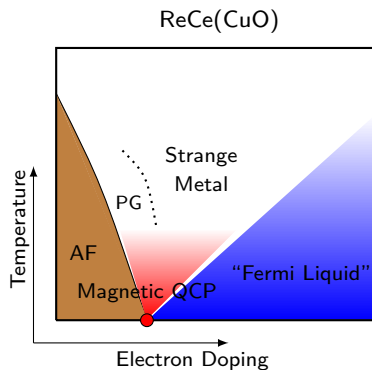
Non Fermi Liquid/ Non BCS some unconventional features

Strange Metal phase, examples:

- $\rho \approx T^n$ with n function of the doping and varying in $[1, 2]$.
- Drude tail falls off with non integer power law, example $w^{2/3}$.

High T_c SuperC phase, examples:

- d-wave order parameter
- T_c around 100K
- $C_e \approx T^n$ for $T < T_c$.



The Spin Fermion Model

$$\text{IR } E \ll \Lambda \quad \text{Spin-Fermion} \quad \Lambda \quad \text{AF} \quad E_0$$

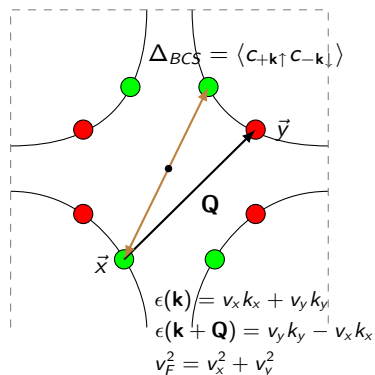
$$\mathcal{L}_{sf} = g c_{w,\mathbf{k}}^\dagger \vec{\sigma} c_{w-\Omega,\mathbf{k}-\mathbf{q}} \vec{S}_{\Omega,\mathbf{q}}$$

$$\mathcal{L}_f = c_{w,\mathbf{k}}^\dagger G_0^{-1}(w, \mathbf{k}) c_{w,\mathbf{k}}$$

$$\mathcal{L}_s = \chi_0^{-1}(\mathbf{q}, \Omega) S_{\Omega,\mathbf{q}} S_{\Omega,\mathbf{q}}$$

$$G_0(w, \mathbf{k})^{-1} = w - \epsilon(\mathbf{k})$$

$$\chi_0(\Omega, \mathbf{q})^{-1} = \left(\xi^{-2} + (\mathbf{q} - \mathbf{Q})^2 - (\Omega/v_s)^2 \right)$$



Hot spot: point $\vec{x} \in \text{FS}$ such that $\exists \vec{y}$ with
the property: $\vec{x} - \vec{y} = \mathbf{Q}$

Loop contr. organized in powers of $\lambda \sim \frac{g^2}{v_f \xi^{-1}}$

Results

- d-wave from BCS at H.S : $\Delta_{\mathbf{k}} = -\Delta_{\mathbf{k}+\mathbf{Q}}$.
- NFL from Loop corrections:

$$G_{H.S.}^{-1} \sim \text{sign} w \sqrt{i|w|} - \vec{v} \vec{k}$$

Limitations

- strong coupling
- No quasiparticle at H.S.
- Large N exp. not under control

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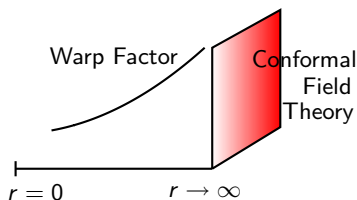
AdS/CFT MINIMAL STRUCTURE

Large N gauge theory
 d dimensions

Classical gravity
 $d + 1$ dimensions

aAdS $_{d+1}$ spacetime

$$ds^2 = \frac{r^2}{L^2}(-dt^2 + d\vec{x}^2) + \frac{L^2}{r^2}dr^2$$



scalars $m^2 = \Delta(\Delta - d)$

$$\phi(r, x_\mu) = \begin{cases} \phi_0/r^{\Delta_-} & \text{source} \\ \mathcal{O}/r^{\Delta_+} & \text{vev} \end{cases}$$

$$\begin{array}{l} \text{AdS} \quad \{t, \vec{x}\} \rightarrow \lambda\{t, \vec{x}\} \quad r \rightarrow r/\lambda \\ \text{CFT} \quad \{t, \vec{x}\} \rightarrow \{t, \vec{x}\}/s \quad E \rightarrow s E \end{array}$$

$$\left\langle \exp \int \phi_0 \mathcal{O} \right\rangle_{\text{CFT}} = \mathcal{Z}_{\text{Grav}}(\phi_0)$$

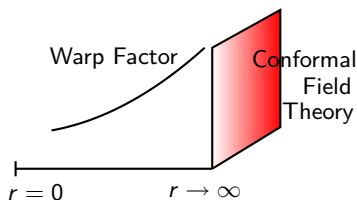
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$$\left\langle \exp \int \phi_0 \mathcal{O} \right\rangle_{\text{CFT}} = e^{-N^2 S_{\text{class}}(\phi)}$$

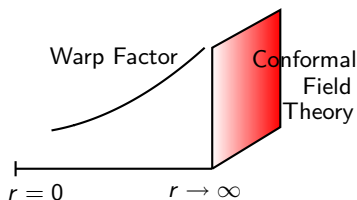
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AdS $_{d+1}$ spacetime

$$ds^2 = \frac{r^2}{L^2}(-dt^2 + d\vec{x}^2) + \frac{L^2}{r^2}dr^2$$



gauge boson $A = A_\mu dx^\mu$

$$A(r, x_\mu) = \begin{cases} \mathcal{S}_0 & \text{source} \\ \mathcal{J}/r^{d-2} & \text{vev} \end{cases}$$

$$\begin{array}{l} \text{AdS} \quad \{t, \vec{x}\} \rightarrow \lambda\{t, \vec{x}\} \quad r \rightarrow r/\lambda \\ \text{CFT} \quad \{t, \vec{x}\} \rightarrow \{t, \vec{x}\}/s \quad E \rightarrow s E \end{array}$$

$$\left\langle \exp \int (\mathcal{S}_0^\mu \mathcal{J}_\mu) \right\rangle_{\text{CFT}} = e^{-N^2 \mathcal{S}_{\text{class}}(A)}$$

BASIC LAGRANGIAN DENSITY

$$\mathcal{L}[g_{\mu\nu}, A_\mu, \zeta] = \frac{1}{2\kappa^2} \left[\mathcal{R} - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} D_\mu \zeta \overline{D^\mu \zeta} - V(|\zeta|) \right]$$

The ansatz

$$ds^2 = -g(r)e^{-\chi(r)} dt^2 + \frac{dr^2}{g(r)} + r^2 d\vec{x}_d^2,$$

$$A_\mu dx^\mu = \Phi(r) dt$$

$$|\zeta| = \eta(r)$$

| | |
|-------------------------|-------------------------|
| $g(r_h)$ | Eq. I order for g |
| $\chi(r_h)$ | Eq. I order for χ |
| $\Phi(r_h), \Phi'(r_h)$ | Eq. II order for Φ |
| $\eta(r_h), \eta'(r_h)$ | Eq. II order for η |
| | → 6 + 1 parameters |

BASIC LAGRANGIAN DENSITY

$$\mathcal{L}[g_{\mu\nu}, A_\mu, \zeta] = \frac{1}{2\kappa^2} \left[\mathcal{R} - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} D_\mu \zeta \overline{D^\mu \zeta} - V(|\zeta|) \right]$$

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$$ds^2 = -g(r)e^{-\chi(r)} dt^2 + \frac{dr^2}{g(r)} + r^2 d\vec{x}_d^2, \quad A_\mu dx^\mu = \Phi(r) dt$$
$$|\zeta| = \eta(r)$$

Eq. I order for g 7 - 2 = 5

Eq. I order for χ

Eq. II order for Φ 2 scalings

Eq. II order for η

→ 6 + 1 parameters

- fix the value of r_h
- $\chi(r_h) = \chi_0$

BASIC LAGRANGIAN DENSITY

$$\mathcal{L}[g_{\mu\nu}, A_\mu, \zeta] = \frac{1}{2\kappa^2} \left[\mathcal{R} - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} D_\mu \zeta \overline{D^\mu \zeta} - V(|\zeta|) \right]$$

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$$|\zeta| = \eta(r)$$

Eq. I order for g

$$5 - 2 = 3$$

Eq. I order for χ

Eq. II order for Φ

because $g(r) \sim (r - r_h)$

Eq. II order for η

- $\Phi(r) \sim \Phi_0(r - r_h)$
- $\eta'(r_h) \propto \eta(r_h) \equiv \eta_0$

→ 6 + 1 parameters

BASIC LAGRANGIAN DENSITY

$$\mathcal{L}[g_{\mu\nu}, A_\mu, \zeta] = \frac{1}{2\kappa^2} \left[\mathcal{R} - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} D_\mu \zeta \overline{D^\mu \zeta} - V(|\zeta|) \right]$$

The ansatz

$$ds^2 = -g(r)e^{-\chi(r)} dt^2 + \frac{dr^2}{g(r)} + r^2 d\vec{x}_d^2, \quad A_\mu dx^\mu = \Phi(r) dt$$
$$|\zeta| = \eta(r)$$

Eq. I order for g

$$3 - 1 = 2$$

Eq. I order for χ

Eq. II order for Φ

$g'(r_h)$ gives the Temperature
and depends on (η_0, Φ_0)

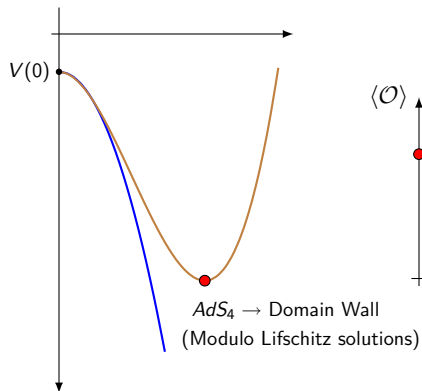
Eq. II order for η

→ 6 + 1 parameters

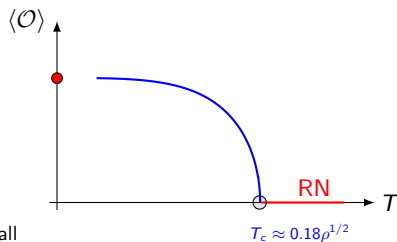
(η_0, Φ_0) to set the source = 0.

TWO SIMPLE POTENTIALS

$$V = -6 - m^2|\zeta|^2$$

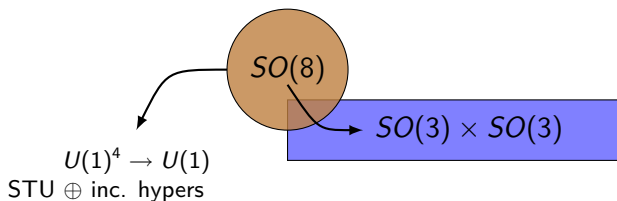


$$V = -6 - m^2|\zeta|^2 + \lambda|\zeta|^4$$



SCALAR MANIFOLD FROM $\mathcal{N} = 8$ $d = 4$

$$\mathcal{L}_{scalar} = \frac{1}{2} \partial^\mu \eta \partial_\mu \eta - \mathcal{J}(\eta) A_\mu A^\mu - V(\eta)$$



$$\mathcal{J}_1 = \sinh^2 \left(\frac{\eta}{2} \right)$$

$$\mathcal{J}_2 = \frac{1}{4} \sinh^2(\eta)$$

$$V_1 = -2(2 + \cosh \eta)$$

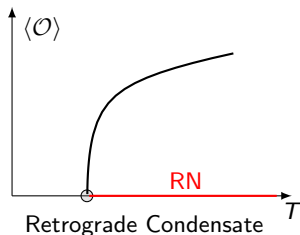
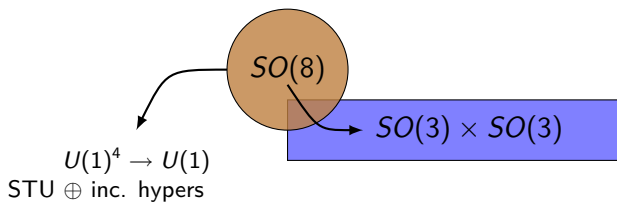
$$V_2 = \frac{1}{2} \sinh^4 \left(\frac{\eta}{2} \right) + V_1$$

Unexpected condensation

Similar to the Abelian Higgs model

SCALAR MANIFOLD FROM $\mathcal{N} = 8$ $d = 4$

$$\mathcal{L}_{scalar} = \frac{1}{2} \partial^\mu \eta \partial_\mu \eta - \mathcal{J}(\eta) A_\mu A^\mu - V(\eta)$$



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Similar to the Abelian Higgs model

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THE $\mathcal{N} = 2$ SUPERGRAVITY SETUP: BOSONIC SECTOR

- ▶ graviton multiplet = { gravity \oplus graviphoton }.
- ▶ Hyperscalars q^μ parametrize a \mathcal{Q} Kahler manifold: $(J^x)_u^\nu, H_{uv}$
- ▶ The $SU(2)$ group of R-symmetry acts on the hyperscalars.
- ▶ The gauge group is introduced by gauging compact isometries (Killing vectors K_λ^μ) of \mathcal{Q} .

As a consequence of the gauging procedure, the Lagrangian gets a unique scalar potential.

$$V = 2g^2 \left(4H^{uv} \partial_u \mathcal{W} \partial_v \mathcal{W} - 3\mathcal{W}^2 \right), \quad \mathcal{W} = \sqrt{\frac{2}{3} P^x P^x}$$

$$2n_H P_\lambda^x = (J^x)_u^\nu \nabla_\nu K_\lambda^\mu = (J^x)_u^\nu (\partial_\nu K_\lambda^\mu - \Gamma_{\nu\rho}^\mu K_\lambda^\rho)$$

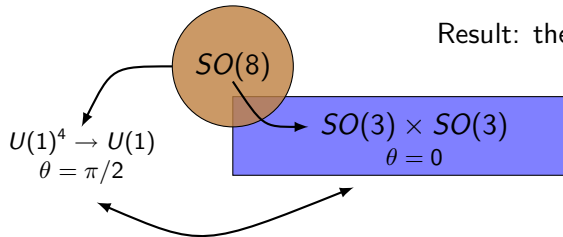
THE UNIVERSAL HYPERMULTIPLYT $SU(2,1)/U(2)$

$\dim_{\mathbb{R}} SU(2,1)/U(2) = 4$. The coset space is top. a ball in \mathbb{C}^2

$$\zeta_1 = \tau \cos \frac{\theta}{2} e^{i(\varphi+\psi)/2} \quad \zeta_2 = \tau \sin \frac{\theta}{2} e^{-i(\varphi-\psi)/2}$$

$$H_{uv} dq^u dq^v = \frac{d\tau^2}{(1-\tau^2)^2} + \frac{\tau^2}{4(1-\tau^2)} (\sigma_1^2 + \sigma_2^2) + \frac{\tau^2}{4(1-\tau^2)^2} \sigma_3^2$$

Isotropy group is $U(2) = SU_R(2) \times U(1)$ with $U(1)_3 \subset SU_R(2)$



Result: the gauging of $U(1)_3$ builds the bridge

$$R[\zeta_1] = +1$$

$$R[\zeta_2] = -1$$

$$\tau = \tanh \frac{\eta}{2}$$

THE UNIVERSAL HYPERMULTIPLYET $SU(2,1)/U(2)$

Idea: If θ can be fixed arbitrarily in the range $[0, \pi/2]$ we find a new family of solutions interpolating between 1 – 2.

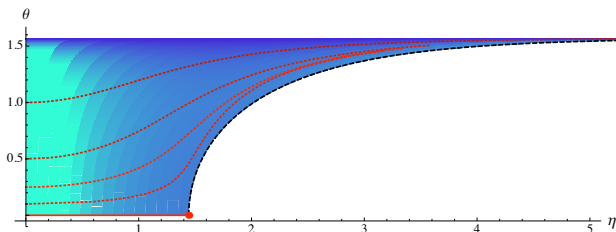
...from this point of view the retrograde condensate can be used as a clue to detect the existence of a bigger family of sol. $\rightarrow d = 5 \mathcal{N} = 8$

UV Asymptotics η : $d = 4$ and $m^2 L^2 = -2 \rightarrow \Delta_- = 1$ and $\Delta_+ = 2$

$$\eta(r) = \frac{\mathcal{O}_1}{r} + \frac{\mathcal{O}_2}{r^2} + \dots, \quad \theta(r) = \theta_\infty + \frac{\xi}{r} + \dots;$$

$$\mathcal{O}_2 = 0 \rightarrow \Delta = 1 \text{ Condensate}$$

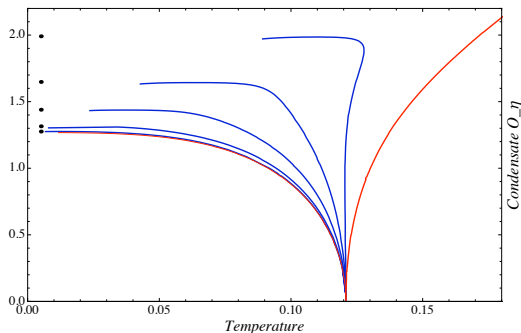
THE POTENTIAL



- ▶ The red dot is the saddle point $\theta = 0$, $\eta = 2 \operatorname{arccosh}\sqrt{5}$.
- ▶ The red lines, are the horizon values of the functions $\theta(r)$ and $\eta(r)$.
- ▶ The value of θ_∞ can be read on the vertical axis.

$\theta_\infty \neq 0$ the superconductor is driven towards $\theta(r_h) = \pi/2$ as $T \rightarrow 0$.

$\Delta = 1$ CONDENSATES: NUMERICS



- From bottom to top $\theta_\infty = 0, 0.1, 0.25, 0.5, 0.75, 1$
- First order phase transitions for $\theta_\infty > \theta_{cr} \approx .95$.

(the curves should be represented in a 3d space according to their value of θ_∞)

EXTREMAL SOLUTIONS FOR $\theta_\infty \neq 0$: PHASE II

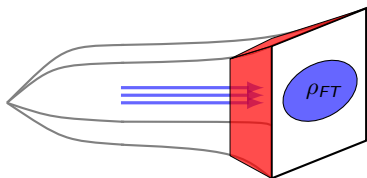
$$+dz^2 + dr^2 + r^2 dM^2$$

$$\cos \alpha = C_\eta$$

$$z/r = \pm \tan \alpha$$

$$dr^2 + r^2 \cos^2 \alpha dM^2$$

cone geometry



$r = 0$

$r \rightarrow \infty$

UV AdS_4

2 Hints:

- $\theta(r_h) \rightarrow \pi/2$

- Solitons with large mass converge to extremal Hol.SC.

$$ds^2 = r^2(-dt^2 + d\vec{x}^2) + \frac{dr^2}{r^2 + C_\eta^2}, \quad \eta(r) = 2 \operatorname{arcsinh} \frac{C_\eta}{r}$$

$$\theta(r) = \frac{\pi}{2} + \delta_\theta r \quad \Phi(r) = \delta_\Phi r$$

EXTREMAL SOLUTIONS FOR $\theta_\infty \neq 0$: PHASE II

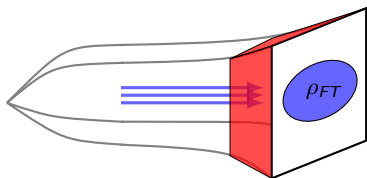
$$-dz^2 + dr^2 + r^2 dM^2$$

$$\cosh \alpha = C_\eta$$

$$z/r = \pm \tanh \alpha$$

$$dr^2 + r^2 \cosh^2 \alpha dM^2$$

cone geometry



$r = 0$

$r \rightarrow \infty$

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2 Hints:

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$$\theta(r) = \frac{\pi}{2} + \delta r \quad \Phi(r) = \delta r$$

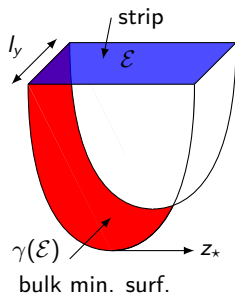
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- Entanglement Entropy

$$S(\mathcal{E}) = -\text{Tr} \rho_{\mathcal{E}} \log \rho_{\mathcal{E}}, \quad \rho_{\mathcal{E}} = \text{Tr}_{\bar{\mathcal{E}}} |gs\rangle\langle gs|$$

- Excitations $\left\{ \begin{array}{l} \text{vector type} \\ \text{conductivity} \\ \text{fermionic type} \end{array} \right.$

- Entanglement Entropy



$$ds_{sp}^2 = \frac{L^2}{z^2}(dx^2 + dy^2 + U(z)dz^2)$$

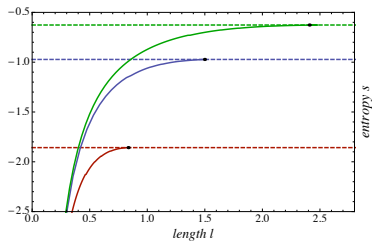
$$S(\mathcal{E}) = \frac{2\pi L^2}{\kappa^2} \text{Area}(\gamma_{\mathcal{E}})$$

$$S(\mathcal{E}) = \frac{4\pi L^2}{\kappa^2} l_y \left(s + \frac{1}{\epsilon} \right)$$

$$s = 2L^2 l_y \int_{\epsilon}^{z_*} \frac{dz}{z^2} \sqrt{U(z) + x'(z)^2}$$

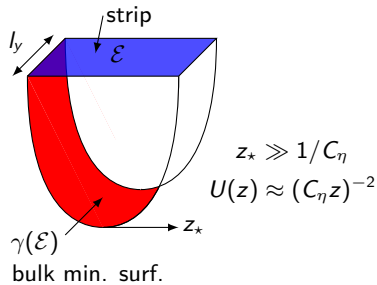
$$\frac{l_x}{2} = \int_{\epsilon}^{z_*} dz \frac{z^2}{z_*^2} \sqrt{\frac{U(z)}{1 - (z/z_*)^4}}$$

PROBING THE IR GEOMETRY: EE AT $T = 0$



From top to bottom

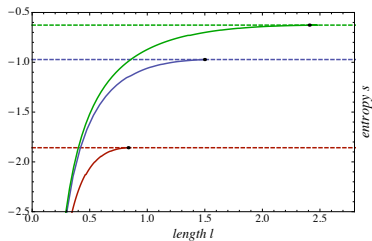
$$\theta_\infty = 0.5, 1., 1.4.$$



$$\frac{l_x}{2} = z_* \int_\epsilon^1 dz \frac{z^2}{\sqrt{1-z^4}} U(z z_*)^{1/2}$$

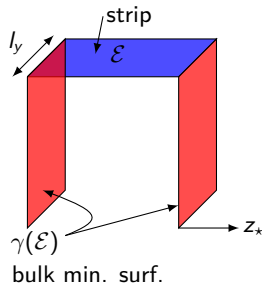
$$\frac{l_x}{2} \sim \text{const} \frac{1}{C_\eta}$$

PROBING THE IR GEOMETRY: EE AT $T = 0$



From top to bottom

$$\theta_\infty = 0.5, 1., 1.4.$$



$$s = 2L^2 l_y \int_\epsilon^{z_*} \frac{dz}{z^2} \sqrt{U(z)}$$

$$z_* \gg \frac{1}{C_\eta}$$

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$$\eta(r) = \frac{\mathcal{O}}{r} + \dots, \quad \theta(r) = \theta_\infty + \frac{\xi}{r} + \dots$$

$\Delta = 1$ Condensate

$$\zeta_1(r) = \tanh \frac{\eta(r)}{2} \cos \frac{\theta(r)}{2}, \quad \zeta_2(r) = \tanh \frac{\eta(r)}{2} \sin \frac{\theta(r)}{2}$$

$$\eta(r) = \frac{\mathcal{O}}{r} + \dots, \quad \theta(r) = \theta_\infty + \frac{\xi}{r} + \dots$$

$\Delta = 1$ Condensate

$$\zeta_1(r) = \frac{\mathcal{O}_1^{(1)}}{r} + \frac{\mathcal{O}_1^{(2)}}{r^2} + \dots, \quad \zeta_2(r) = \frac{\mathcal{O}_2^{(1)}}{r} + \frac{\mathcal{O}_2^{(2)}}{r^2} + \dots$$

$$\mathcal{O}_1^{(1)} = \frac{1}{2} \mathcal{O} \cos \frac{\theta_\infty}{2} \quad \mathcal{O}_1^{(2)} = -\frac{1}{4} \mathcal{O} \xi \sin \frac{\theta_\infty}{2}$$

$$\mathcal{O}_2^{(1)} = \frac{1}{2} \mathcal{O} \sin \frac{\theta_\infty}{2} \quad \mathcal{O}_2^{(2)} = \frac{1}{4} \mathcal{O} \xi \cos \frac{\theta_\infty}{2}$$

The dictionary is $\zeta_1 \rightarrow \Delta = 1$ Op. i.e. opposite quant.
 $\zeta_2 \rightarrow \Delta = 2$ Op.

- Double trace deformation! $\mathcal{O}_2^{(1)} = \lambda \mathcal{O}_1^{(1)}$ and $\mathcal{O}_1^{(2)} = -\lambda \mathcal{O}_2^{(2)}$

The marginal coupling is $\lambda = \tanh \frac{\theta_\infty}{2}$

$$\mathcal{O}_1^{(1)} = \frac{1}{2} \mathcal{O} \cos \frac{\theta_\infty}{2} \quad \mathcal{O}_1^{(2)} = -\frac{1}{4} \mathcal{O}_\xi \sin \frac{\theta_\infty}{2}$$

$$\mathcal{O}_2^{(1)} = \frac{1}{2} \mathcal{O} \sin \frac{\theta_\infty}{2} \quad \mathcal{O}_2^{(2)} = \frac{1}{4} \mathcal{O}_\xi \cos \frac{\theta_\infty}{2}$$

The dictionary is $\zeta_1 \rightarrow \Delta = 1$ Op. i.e. opposite quant.
 $\zeta_2^\dagger \rightarrow \Delta = 2$ Op.

- Double trace deformation! $\mathcal{O}_2^{(1)\dagger} = \lambda \mathcal{O}_1^{(1)}$ and $\mathcal{O}_1^{(2)} = -\bar{\lambda} \mathcal{O}_2^{(2)\dagger}$

Taking into account the charges $\zeta_1 \leftrightarrow \zeta_2^\dagger$. Then, $\lambda = \tanh \frac{\theta_\infty}{2} e^{-i\psi}$

$$\mathcal{O}_1^{(1)} = \frac{1}{2} \mathcal{O} \cos \frac{\theta_\infty}{2} e^{i(\phi+\psi)/2} \quad \mathcal{O}_1^{(2)} = -\frac{1}{4} \mathcal{O} \xi \sin \frac{\theta_\infty}{2} e^{i(\phi+\psi)/2}$$

$$(\mathcal{O}_2^{(1)})^\dagger = \frac{1}{2} \mathcal{O} \sin \frac{\theta_\infty}{2} e^{i(\phi-\psi)/2} \quad (\mathcal{O}_2^{(2)})^\dagger = \frac{1}{4} \mathcal{O} \xi \cos \frac{\theta_\infty}{2} e^{i(\phi-\psi)/2}$$

DUAL FIELD THEORY

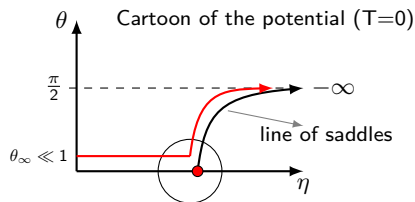
Marginal deformation

$$\int d^3x (\lambda \mathcal{O}_1 \mathcal{O}_2 + \bar{\lambda} \mathcal{O}_1^\dagger \mathcal{O}_2^\dagger) \quad \mathcal{O}_2^{(2)\dagger} = \frac{1}{2} \xi \mathcal{O}_1^{(1)} e^{-i\psi} .$$

We interpret $\theta(r)$ in an RG fashion:

$\theta_\infty \neq 0$ in the UV, drives the theory to $\theta(0) = \pi/2$ in the IR.

This value is associated to the confining background \rightarrow Issue on $\lambda!$



λ exactly marginal but the confining IR phase has to be associated to a relevant def.

$$\theta(r) = \theta_\infty + \frac{\xi}{r} + \dots$$

$$\xi = 0 \leftrightarrow \theta(r) = \text{const.}$$

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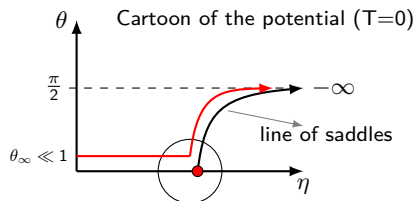
Marginal deformation

$$\sim \int d^3x \left(\xi \mathcal{O}_1^\dagger \mathcal{O}_1 \right) \quad \mathcal{O}_2^{(2)\dagger} = \frac{1}{2} \xi \mathcal{O}_1^{(1)} e^{-i\psi} .$$

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CONCLUSIONS

We have found new holographic superconductor solutions in $\mathcal{N} = 8$ sugra where:

- The topology of the underlying $\mathcal{N} = 2$ model plays an important role
- The back-reaction changes the IR physics of the solutions and this IR physics is geometrically understood

It may be that a similar story holds for the 5D $\mathcal{N} = 8$.

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We have find new holographic superconductor solutions in $\mathcal{N} = 8$ sugra where:

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Thanks for the attention!!