Quarkonium dissociation by anisotropy in a strongly coupled plasma

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Based on 1208.2672 (and 1202.3696) in collaboration with D. Fernandez, D. Mateos and D. Trancanelli

Plan for the talk

Motivation

• The AdS/CFT toolkit

• Quarkonium physics

Conclusions

For the creation of the quark gluon plasma

400 nucleons go in



Energy of CM 200 GeV

8000 hadrons are produced



1-10 GeV per hadron

The time evolution of the quark gluon plasma



 $\tau_{\rm iso} \lesssim 1 {\rm fm}$

[Romantschke et al; Mrowczynski et al.]

 $z \equiv$ longitudinal direction

 $x, y \equiv$ transverse direction



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→ Some observables are sensitive to the presence of an anisotropy

- Quarkonium physics (J/Ψ) [Dumitru et al.; Philipsen et al.]
- Momentum broadening [Dumitru et al.; Mehtar-Tani; Romantschke et al.]

About quarkonium in heavy ion collisions:

→ Quarkonium refers to charm-anticharm mesons (J/Ψ , Ψ' , χ_c , ...) and bottom-antibottom mesons (Υ , Υ' , ...)

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- \rightarrow RHIC data: J/Ψ suppression in nucleus-nucleus collisions when compared to proton-proton collisions.

 J/Ψ mesons are screened in the quark gluon plasma

It is important to understand how they are screened by the QGP

- \rightarrow What is the effect of the anisotropy?
- They might be moving with significant transverse momentum through the hot medium, what is the effect of such "wind"?

We will use the AdS/CFT correspondence to address this questions



 $\mathcal{N} = 4$ SYM at finite temperature = Schwarzschild AdS black hole



Note: we will refer to this metric as the isotropic metric

External quark — Fundamental string



• A fundamental string extending from the boundary at u = 0 to the horizon corresponds to an infinitely massive quark.

• The string endpoint represents the quark, while the rest of the string codifies the profile of the gluonic field

meson (bound state) — U-shaped string



meson (bound state) moving - U-shaped string moving at at constant velocity

constant velocity



meson (bound state) moving = U-s at constant velocity con

U-shaped string moving at constant velocity



But we are interested in studying an anisotropic strongly coupled plasma

How can we do that using the AdS/CFT correspondence?

The gauge theory that we will consider is a deformation of $\mathcal{N} = 4$ SYM



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---> The axion is magnetically sourced by D7-branes

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Finally, putting all these ingredients together, and solving the eom...

The anisotropic metric is

$$ds^{2} = \frac{L^{2}}{u^{2}} \Big[-\mathcal{F}(u)\mathcal{B}(u)dt^{2} + dx^{2} + dy^{2} + \mathcal{H}(u)dz^{2} + \frac{du^{2}}{\mathcal{F}(u)} \Big]$$
$$\chi(z) = az \quad \text{and} \quad \phi \equiv \phi(u)$$

[Mateos and Trancanelli]



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[Mateos and Trancanelli]

→ Regular on and outside the horizon

- → RG flow between AdS (UV) and Lifshitz type (IR)
- → The entropy density interpolates between

 $T \gg a$ $s \sim T^3$ and $T \ll a$ $s \sim a^{1/3}T^{8/3}$

 \longrightarrow There is an analytical expression for the near-boundary behavior of metric functions $\mathcal{O}(u^6)$

Preliminaries

→ The screening length L_s is define as the separation between a $q\bar{q}$ such that for $\ell < L_s$ ($\ell > L_s$) it is energetically favorable for the pair to be bound (unbound).

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- → We will determine L_s by comparing the action $S(\ell)$ of the $q\bar{q}$ pair to the action S_{unb} of the unbound system; i.e.

 $\Delta S(\ell) = S(\ell) - S_{\rm unb}$

(In the Euclidean version, this criterion corresponds to determining which configuration has the lowest free energy)

The screening length is the maximum value of ℓ for which ΔS is positive

1. Static case (to warm up)

Given the rotational symmetry in the xy-plane, the most general case is to consider the dipole in the xz-plane.



Choosing the static gauge $\tau = t$, $\sigma = u$, and the string embedding:

 $Z(u) = z(u)\cos\theta$ and $X(u) = x(u)\sin\theta$

1. Static case

The action for the U-shaped string takes the form

$$S = -\frac{L^2}{2\pi\alpha'} 2 \int dt \int_0^{u_{\text{max}}} du \frac{1}{u^2} \sqrt{\mathcal{B}(1 + \mathcal{F}\mathcal{H}\cos^2\theta z'^2 + \mathcal{F}\sin^2\theta x'^2)}$$

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Two conserved momenta \prod_z and \prod_x associated to translation invariance in the x, z direction. Then, the on-shell action can be written as

$$S = -\frac{L^2}{2\pi\alpha'} 2 \int dt \int_0^{u_{\max}} du \frac{1}{u^2} \frac{\mathcal{B}\sqrt{\mathcal{F}\mathcal{H}}}{\sqrt{\mathcal{F}\mathcal{B}\mathcal{H} - u^4(\Pi_z^2 + \mathcal{H}\Pi_x^2)}}$$

where the turning point u_{\max} is determined from the condition

$$x'(u_{\max}) = z'(u_{\max}) \to \infty$$

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which in terms of the momenta reads

$$\mathcal{FBH} - u^4 (\Pi_z^2 + \mathcal{H}\Pi_x^2)|_{u_{\max}} = 0 \quad \Rightarrow \quad u_{\max} \equiv u_{\max}(a, T, \Pi_i)$$

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From the boundary conditions we obtain the relation between the momenta \prod_z , \prod_x and the quark-antiquark separation ℓ

$$\frac{l}{2} = \int_0^{u_{\max}} du X' = \int_0^{u_{\max}} du Z'$$

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Finally, to determine L_s , we need to subtract from the U-shaped string action, that of the unbound pair (i.e. two straight strings)

$$S_{\rm unb} = -\frac{L^2}{2\pi\alpha'} 2 \int dt \int_0^{u_{\rm h}} du \frac{\sqrt{\mathcal{B}}}{u^2}$$

The UV divergences associated to integrating all the way to the boundary cancel out in the difference, and there are no IR divergences.

1. Static case

The isotropic result a=0 ($H
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 $L_s\simeq {0.24\over T}$ [Rey et al; Brandhuber et al] Or $L_s\simeq 0.24({\pi^2 N_c^2\over 2s})^{1/3}$ at constant entropy

density

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The anisotropic results:



2. Dipole in a plasma wind

We will first consider the ultra-relativistic limit. There are at least two important reasons for doing so:

It is relevant for the experiments.

→ It can be understood analytically. For the isotropic case:

 $L_s(T,v)\sim (1-v^2)^{1/4}$ [Liu et al.]

2. Dipole in a plasma wind

Our set up:



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Let us summarize the important steps:

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→ The position of the turning point is now $u_{\max} \equiv u_{\max}(a, T, \Pi_i, v)$ It is easy to check that for a fixed separation of the string endpoints,

 $\lim_{v \to 1} u_{\max} \to 0$

Then the dynamics of the string can be determined using the near boundary expansion of the metric.

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$$\mathcal{F}, \mathcal{B}, \mathcal{H} \sim 1 + W_i(a)u^2 + G_i(a,T)u^4 + \mathcal{O}(u^6)$$
 [Mateos et al.]
 T - independent

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$$\Delta S(l, v) \sim (1 - v^2)^{-1/2} \times (\text{finite integral}) \qquad \text{motion outside the transverse plane}$$

$$\mathcal{I}(a, \theta_v, \Pi_i, \mathcal{O}(u^6)) \implies T \text{ independent!}$$

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After some algebra:

 $\Delta S(l, v) \sim (1 - v^2)^{-1/2} \times (\text{finite integral})$ motion outside the transverse plane $\Delta S(l, v) \sim (1 - v^2)^{-1/4} \times (\text{finite integral})$ motion within the transverse plane

And finally, using the **boundary conditions**, we obtain how the screening length scales in the ultra-relativistic limit:

$$L_s \sim \begin{cases} (1-v^2)^{1/2} \times \mathcal{I}(a, \Pi_i, \mathcal{O}(u^6)) \text{ if } \theta_v \neq \pi/2 \\ (1-v^2)^{1/4} \times \mathcal{J}(a, T, \Pi_i, \mathcal{O}(u^6)) \text{ if } \theta_v = \pi/2 \end{cases}$$

2. Dipole in a plasma wind

A glimpse of the numerical results:

→ Wind along "z" and dipole along "x"



 $L_s/L_{
m iso}$ vanishes as $(1-v^2)^{1/4}$ in the limit v
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2. Dipole in a plasma wind

A glimpse of the numerical results:

→ Wind along "x" and dipole along "z"



 $L_s/L_{
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Two observations:

 \rightarrow The proper velocity along "z" of a point on the string at some u

$$v_{\text{proper}}(u) = v_z \sqrt{\frac{\mathcal{H}(u)}{\mathcal{F}(u)\mathcal{B}(u)}}$$

 $\mathcal{H}(u)$ increases from u = 0 to $u = u_h$, more steeply as a/T increases, $\mathcal{F}(u)\mathcal{B}(u)$ has the opposite behavior.

 \Rightarrow Maximum value of $u_{\rm max}$ beyond which $v_{\rm proper}$ becomes superluminal

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Maximum value of $u_{\rm max}$ beyond which $v_{\rm proper}$ becomes superluminal

→ We can show that for $v_z \neq 0$, u_{\max} decreases as a/T increases. More over,

$$\lim_{a/T \gg 1} u_{\max} \to 0 \quad \Rightarrow \quad \text{Use near boundary metric to} \\ \text{study } L_s$$

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For motion within the transverse plane ($v_z = 0$) $\Rightarrow L_s \sim f(a, T)$

No $a_{\rm diss}$ when $T \rightarrow 0$

→ So far we have studied $L_s(a, T, v)$, but clearly we could also think of $T_{\rm diss}(a, \ell, v)$ and $a_{\rm diss}(T, \ell, v)$

i.e. $T_{\text{diss}}(a, \ell, v)$ characterizes the dissociation of a qq-pair of fixed size ℓ in a plasma with a given degree of anisotropy a. Analogously for a_{diss} .

→ Using our results for the screening length, we can study the behavior of $T_{\rm diss}(a, \ell, v)$ and $a_{\rm diss}(T, \ell, v)$



→ As explained before, even at zero temperature a meson of size ℓ will dissociate if the anisotropy is increased above

$$a_{\rm diss}(T=0,\ell) \propto 1/\ell$$

and the proportionality constant is a decreasing function of the velocity

Numerical results for motion within the transverse plane:



The behavior is qualitatively analogous to that of the isotropic case.

$$T_{\rm diss}(v) \simeq T_{\rm diss}(0)(1-v^2)^{1/4}$$

[Liu et al.]

Numerical results for motion outside the transverse plane:



There is a limiting velocity $v_{\text{lim}} < 1$ even at zero temperature!

Limiting velocity for a fixed anisotropy and T = 0, meson oriented along the x-direction and moving along the z-direction



Limiting velocity for a fixed anisotropy and T = 0, meson oriented along the x-direction and moving along the z-direction



In the case of ultra-relativistic motion and $a/T \gg 1$:

$$a_{\rm diss} \sim \frac{1}{\ell} (1 - v_{\rm lim}^2)^{1/2} \text{ if } \theta_v \neq \pi/2$$
$$T_{\rm diss} \sim \frac{1}{\ell} (1 - v_{\rm lim}^2)^{1/4} \text{ if } \theta_v = \pi/2$$

Conclusions

• We have completely characterized the screening length for quarkonium mesons moving with arbitrary velocities and orientations.

• Mesons dissociate above certain critical value of the anisotropy, even at zero temperature.

• There is a limiting velocity for mesons moving through the plasma, even at zero temperature .

• The gravity calculation involves only the coupling of the string to the background metric, so any anisotropy that gives rise to a qualitatively similar metric will yield qualitatively similar results.

Back up slide

The near-boundary behavior of metric functions:

$$\mathcal{F} = 1 + \frac{11}{24}a^2u^2 + \left(\mathcal{F}_4 + \frac{7}{12}a^4\log u\right)u^4 + O(u^6),$$
$$\mathcal{B} = 1 - \frac{11}{24}a^2u^2 + \left(\mathcal{B}_4 - \frac{7}{12}a^4\log u\right)u^4 + O(u^6),$$
$$\mathcal{H} = 1 + \frac{1}{4}a^2u^2 - \left(\frac{2}{7}\mathcal{B}_4 - \frac{5}{4032}a^4 - \frac{1}{6}a^4\log u\right)u^4 + O(u^6)$$

with $\mathcal{F}_4(a,T)$ and $\mathcal{B}_4(a,T)$