CERN Summer lectures, August, 2007

POSSIBLE PHYSICS BEYOND THE STANDARD MODEL

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"Understanding nature is one of the noblest endeavors the human race

has ever undertaken"

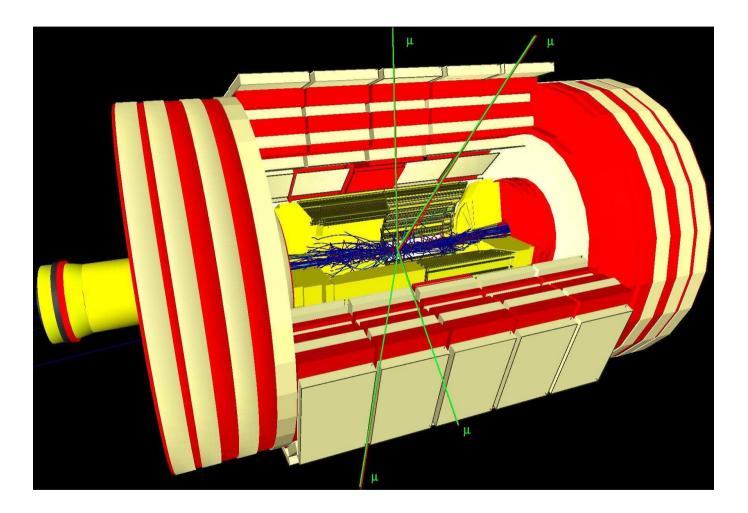
Steven Weinberg



• What do we expect to see at LHC?

Preview: Higgs

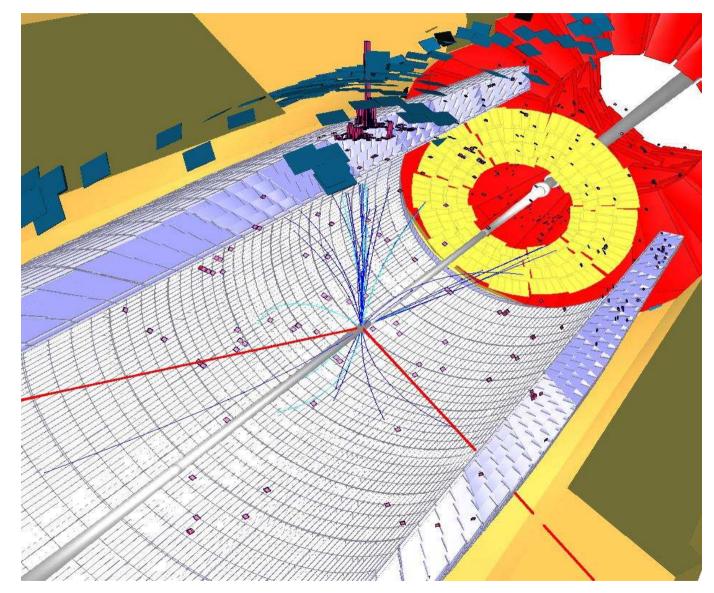
Possible exciting physics we are preparing to search for: Higgs particle



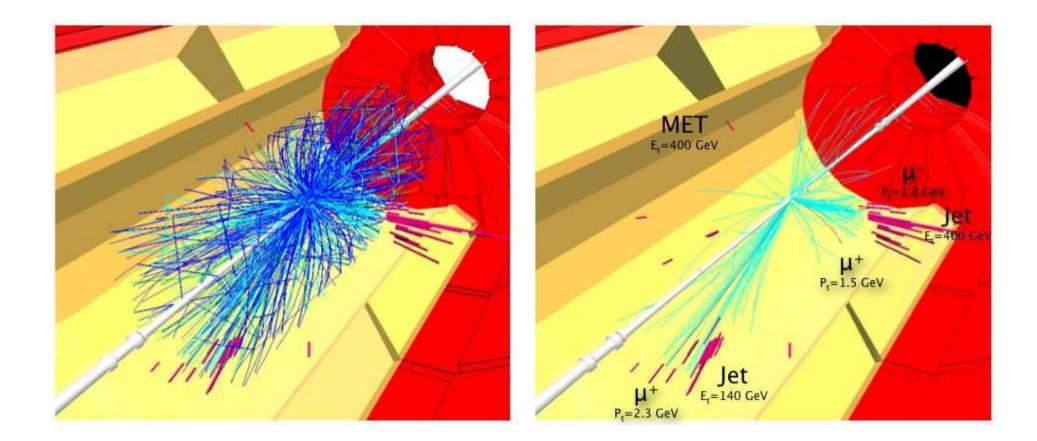
Requested by the SM, might tell us a lot about the hierarchy puzzle.

Beyond the Standard Model,

Preview: Supersymmetry



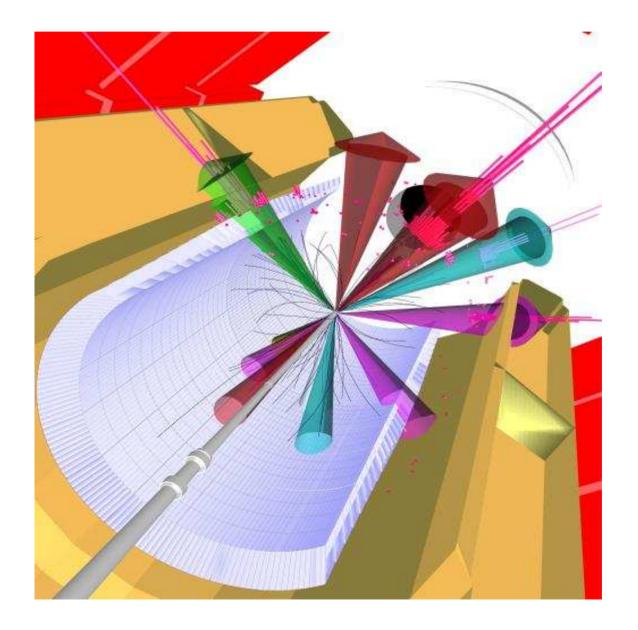
SUSY event: A decay of a neutralino into Z + LSP, the Z decays into two muons.

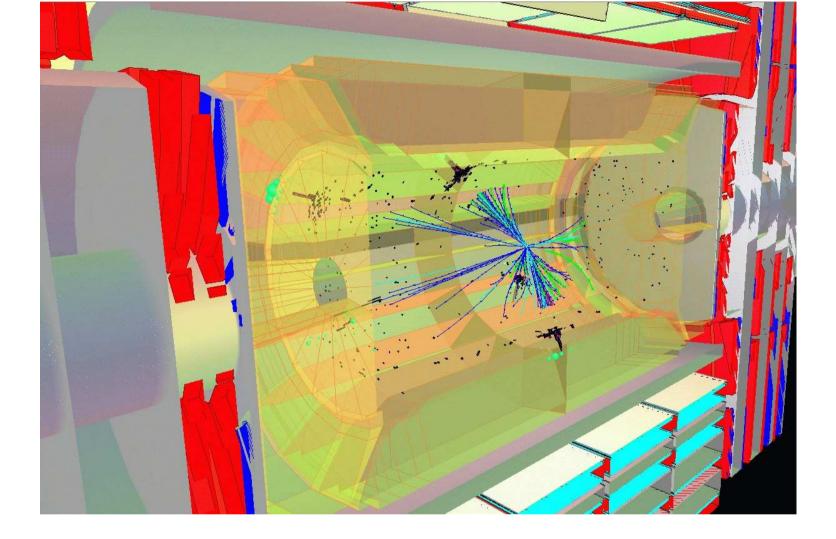


Missing transverse energy susy event at high luminosity

Preview: Small black-Hole production

Small black-hole may be produced and decay via Hawking radiation at LHC, if the scale of (quantum) gravity is low.





Event of BH production with $M_P = 1$ TeV and two extra dimensions.

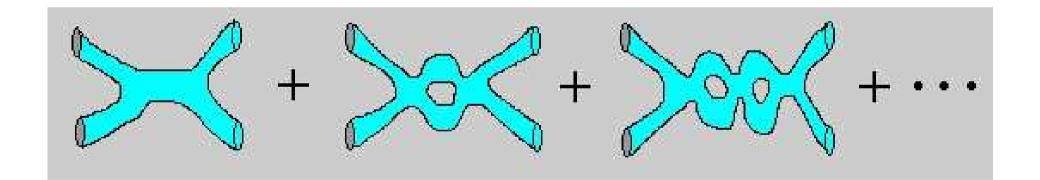
See the Charybdis site

http://www.ippp.dur.ac.uk/montecarlo/leshouches/generators/charybdis/manual.html

Beyond the Standard Model,

Preview: Strings?

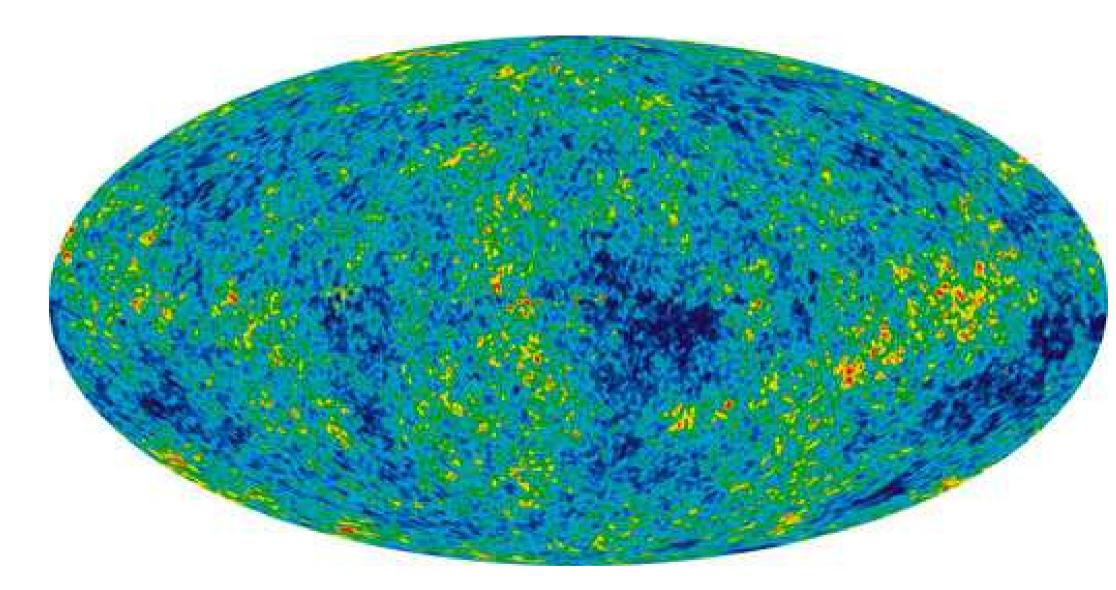
String excited modes can also be produced if the string scale is sufficiently low.



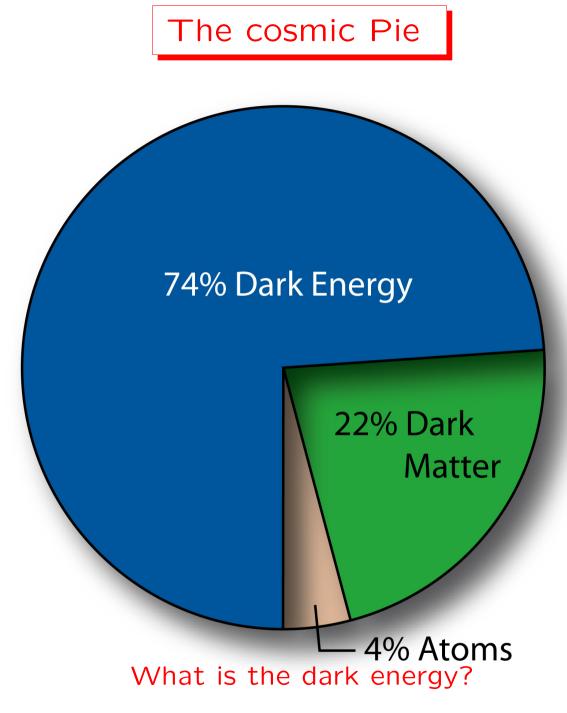
Preview: Dark Matter+Dark Energy



Can particle physics provide a candidate for the dark matter of the universe?



Can particle physics provide explanations for the primordial spectrum of cosmological fluctuations?



The purpose of these lectures

• Why we believe the Standard Model is not the final (fundamental) theory of the world?

• Why do we believe that there is new physics around the TeV range?

• What types of new physics at shorter distances theorists have guessed during the past twenty years and why?

♡ This is an exciting period because it is some of this new physics that we are going to test at LHC

♠ We are also living in an era where similar, revolutionary data are coming from cosmology and they also probe the nature of the fundamental theory

A Most probably it will be some of you that will solve the puzzles and nail down the fundamental theory that extends and completes the SM!

Suggested reading

- "Beyond the Standard Model" by Fabio Zwirner, http://doc.cern.ch/cernrep/1998/98-03/98-03.html
- "Supersymmetry Phenomenology" by Hitoshi Murayama [arXiv:hep-ph/0002232]
- "Physics beyond the Standard Model" by Gian Giudice, Lect. Notes Phys. **591**:294-327,2002
- "Beyond the Standard Model" by John Iliopoulos http://preprints.cern.ch/cernrep/2004/2004-001/2004-001.html
- "Phenomenological guide to physics beyond the standard model", by Stefan Pokorski, [arXiv:hep-ph/0502132]
- "Phenomenology beyond the Standard Model" by Joe Lykken, [arXiv:hep-ph/0503148]

Most obtainable from the archive http://xxx.arxiv.cornell.edu/

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Beyond the Standard Model,
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A tentative plan

- The Standard Model and its problems: Why do we expect new physics?
- Supersymmetry
- Grand Unification
- Gravity and String Theory
- The physics of extra dimensions.

Beyond the Standard Model,

High Energy Units

We use

h=1 , c=1

$[Energy] \sim [Mass] \sim \frac{1}{[Length]} \sim \frac{1}{[Time]}$

Beyond the Standard Model,

The Standard Model: principles

- The Standard Model of the Electroweak and Strong interactions has been a very successful theory.
- Effort started at the beginning of the twentieth century. Consolidated by the establishment of Quantum Field Theory.

QFT=Special Relativity+ Quantum Mechanics

- All interactions are based on the "gauge principle" (including gravity) \Rightarrow invariance under local (independent) symmetry transformations. (the first model for this was electromagnetism)
- Renormalizability was another principle at the time the SM was formulated. We understand today that it is not a necessity: Any extension of a fundamental theory (not including gravity) is necessarily renormalizable to begin with.
- Other important principles are: Locality, Unitarity.

Standard Model: Open problems

The standard model was constructed as a renormalizable theory \rightarrow as such it can be extended in principle to very high energies.

Why do we believe that there is more to know beyond the Standard Model?

Three sets of experimental data that are not accounted for by the SM:

Neutrinos have (VERY small) masses and they mix.

♠ There is a lot (22%) of dark (non-SM) matter in the universe. Neutrinos are part of it but cannot account for most of it.

♠ There is another source of energy in the universe (74%), known as "dark energy" (vacuum energy?) This translates to $|V_{vac}| \sim 10^{-12}$ eV⁴.



Off by 56 orders of magnitude

Standard Model: Open problems II

• (Quantum) Gravity is not part of the Standard Model. One of the deepest questions of modern theoretical physics is: why the characteristic scale of gravity

$$M_{\mathsf{Planck}} = \frac{1}{\sqrt{G_N}} \simeq 10^{19} \quad \mathrm{GeV}$$

is so much higher than the other scales of particle physics?

- The Standard model alone contains IR-free couplings \Rightarrow strongly-coupled UV physics.
- The SM has many unexplained parameters and patterns.

THEREFORE: SM is an Effective Field Theory (EFT) valid below 100 GeV. Must be replaced by a more fundamental theory at a higher scale Λ . How big is Λ ?

• Λ must be small: $\Lambda \sim$ a few TeV. Otherwise we suffer from a technical (fine-tuning) problem also known as the hierarchy problem (more later).

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Beyond the Standard Model,
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SM patterns and parameters

• The standard model group $SU(3) \times SU(2) \times U(1)$ is not "unified", the coupling constants

$$g_3^2 \simeq 1.5, \; g_2^2 \simeq 0.42, \; g_Y^2 \simeq 0.13$$

are independent parameters. This can be improved if the fundamental theory has a simple gauge group, like SU(5) that contains the SM gauge group.

- The matter content and representations seems not very "regular". Why not higher representations? Hypercharges seem also bizarre. (but up to normalizations they are determined by the absence of gauge anomalies (BIM)
- Why three families? ("Who ordered that?")
- What decides the scale of Electroweak symmetry breaking

 $v_F \simeq 174$ GeV ?

What decides the mass of the Higgs?

Beyond the Standard Model,

The pattern of masses

• The pattern of SM masses is mysterious at least:

family type	ups	downs	leptons
3rd	$m_t = 175$	$m_b = 4.2$	$m_{\tau} = 1.7$
2nd	$m_{c} = 1.2$	$m_{s} = 0.1$	$m_{\mu} = 0.1$
lst	$m_u = 3 \times 10^{-3}$	$m_d = 5 \times 10^{-3}$	$m_e = 5 \times 10^{-4}$

• Neutrino masses seem to be in the $10^{-12} - 10^{-14}$ GeV range. SM masses span 16 orders of magnitude.

This is a question for the Yukawa couplings λ_i : $m_i = \lambda_i v_F$. We want to explain their ratios and the absolute normalization, (as we can do it for the spectral lines of atoms.)

• There are other parameters of the Standard Model that we would like to understand.

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How parameters affect us?

How academic is the issue of such parameters?

Most of them are crucial to the existence of our universe as we know it, and the existence of humans as we know them.

• $v_F \rightarrow 0$ then p is unstable to decay to neutrons \rightarrow no Hydrogen.

• $v_F >> 170 GeV$ n-p mass difference is very large and the nuclear force becomes of shorter range \rightarrow nuclei cannot be bound \rightarrow nothing but hydrogen in the universe.

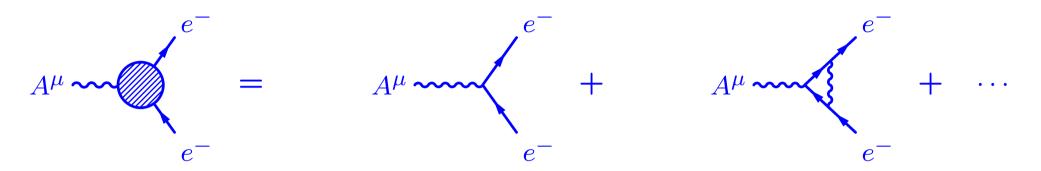
• changing the $\alpha_{em} \rightarrow \text{no } C^{12}$ resonance \rightarrow no carbon in our universe.

Exercise : Justify by simple reasoning the first two statements. If unable look here.

Beyond the Standard Model,

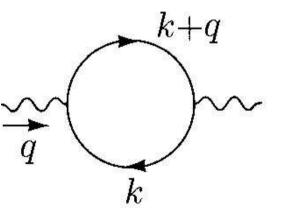
Renormalization: "Integrating out" high-energy d.o.f

• In QFT physical processes have quantum corrections



- They involve "virtual" particles that do not satisfy the mass-shell condition $E^2 = \vec{p}^2 + m^2$. This is allowed because of the uncertainty principle.
- Therefore the energies of "virtual" particles are not constrained and can be arbitrarily high.

$$I_{vp} \sim \int_{-\infty}^{\infty} \frac{d^4 k}{(2\pi)^4} \frac{1}{k^2 + m_e^2} \frac{1}{(k+q)^2 + m_e^2}$$



Beyond the Standard Model,

• High energy degrees of freedom, unobservable directly in low energy experiments, make (indirect) quantum contributions to low-energy observables.

• We can therefore "integrate out" such degrees of freedom, and substitute their effects directly in the action of the low energy degrees of freedom (d.o.f).=Low Energy Effective Action

• This notion is more transparent in the path-integral formulation of Quantum Mechanics and QFT:

$$\begin{split} Z &\equiv \int \mathcal{D}L \ \mathcal{D}H \ e^{iS(L,H)} \quad , \quad H \to \text{heavy d.o.f} \quad , \quad L \to \text{light d.o.f} \\ Z &= \int \mathcal{D}L \ e^{iS_{\text{eff}}(L)} \quad , \quad e^{iS_{\text{eff}}(L)} \equiv \int \mathcal{D}H \ e^{iS(L,H)} \end{split}$$

• It is also similar to what we do with the probabilities of unobservable events: P(x,y), with y unobservable gives a probability for x:

$$P_{eff}(x) = \int dy \ P(x,y)$$

Beyond the Standard Model,

Effective field theory

• Therefore, if we are interested in the low energy dynamics we can integrate-out the high energy d.o.f, and incorporate their effects in the action for the light particles. This we call the (low-energy) effective action.

• The heavy particles are unobservable from the low-energy point of view (cannot be produced) but they have "virtual" effects that affect the low energy dynamics.

- The effects of the high-energy d.o.f are summarized in the EFT by a **few local interactions** to a good degree of accuracy.
- Effective interactions with dimension Δ have coefficients (dimensional analysis)

$$C_{\Delta} \sim \frac{1}{\Lambda^{\Delta-4}}$$
 , $C_{\Delta=4} \sim \log \Lambda$

where Λ is the (large) scale of the high energy d.o.f.

- Corrections to interactions with $\Delta \leq 4$ are large. This is what we call the **renormalizable interactions**. All the interactions of the Standard model are such interactions.
- Corrections to non-renormalizable interactions $\Delta > 4$ are small. This is where the new information of the high-energy theory is hiding (most of the time)

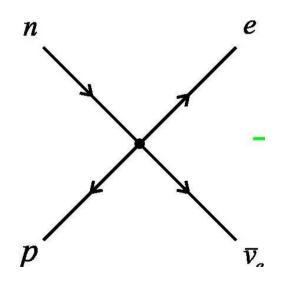
Beyond the Standard Model,

Effective couplings: the Fermi theory paradigm

The Fermi theory described the decay of neutrons:

 $n \to p + e + \bar{\nu}_e$

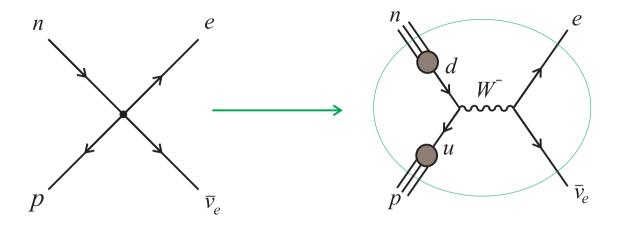
via a four-fermion (dimension-6=non-renormalizable interaction)



 $L_{\text{interaction}} = G_F \ (\bar{p} \ \gamma^{\mu} \ n) (\bar{\nu}_e \ \gamma_{\mu} \ e)$ with $G_F \simeq \frac{1}{(300 \ GeV)^2}$

This descriptions is very accurate for energies E << 100 GeV .

However, with a better magnifying glass the four-fermi interaction originates from the Standard Model electroweak gauge interactions



Effective interaction :

p = (uud) , n = (udd) , $d \rightarrow W^- + u \rightarrow (e^- + \overline{\nu}_e) + u$

$$\frac{g_W^2}{p^2 + M_W^2} \simeq \frac{g_W^2}{M_W^2} - \frac{g_W^2}{M_W^2} \frac{p^2}{M_W^2} + \dots = G_F + \dots , \quad p^2 \ll M_W^2$$

The effective interaction is dimension 6. It is the result of interactions with dimension 4 (renormalizable) interactions at higher energy.

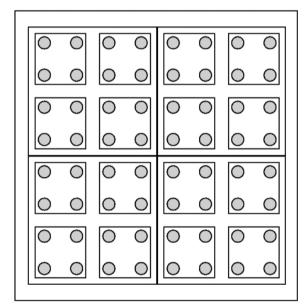
• We can improve by including the next term:

$${G_F\over M_W^2}(ar p \ \gamma^\mu\partial_\mu \ n)(ar
u_e \ \gamma^
u\partial_
u \ e)$$

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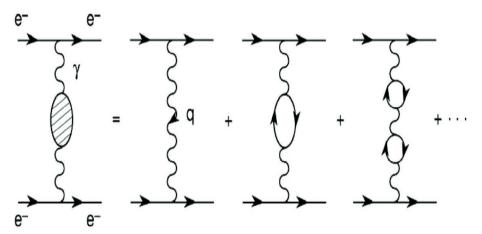


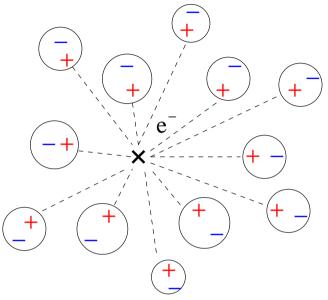
- Integrating out high-energy d.o.f is an "irreversible" process.
- From a high energy theory, we calculate the low energy interactions. From a finite number of low-energy interactions we cannot reconstruct the high-energy theory.
- A simple example of integrating out: "renormalization": the block spin transformation.
- An everyday analog: converting from RAW to jpeg format.



Effective interactions: Running Couplings

You have learned that coupling constants "run" with energy. The reason is : quantum effects of high-energy d.o.f

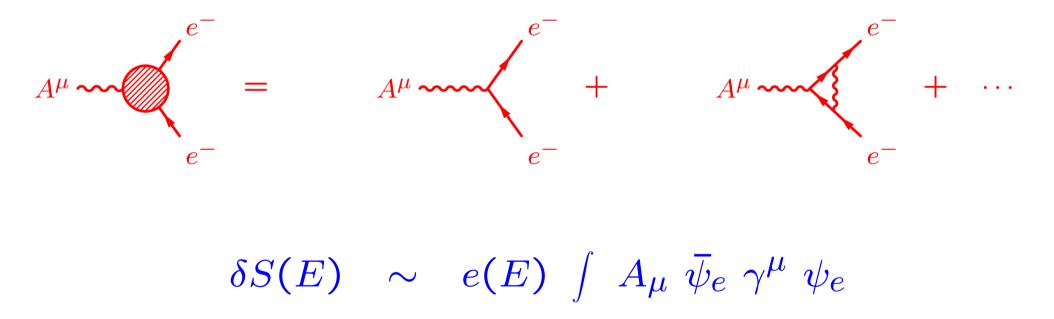




- In electromagnetism we have "screening":
- $e^+ e^-$ pairs have the tendency to screen lone charges.
- The larger the distance = more $e^+ e^-$ pairs in-between = more charge screening.
- Result: charge is a function of the energy $= \frac{1}{\text{distance}}$: Beyond the Standard Model,

$$\alpha_{\rm em}(E) \simeq \frac{\alpha_{\rm em}(m_{\rm e})}{1 - \frac{\alpha_{\rm em}(m_{\rm e})}{3\pi} \log \frac{E^2}{m_{\rm e}^2}} \quad , \qquad \alpha_{\rm em} \equiv \frac{e^2}{2(\hbar c)}$$

- The charge becomes larger as we approach the electron closer.
- After taking into account these quantum effects on the coupling, we may replace the EM interaction by its corrected value:



• This is the effective interaction valid at energy E.

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Renormalization Summary

- The fundamental theory is defined at a high-energy scale $\Lambda \to \infty$.
- What we measure are effective interactions at low(er) energy (larger distance)
- Knowledge of the high-energy (short-distance) theory defines completely the low energy theory. It does not work the other way around! (Universal-ity!)
- At low energy , interactions of all possible dimensions (allowed by symmetries) are generated. Their effective couplings scale generically as

$$\lambda_{\Delta} \simeq \Lambda^{4-\Delta} \left[1 + \mathcal{O} \left(\frac{E}{\Lambda} \right) \right] \quad , \quad \lambda_{\Delta=4} \sim \log \Lambda$$

 Λ = the characteristic high energy scale, Δ = the (mass) dimension of the interaction.

- The (old) wisdom: a quantum theory must be renormalizable ⇒
 Only renormalizable theories can be extended to high energy without modification (They depend on a finite number of fundamental parameters)
- Suggestions or further reading are here

The hierarchy problem:introduction

- According to our previous discussion:
- Couplings of operators with $\Delta = 4$ depend logarithmically on the high energy scale Λ

♠ Operators of dimension two and three (mass terms for bosons and fermions) should have at low energy their coefficients scale as

$$m_i^2 \sim \Lambda^2 \quad \Leftrightarrow \quad m_i \sim \Lambda$$

If we want the SM to make sense up to $\Lambda \simeq 10^{18}$ GeV, then either:

- All masses are generically enormous (excluded from experiment)
- If there are light particles there are two possibilities:
- ♠ The masses are light due to a symmetry.
- The masses are accidentally light (fine-tuning).

 \blacklozenge "No free lunch": we must have new physics at $\Lambda \sim 1-10$ TeV to avoid fine-tuning.

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Beyond the Standard Model,
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Fermion masses

Consider the electron Lagrangian written in terms of the left- and righthanded components of the electron,

$$e_{L,R} = \frac{1 \pm \gamma^5}{2} \ e$$

 $S = i \left[\bar{e}_R (\partial + A) e_R + \bar{e}_L (\partial + A) e_L \right] + m_e \left(\bar{e}_L e_R + \bar{e}_R e_L \right)$

The theory has the usual vector U(1) symmetry (conservation of electric charge):

$$e_{L,R} \to e^{i\epsilon} e_{L,R} \quad , \quad \overline{e}_{L,R} \to e^{-i\epsilon} \overline{e}_{L,R}$$

When $m_e = 0$ there is more symmetry: chiral symmetry,

$$e_L \to e^{i\epsilon} e_L \quad , \quad e_L \to e^{-i\epsilon} e_L$$

Inversely: chiral symmetry forbids a mass.

Beyond the Standard Model,

The quantum corrections to the fermion mass coming from the diagrams



- We would expect that $\delta m \sim \Lambda \left[c_1 + c_2 \frac{m_e}{\Lambda} \log \frac{E}{\Lambda} + \mathcal{O}(\Lambda^{-2}) \right]$.
- The result of the calculation gives though (to leading order in α_{em})

$$m_{eff}(E) = m_e + \frac{3\alpha_{em}}{4\pi} m_e \log \frac{E}{\Lambda} = m_e \left[1 + \frac{3\alpha_{em}}{4\pi} \log \frac{E}{\Lambda}\right]$$

- There is no linear dependence on Λ !
- Therefore, it is very insensitive to the high-energy scale Λ . (~ 4% for E = 1 GeV and $\Lambda = 10^{19}$ GeV).

Gauge boson masses

Unbroken gauge symmetry forbids gauge bosons to have a mass. Upon spontaneous breaking of the gauge symmetry gauge bosons acquire masses.

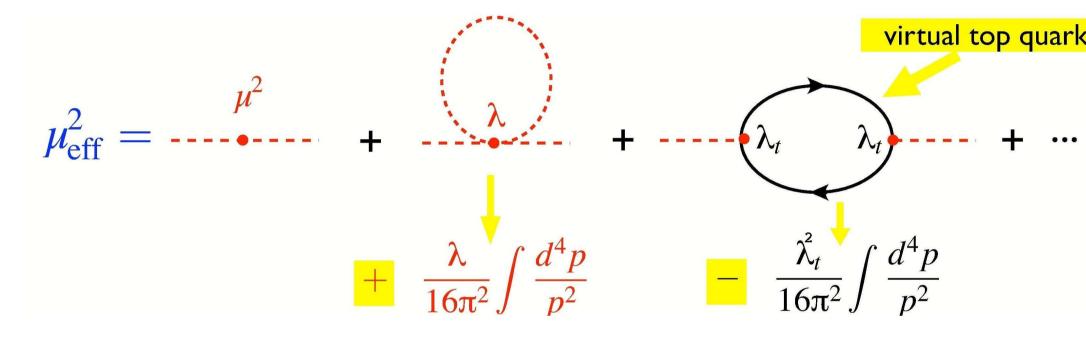
$$M_{Z,W^{\pm}} \sim g v_F \quad v_F \sim \frac{\mu}{\sqrt{\lambda}} \quad , \quad V = -\frac{\mu^2}{2}H^2 + \lambda H^4$$

Dimensionless couplings run logarithmically $\sim \log \frac{E}{\Lambda}$ and therefore are not very sensitive to Λ .

- The important sensitivity comes from the renormalization of the mass-term of the Higgs, μ .
- In the SM this is also the case for the fermions as $m_f \sim \lambda$ Yukawa v_F Beyond the Standard Model,

The Higgs mass term

We have seen that the sensitivity of SM masses depends on the behavior of a single parameter: the mass term μ of the Higgs scalar.



$$\mu_{eff}^2(E) = \mu^2 + \frac{\lambda - \lambda_t^2}{4\pi^2} (\Lambda^2 - E^2)$$

The Higgs mass, and therefore many other SM masses depend quadratically on the UV scale Λ .

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Beyond the Standard Model,
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The hierarchy problem

We found that:

• All dimensionless couplings of the SM run logarithmically and are therefore not very sensitive to the UV scale of the theory.

- The Higgs quadratic term $\mu \Rightarrow$ the Higgs expectation value $v_F \Rightarrow$ Fermion and gauge-boson masses is linearly sensitive to Λ .
- The SM physics at high energy is therefore technically hard to calculate as fine-tuning is required.

This is the hierarchy problem: It is very difficult in a theory where parameters run polynomially with the cutoff Λ to extend it to hierarchically higher energies.

End of first act

Evading the hierarchy problem

Very **SPECIAL** theories may avoid the hierarchy problem.

• "Technicolor"

• "Supersymmetry"

• Large dimensions

• Pseudo-Goldstone particles (aka Little Higgs) See [arXiv:hep-ph/0512128] and [arXiv:hep-ph/0502182]

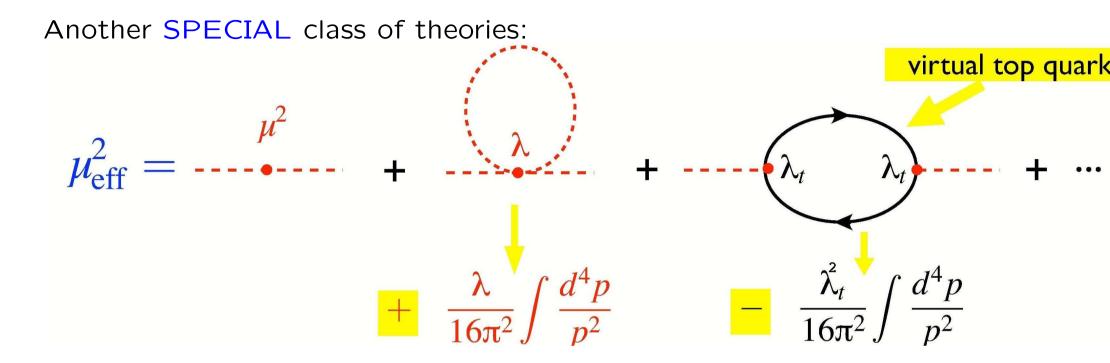
Technicolor

- The idea, known under the name of "technicolor", is to assume that all particles in the fundamental theory except the gauge bosons are fermions.
- And the Higgs? It could be a bound state of two fermions (like meson scalars are bound states of quarks and anti-quarks, or the Cooper pair in superconductors).
- This needs a new gauge interaction (technicolor) that becomes strong at an energy $\Lambda_T > v_F$.
- For $\infty >> E >> \Lambda_T$ the theory is a theory of fermions and all masses run logarithmically.
- For $E << \Lambda_T$ the theory looks like the SM.
- Therefore $\Lambda_T \sim 1 T e V$.

Unfortunately detailed models that satisfy known experimental constraints are very difficult to construct. (See hep-ph/0007304 for a review.)

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Beyond the Standard Model,
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If $\lambda = \lambda_t^2$ then the quadratic divergence will cancel. Fermion and boson loops cancel each other.

The symmetry that imposes such relations is known as supersymmetry (SUSY)

Supersymmetry, Vol II

 $\delta_{\text{SUSY}}(\text{Boson}) = \epsilon \cdot (\text{Fermion})$

 δ_{SUSY} (Fermion) = $\epsilon \cdot \partial$ (Boson)

Therefore

$$\delta_{SUSY} \cdot \delta_{SUSY} \sim \partial$$

and in this sense SUSY is a "square root" of a translation.

Supersymmetry pairs a particle with spin j will another with spin $j \pm \frac{1}{2}$

Then the Higgs will have a fermionic partner (the Higgsino) whose effect will be to cancel the quadratic terms in the running of the mass.

The Supersymmetric Multiplets (representations)

- In the SSM we have vector multiplets containing a vector (gauge boson) and a Majorana fermion (gaugino) in the adjoint of the gauge group $\rightarrow (A^a_\mu, \lambda^a)$.
- We also have chiral multiplets containing a complex scalar and a Weyl fermion, in some appropriate representation of the gauge group $\Phi_i \equiv (\phi^i, \psi^i)$.
- ♠ In the SSM we have such multiplets for each quark and lepton as well as two conjugate multiplets H_1^{-1} , H_2^{+1} for the Higgs.
- This is to avoid $U(1)_Y$ anomalies and give masses to both up and down quarks (see later).

The Supersymmetric Standard Model				
particles Sparticles				
quarks $\begin{pmatrix} u_L \\ d_L \end{pmatrix}$ u_R d_R	squarks $\begin{pmatrix} ilde{u}_L \\ ilde{d}_L \end{pmatrix}$ $ ilde{u}_R$ $ ilde{d}_R$			
$\begin{array}{c} leptons \\ v_L \end{array} \qquad e_R \end{array}$	sleptons $\begin{pmatrix} ilde{e}_L \\ ilde{ u}_L \end{pmatrix}$ $ ilde{e}_R$			
Higgs H_1 (hypercharge = -1)doublets H_2 (hypercharge = +1)	$\begin{array}{l} \textbf{Higgsinos} & \tilde{H}_1 \\ \tilde{H}_2 \end{array}$			
W^+, H^+	charginos χ_1^+, χ_2^+ neutralinos χ_a^0 $(a = 1, 2, 3, 4)$			
Z, γ, H_i^0 $(i = 1, 2, 3)$	neutralinos χ_a^0 $(a=1,2,3,4)$			
g	gluino <i>§</i>			
Exercise : Show that no particle of the SM can be a susy partner: a full doubling of the spectrum is necessary.				

Beyond the Standard Model,

The quantum numbers

chiral	SU(3)	SU(2)	$U(1)_Y$
supermultiplet			
Q	3	2	$\frac{1}{6}$
UC	3	1	$-\frac{2}{3}$
D ^c	3	1	$\frac{1}{3}$
L	1	2	$-\frac{1}{2}$
E ^c	1	1	1
H ₁	1	2	$-\frac{1}{2}$
H ₂	1	2	$\frac{1}{2}$

Note that L and H_1 are indistinguishable in terms of gauge quantum numbers.

• The renormalizable interactions of a gauge theory are encoded in gauge couplings, Yukawa couplings and the potential for the scalars.

• In a supersymmetric renormalizable theory, the interactions are encoded into the gauge couplings and the super-potential W.

• W is a gauge-invariant function of the scalar fields, (but not of their complex conjugates). A renormalizable W is at most cubic.

• The kinetic terms of the fields and their couplings to the gauge bosons are standard and determined by the representations/charges and the gauge couplings.

• The Yukawa couplings are as follows:

$$L_{\text{Yukawa}} = [i\sqrt{2} \ g \ \bar{\psi}_i \ \lambda^a (T^a \phi)^i + h.c.] - \frac{1}{2} \left[\frac{\partial^2 W}{\partial \phi^i \partial \phi^j} \ \bar{\psi}^i \psi^j + h.c. \right]$$

• Finally there is the scalar potential

$$V = \sum_{i} F_i^* F_i + \frac{g^2}{2} \sum_{a} D^a D^a \ge 0$$

$$F_i = \frac{\partial W}{\partial \phi^i}$$
, $D^a = \phi_i^* (T^a)^i{}_j \phi^j$

 $\sim - - -$

Beyond the Standard Model,

• The most general cubic, gauge invariant and holomorphic superpotential:

$$\begin{split} W &= \zeta^U \; Q U^c H_2 + \zeta^D \; Q D^c H_1 + \zeta^E \; L E^c H_1 + \mu H_1 H_2 + \\ &+ \lambda Q D^c L + \lambda' L L E^c + \mu' L H_2 + \lambda'' U^c D^c D^c \\ \\ \hline \text{Exercise} \quad \text{Show this!} \end{split}$$

• μ' has one family index $(\zeta^U, \zeta^D, \zeta^E)$ have two such indices and $(\lambda, \lambda', \lambda'')$ have three.

• The last four terms violate baryon and lepton number.

 $\lambda, \lambda', \mu' \neq 0 \quad \rightarrow \quad \Delta B = 0, |\Delta L| = 1 \quad , \quad \lambda'' \neq 0 \quad \rightarrow \quad \Delta B = 1, |\Delta L| = 0$

A symmetry (R-parity) must be imposed to forbid them. Exercise Why such offending terms are absent in the SM?

Beyond the Standard Model,



To avoid problems with fast proton decay and lepton number violation: assume the existence of an extra Z_2 symmetry

 $R - parity = (-1)^{2S+3B+L} = (-1)^{number of Sparticles}$

• Sparticles can only be produced or annihilated in pairs (harder to produce).

• The lightest Sparticle (LSP) is absolutely stable.

• It is almost always a neutralino \rightarrow it has only weak interactions \rightarrow it is not directly visible in experiments \rightarrow missing energy.

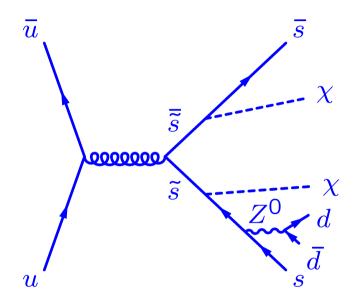
This is a characteristic SUSY signal at LHC.

• When supersymmetry breaks, R-parity must remain intact!

Exercise Why we do not set the coefficients of the offending (baryon+lepton violating) terms to zero in the superpotential?



This is an example of a possible event that can be seen at LHC:

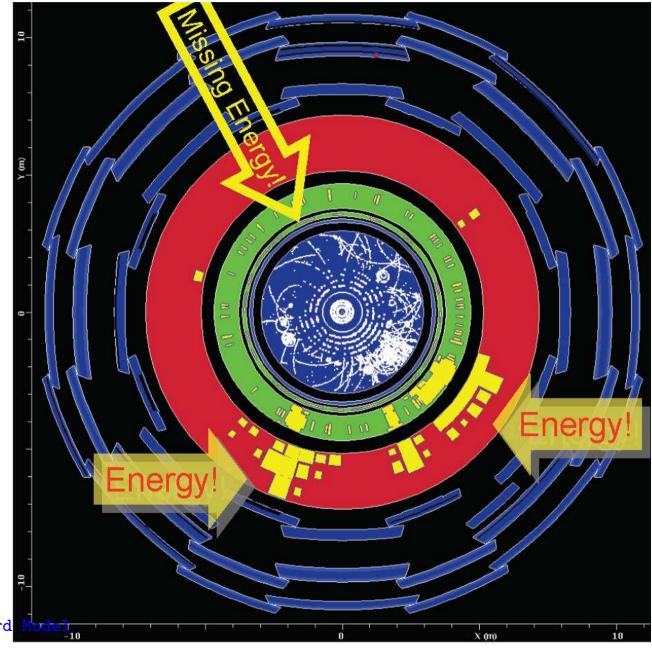


where:

$$\tilde{q} = squark$$

$$\chi = LSP$$

Missing Energy (Atlas simulation)



Beyond the Standard Model

A link to the dark matter of the Universe

- The universe contains an important fraction (22%) of non-relativistic, non-SM matter. This is known as Dark Matter.
- Its presence is crucial for structure formation in the universe.
- It is mostly composed of Weakly Interacting (very) Massive Particles: WIMPS.
- The supersymmetric LSP, is an excellent candidate for forming the dark matter of our universe.

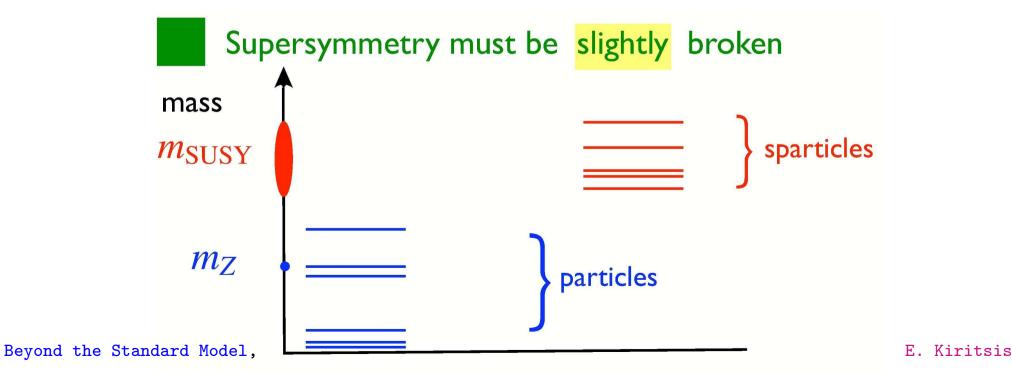
Supersymmetry breaking

So far we have neglected the fact that exact supersymmetry forces the

superpartners to have the same mass as the SM particles, e.g.

$$m_e = m_{\tilde{e}}$$
 , etc.

It is unavoidable to conclude that:



Supersymmetry breaking, II

We must ensure that SUSY breaking does not destroy the good properties of SUSY:

• Like gauge symmetry breaking, supersymmetry breaking must be spontaneous (soft). Then the Higgs mass runs logarithmically like that of the fermions!

• M_{SUSY} must not be very far from v_F . It should be 1 - 10 TeV.

If $M_{SUSY} >> v_F$ the hierarchy problem resurfaces.

- Therefore, naturalness tells us that the superpartners must be in the TeV range.
- If this idea is correct, most probably the superpartners will be found at LHC.

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Beyond the Standard Model,
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The soft supersymmetry breaking terms

We can parameterize all possible extra terms that can appear because of supersymmetry breaking ($\Delta < 4$) These are scalar masses, gaugino masses, and cubic scalar interactions proportional to the ones present in the superpotential (soft breaking terms):

$$L_{\text{soft}} = \sum_{i} \tilde{m}_{i}^{2} |\phi_{i}|^{2} + \frac{1}{2} \sum_{A} M_{A} \bar{\lambda}^{A} \lambda^{A} +$$

 $+ \left(\zeta^U A^U \ \tilde{q} \tilde{u}^c h_2 + \zeta^D A^D \ \tilde{q} \tilde{d}^c h_1 + \zeta^E A^E \ \tilde{\lambda} \tilde{e}^c h_1 + m_3^2 \ h_1 h_2 + h.c. \right)$

where $\tilde{q}, \tilde{u}^c, \tilde{d}^c$ are the respective squarks and $h_{1,2}$ the two Higgs doublets.

This gives rise to the Minimal Supersymmetric Standard Model (MSSM).

- Since A^i are matrices in flavor space, we have a large number of parameters. For generic values of such parameters there are phenomenological problems (like flavor changing neutral currents).
- There are several simple choices of soft parameters that are motivated by (i) simplicity (ii) some concrete Susy-breaking mechanism.

The tree-level MSSM potential that involves the Higgses* is:

$$V = m_1^2 |h_1|^2 + m_2^2 |h_2|^2 + m_3^2 (h_1 h_2 + h.c.) + \frac{g_2^2}{8} \left(h_2^{\dagger} \vec{\sigma} h_2 + h_1^{\dagger} \vec{\sigma} h_1 \right)^2 + \frac{g_Y^2}{8} \left(|h_2|^2 - |h_1|^2 \right)^2$$
$$m_1^2 = \mu^2 + \tilde{m}_{h_1}^2 \quad , \quad m_2^2 = \mu^2 + \tilde{m}_{h_2}^2$$

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*There is also the potential for squarks and sleptons

Without any extra input, there are no UV constraints on the MSSM parameters. Simple ansatz (compatible with data so far, and can arise from supergravity/string theory). Imposed at some UV scale Λ :

Gaugino masses and soft scalar masses are universal

$$M_3 = M_2 = M_Y \equiv m_{1/2}$$

$$ilde{m}_Q= ilde{m}_{U^c}= ilde{m}_{D^c}= ilde{m}_L= ilde{m}_{E^c}= ilde{m}_{H_1}= ilde{m}_{H_2}\equiv m_0$$

So are the soft scalar couplings

$$A^U = A^D = A^E \equiv A_0$$

If we now include the μ -term coefficient, μ and the soft breaking term m_3 we end up with 5 extra parameters on top of the SM ones:

$$\mu$$
 , $m_{1/2}$, m_0 , A_0 , m_3

• After minimization of the Higgs potential with $\langle H_1 \rangle = \begin{pmatrix} v_1 \\ 0 \end{pmatrix}$, $\langle H_2 \rangle = \begin{pmatrix} 0 \\ v_2 \end{pmatrix}$ we can trade μ and m_3 with sign(μ) and tan $\beta \equiv \frac{v_1}{v_2}$.

$$\mathsf{sign}(\mu)$$
 , $m_{1/2}$, m_0 , A_0 , $aneta$

This is known as the mSUGRA parametrization of the MSSM.

• The parameters, $m_{1/2}, m_0, A_0$, must be evolved to low energy using the RGE equations and eventually compared to data. tan β is already a low energy parameter.

You are now guided to this page where a simple example is analyzed in order to illustrate the derivation of the softly broken supersymmetric action

Beyond the Standard Model,

Spontaneous supersymmetry breaking

Spontaneous supersymmetry breaking is an important problem. There are many different classes of models.

• Global supersymmetry breaks spontaneously, when $\langle V \rangle > 0$. Since $V \sim |F_i|^2 + |D^a|^2$, this implies that if some $\langle F_i \rangle$ or $\langle D^a \rangle$ are non-zero susy is broken.

• Like standard global symmetries, there is a massless fermion, the Goldstino, $\tilde{G} = \langle F_i \rangle \psi^i + \langle D_a \rangle \lambda^a$, associated with spontaneous global supersymmetry breaking.

• Supersymmetry can be promoted into a local symmetry. The appropriate theory then contains also gravity and is known as supergravity.

• In particular, the "gauge-field" associated to local supersymmetry is a spin-3/2 fermion known as the gravitino. It is the supersymmetric partner of the graviton. Like the graviton it is massless when supersymmetry is unbroken.

• When supersymmetry breaks spontaneously, the gravitino acquires a nonzero mass $m_{3/2}$. It becomes massive by combining with the Goldstino field. This is the super-Higgs mechanism.

• The supersymmetry breaking scale Λ_S is related to the gravitino mass in a universal fashion:

$$\Lambda_S = \sqrt{3 \ m_{3/2} \ M_P}$$

• The superpartner mass splittings depend on the sector I of the theory as:

 $(\Delta m^2)_I \sim \lambda_I \Lambda_S^2$

where λ_I is the (renormalized) Goldstino/gravitino coupling to sector I.

There are two rough avenues to arrange for $\Delta m \sim \text{TeV}$:

(A) Heavy gravitino mass \rightarrow large Λ_S , but very small λ_I .

(B) Light gravitino mass, and $\lambda_I \sim 1$.

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Beyond the Standard Model,
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Grand Unification: The idea

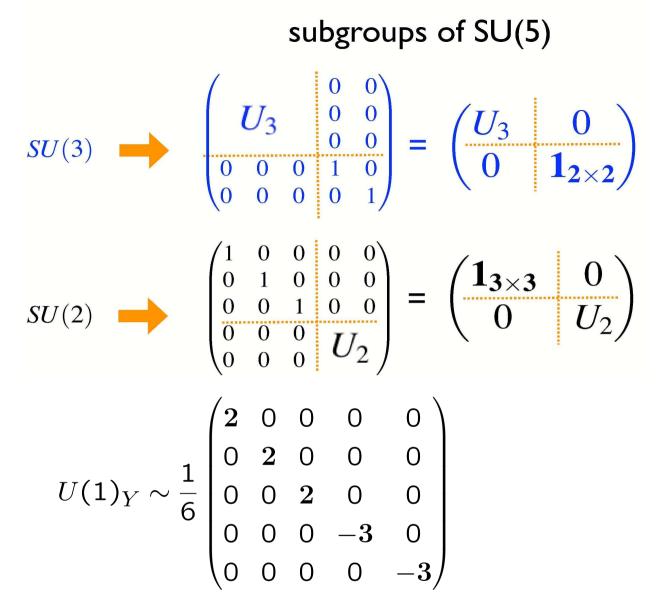
The Standard Model gauge group is not "fully unified". At higher energy, the symmetry becomes larger. At lower energies it breaks spontaneously to the standard model group: $SU(3) \times SU(2) \times U(1)_Y$

$$SU(3) \Longrightarrow U_3 U_3^{\dagger} = 1$$
 , $det(U_3) = 1$
 $SU(2) \Longrightarrow U_2 U_2^{\dagger} = 1$, $det(U_2) = 1$

We can include $SU(3) \times SU(2) \times U(1)_Y$ inside SU(5)

$$SU(5) \Longrightarrow U_5 U_5^{\dagger} = 1$$
 , $det(U_5) = 1$

Beyond the Standard Model,



Since $\dim(SU(5))=24$, there are 12 extra gauge bosons apart from the SM ones.

Beyond the Standard Model,

SU(5): the matter

$$\mathbf{10} = \begin{pmatrix} 0 & \bar{u}_3 & -\bar{u}_2 & u_1 & d_1 \\ -\bar{u}_3 & 0 & \bar{u}_1 & u_2 & d_2 \\ \bar{u}_2 & -\bar{u}_1 & 0 & u_3 & d_3 \\ -u_1 & -u_2 & -u_3 & 0 & \bar{e} \\ -d_1 & -d_2 & -d_3 & -\bar{e} & 0 \end{pmatrix} \qquad \bar{e}_R \qquad \bar{s} = \begin{pmatrix} \bar{d}_1 \\ \bar{d}_2 \\ \bar{d}_3 \\ \bar{d}_3 \\ \bar{e}_L \\ \bar{v}_L \end{pmatrix}$$

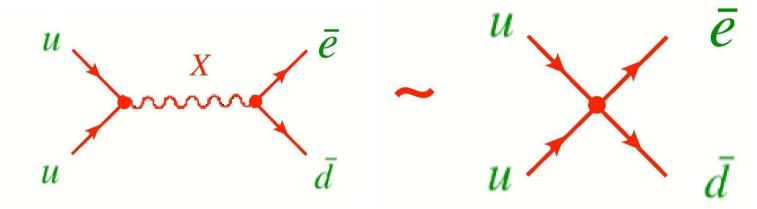
There should also be a singlet to accommodate ν_R .

- We have three copies of such representations to generate the three families.
- The new, larger symmetry mixes quarks and leptons: We expect baryon and lepton number to be violated by the new gauge interactions.

Beyond the Standard Model,



The SU(5) symmetry should break spontaneously at some high energy scale Λ_{GUT} to $SU(3) \times SU(2) \times U(1)_Y$ (via a new Higgs effect). The 12 extra gauge bosons X will acquire masses $M_X \sim \Lambda_{GUT}$.



As with the Fermi example this four-fermion effective interaction has a coupling $\sim \frac{g_5^2}{M_V^2}$

From experiment we obtain that
$$\tau_p > 2.6 \times 10^{33}$$
 years. This implies $M_X > 10^{15}~{\rm GeV}$

Beyond the Standard Model,

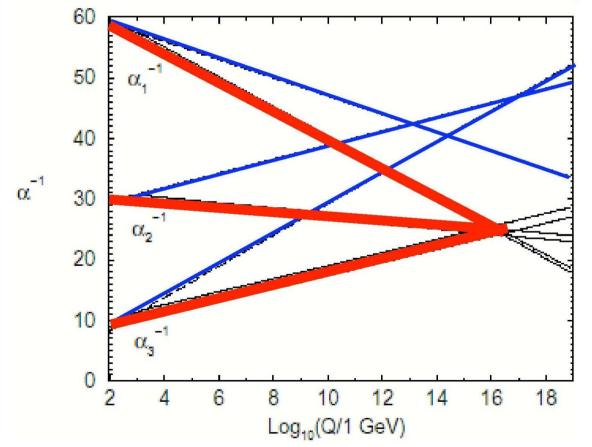
Coupling unification

We have coupling unification at the scale $\Lambda = M_X$

$$g_3 = g_2 = \sqrt{\frac{5}{3}} g_Y = g_5 \equiv g_{GUT}$$

This seems in good agreement with the data if we allow for the renormalization group

running



The gravitational coupling

The coupling of gravity, Newton's constant G_N has dimensions M^{-2} . This is how we define the Planck Mass : $G_N = M_{\text{Planck}}^{-2}$.

Gravitational force:

$$F = G_N \; \frac{M_1 \; M_2}{R^2} \sim G_N \; \frac{E_1 \; E_2}{R^2}$$

The dimensionless gravitational coupling runs fast with energy:

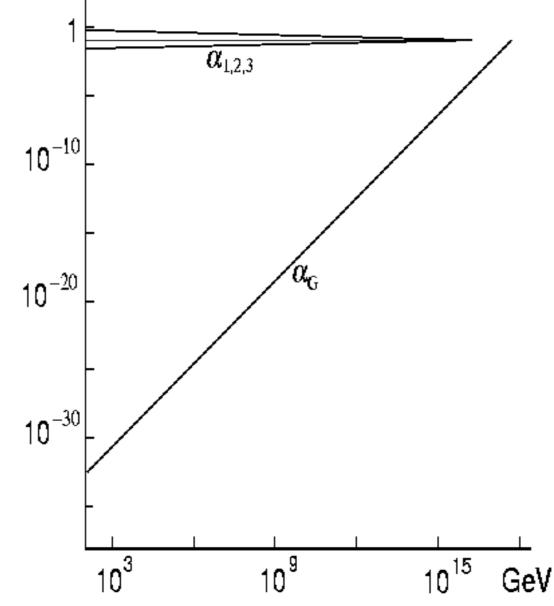
$$\alpha_{grav} \equiv G_N \ E^2 = \frac{E^2}{M_{\rm Planck}^2}$$

Beyond the Standard Model,

Gravity versus other interactions				
interaction	dimensionless coupling	strength		
Strong	$\alpha_s = \frac{g_s^2}{4\pi\hbar c}$	~ 1		
Electromagnetic	$\alpha_{\rm em} = rac{e^2}{4\pi\hbar c}$	$\sim rac{1}{137}$		
Weak	$G_F m_p^2$	$\sim 10^{-5}$		
Gravity	$G_N \ {m_p^2\over \hbar c}$	$\sim 10^{-36}$		

Therefore until now gravity has been safely neglected in particle physics.

The running of all couplings

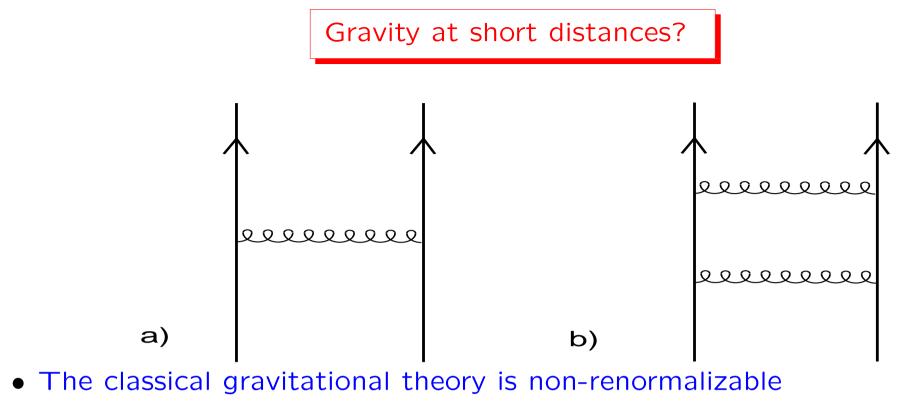


Beyond the Standard Model,

The existence of gravity is one of the most solid arguments that the SM is not the final theory.

- Gravity interacts with SM fields.
- At some high energy scale, Λ_P gravity will become strong, and quantum effects must be incorporated. This scale could be $M_P \sim 10^{19}$ GeV but (as we will see later) it could also be much lower.
- This fundamental theory, would look like classical gravity plus the SM at energies $E << \Lambda_P$.
- In this sense the SM is an effective theory, valid (at most) up to Λ_P .
- Things look bad, since classical gravity (general relativity) is a non-renormalizable theory.

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Beyond the Standard Model,
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(b)
$$\sim \frac{E^2}{M_{\text{Planck}}^4} \int_0^{\Lambda} dp \ p \sim \frac{\Lambda^2 \ E^2}{M_{\text{Planck}}^4},$$

- At higher orders it gets worse and worse.
- No clue as to what the short distance theory is.
- This has been an open problem for more than 50 years.

Beyond the Standard Model,

• String theory is a different framework for describing and unifying all interactions.

- It always includes quantum gravity, without UV problems (UV divergences)
- It also includes the other ingredients of the SM: Gauge interactions, chiral matter (fermions) and if needed, supersymmetry.
- It offers some conceptual features that are appealing to physicists:
- (a) String theory ALWAYS contains gravity
- (b) The existence of fermions implies supersymmetry at high energy.

(c) It has a priori no fundamental parameters but only one dimensionfull scale: the size of the strings. All dimensionless parameters of a given ground state of the theory are "dynamical" (expectation values of scalar fields).

(d) It contains solitonic extended objects (known as branes) that provide an incredible richness to the theory as well as a deep link between gauge theories and gravity.

Beyond the Standard Model,

Shift in paradigm: from point particle to a closed string.

• In QFT fields are "point-like". In string theory, they depend not on a point of space-time but a loop in space-time (the position of a closed string).

What is the difference between a closed "fundamental" string and a loop of wire?

(A) The fundamental string is much smaller: its size is definitely smaller than 10^{-18} m. This would explain why we have not seen one so far.

(B) Apart from the usual degrees of freedom (their coordinates in spacetime), fundamental strings have also fermionic degrees of freedom. There a kind of supersymmetry relating the coordinates to such fermionic degrees of freedom.

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Beyond the Standard Model,
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Since the smallest length we can see today (with accelerators) is approximately 10^{-18} m strings would appear in experiments so far as point-like objects.



• Fundamental strings, like the analogous classical objects, can vibrate in an infinite possible number of harmonics.

• Upon quantization, these harmonics behave like different particles in space-time.

A single string upon quantization \implies an infinite number of particles with ever increasing mass.

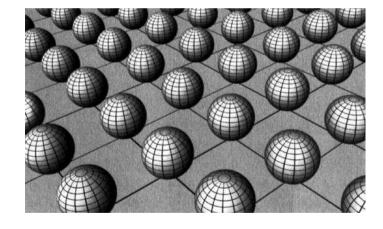
• Infinity of particles is responsible for the unusual properties of string theory (and its complicated structure).

• Strings live in diverse dimensions. Lorentz invariance \Leftrightarrow 9+1 dimensions. Although this seems to contradict common experience it can be compatible under certain circumstances. How do we see the extra dimensions?

Extra space dimensions

- The idea that space has extra, hitherto unobservable dimensions goes back to the beginning of the twentieth century, with Nordström (1914), Kaluza (1925) and Klein (1926).
- It comes naturally in string theory. How come they are not visible today?
- (A) Because they compact and sufficiently small.
- (B) Because we are "stuck" on the 4D world.
- (C) Because they are of a more bizarre kind (for example, they are discretized appropriately)





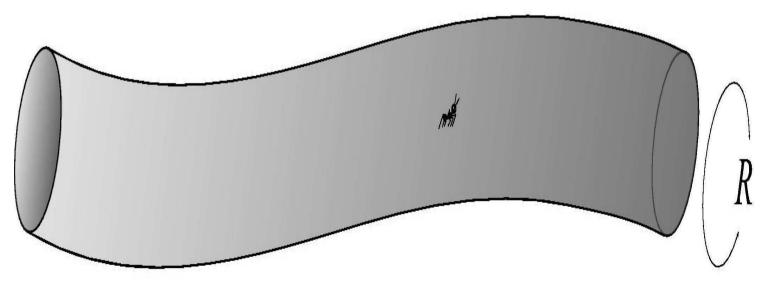


A compact, sufficiently small extra dimension is not visible !

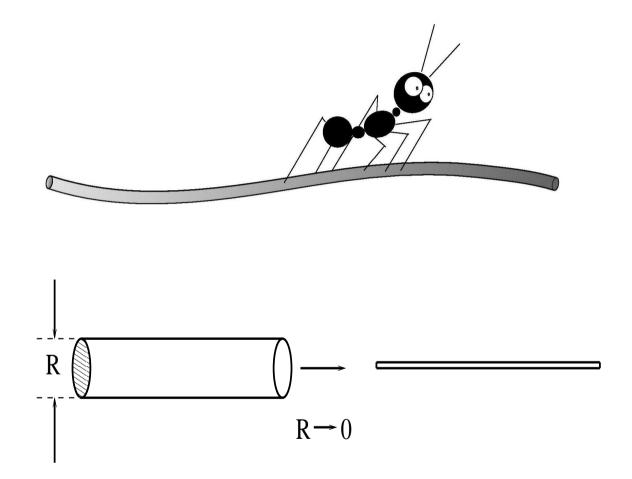
A simple example of a space with one compact (circle) and one noncompact (real line) dimension: a hose of infinite length and radius R.

There are two regimes:

(A) At distance << R the space looks like an (infinite) two-dimensional plane.



(B) At distance >> R the compact direction of the hose is invisible. The hose looks one-dimensional.



We will now make this intuition more precise.

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Beyond the Standard Model,
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Kaluza-Klein states

Consider the usual 3+1 dimensional space-time and a fifth dimension that is a circle of radius R. Consider also a free massless scalar field in this 5d space-time.

• From QM: the momentum on a circle is quantized.

$$\exp\left[ip_4 \ (x^4 + 2\pi R)\right] = \exp\left[i \ p_4 \ x^4\right] \longrightarrow p_4 = \frac{n}{R}$$

From the mass-less condition in 5 dimensions:

$$E^2 - \vec{p}^2 = 0 \rightarrow E^2 - p_1^2 - p_2^2 - p_3^2 - p_4^2 = 0 \rightarrow E^2 - p_1^2 - p_2^2 - p_3^2 = \frac{n^2}{R^2}$$

Compare with four-dimensional relation for massive particles:

$$E^2 - p_1^2 - p_2^2 - p_3^2 = M^2$$

This is equivalent to an infinite tower of four-dimensional particles (KK states) with masses

$$M_n = \frac{|n|}{R} \quad , \quad n \in \mathbb{Z}$$

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This result is generic and applies also to massive fields or fields with spin. (Exercise Derive the KK masses for a massive 5d scalar. Derive the analogous result for a 5-dimensional gauge field. What is the spin of 4-dimensional fields that are obtained and what are their masses?)

If at low energy, our available energy in accelerators is

$$E \lesssim \frac{1}{R}$$

none of the massive KK-states can be produced ("seen"). The extra dimension is invisible!

• When $E >> \frac{1}{R}$ several KK states can be produced and studied. When many have been seen the extra compact dimension can be reconstructed.

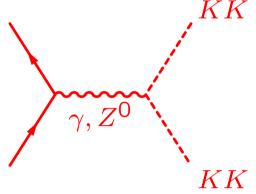
 \diamond The fact that till today in colliders we have not seen such states (with SM charges) gives a limit on R:

$$\frac{1}{R}$$
 > 300 GeV

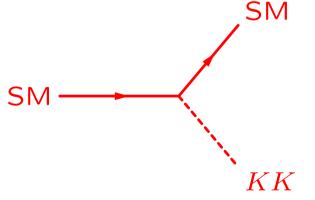
In LHC, there will be searches for KK states.

• Since a circle is translationally invariant, p_4 is conserved. n is therefore like a conserved KK U(1) charge.

• Therefore KK-states must be pair produced, so the threshold for their production is $\frac{2}{R}$.

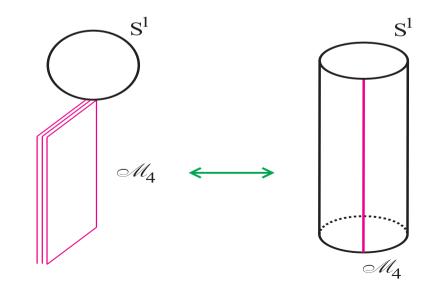


• There are cases where the extra dimension is not translationally invariant. (e.g. a finite interval) Then KK-charge is not conserved, KK states can be singly produced and the threshold for production is $\frac{1}{R}$.



Branes and large extra dimensions

- The collider bound on R: 1/R > 300 GeV can be simply evaded if the KK states carry no SM charges. In the simplest case they couple gravitationally.
- This setup is possible using the idea of branes.
- Consider $M_4 \times S^1$ as an example, with the circle of radius R.
- A 3-brane is a (hyper)-membrane with 3 spacial dimensions. We can imagine such a 3-brane embedded inside our (4+1)-dimensional space.



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 Branes are part of string theory. They have flug them.

- Such localized fields are typically gauge fields, fermions and scalars.
- We may therefore arrange that the SM fields live on such a 3-brane and cannot propagate in the rest n dimensions (the "bulk")

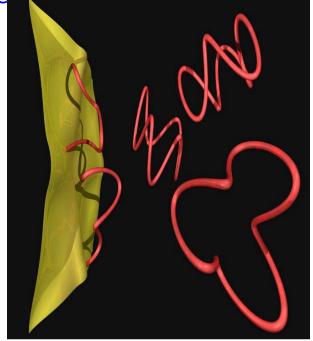
• The gravitational field on the other hand can propagate in all (4+1)directions.

Consider the Newton constant and Planck mass in a (4+N)-dimensional theory:

$$\mathcal{L} = \frac{1}{G_{4+N}} \int d^{4+N} x \ \sqrt{g} \ R_{N+4} \quad , \quad G_{4+N} \sim \frac{1}{M_*^{(N+2)}}$$

$$d^{4+N}x \sqrt{g} R_{N+4}$$
 , $G_{4+N} \sim \frac{1}{\sqrt{N}}$

on



• At distances $l \ll R$ gravity is effectively (4+N)-dimensional.

• At large distances l >> R gravity is four-dimensional. The effective 4D Newton constant $G_4 = M_P^{-2}$ can be calculated from

 $V(r) \sim rac{1}{r^{1+N}}$

$$M_*^{N+2} \int d^{4+N}x \,\sqrt{g} \,R_{4+N} \sim M_*^{N+2}R^N \int d^4x \,\sqrt{g} \,R_4$$
$$\frac{1}{G_4} \sim M_P^2 \sim M_*^{(N+2)}R^n$$

By choosing appropriately the size of extra dimensions

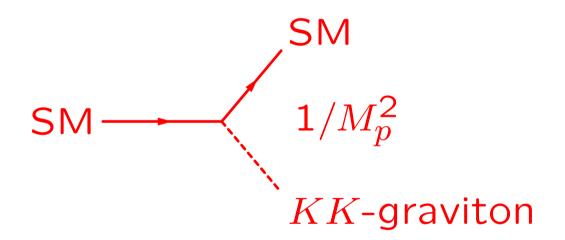
$$R \sim 10^{\frac{32}{N}} \text{TeV}^{-1} \sim 10^{\frac{32}{N}-12} \text{ eV}^{-1} \sim 10^{\frac{32}{N}-16} \text{ mm}$$

we can arrange that the quantum gravity scale of the full theory

 M_* is as low as 1 TeV while $M_P = 10^{19}$ GeV.

Beyond the Standard Model,

- SM particles have no KK descendants (no bulk propagation). They do not directly feel the extra dimensions. The collider bound on R is not relevant here.
- The graviton has KK descendants, with the usual masses $\frac{|n|}{R}$. They couple to SM matter gravitationally.
- Each KK graviton couples with strength M_P^{-2} which is very weak.



• However, the existence of many KK-gravitons enhances this coupling (more later).

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Beyond the Standard Model,
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- For two extra dimensions their size can be 0.1 mm !!! How come we have not seen such a "large dimension"?
- It cannot be seen at accelerators because of the weak coupling of KK gravitons. (It becomes substantial at 1 TeV or more).
- For distances smaller than 0.1 mm gravity becomes higher-dimensional :

$$F \sim \frac{1}{r^{2+N}}$$
 or $V \sim \frac{1}{r^{1+N}}$

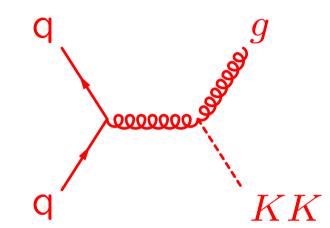
(Exercise : The compact Newton's law Show that the Newtonian force with N compact dimensions all of radius R is $F = G_* M^2 \sum_{\vec{n} \in Z^N} \frac{1}{|\vec{r}+2\pi R\vec{n}|^{(N+2)}}$ where \vec{n} is a vector of integers)

Surprisingly, until recently the gravitational law has been measured only up to distances of 1 mm! Today, the limiting distance has gone down to 10 μ m.

Where can we see signals for all this?

(A) From tabletop short distance experiments Beyond the Standard Model,

(B) At LHC. The signal is missing energy due to brehmstralung into KK gravitons that escape undetected in the bulk.



For
$$E >> \frac{1}{R}$$

 $\sigma \sim \frac{1}{M_P^2} (\# of KK gravitons) \sim \frac{1}{M_P^2} (ER)^N \sim \frac{1}{M_*^2} (EM_*)^N$
Exercise: calculate the number $(ER)^N$ of KK states that can contribute to this process.)
Here you may find some cross sections for KK-graviton production at LHC.

Further reading:[arXiv:hep-ph/0503148]

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Beyond the Standard Model,
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Black holes at colliders?

Black holes are very special (and singular) solutions of GR

$$ds^{2} = -f(r)dt^{2} + \frac{dr^{2}}{f(r)} + r^{2}(d\theta^{2} + \sin^{2}\theta \ d\phi^{2})$$

$$f(r) = 1 - \frac{2M}{M_P^2 r}$$
, $f(R) = 0 \rightarrow R = 2 \frac{M}{M_P^2} = 2 \frac{M}{M_P} \ell_P$

Far away, $r \to \infty$ the space is flat

$$ds^{2} = -dt^{2} + dr^{2} + r^{2}(d\theta^{2} + \sin^{2}\theta \ d\phi^{2}) = -dt^{2} + dx^{i}dx^{i}$$

- r = R is the horizon, r = 0 is the singularity.
- Black holes are classically stable (and "hungry").
- In the quantum theory they decay via Hawking radiation.
- This fact is correlated with many of the theoretical puzzles posed by black-holes (black-hole thermodynamics and "the black-hole information paradox").

The black-hole information saga

• Particles with masses $M \ll M_P$ have an invisible horizon size: $R \ll \ell_P$ But very massive particles $M \gg M_P$ have a macroscopic horizon: $R \gg \ell_P$ They should be treated as black holes

• In the case of large extra dimensions, the higher-dimensional Planck scale M_* is much smaller than the four-dimensional one M_P .

$$rac{M_P^2}{M_*^2} \sim (M_*R)^n \sim \left(rac{R}{\ell_*}
ight)^N \gg 1$$

• If $M_* \sim 1$ TeV then multi-TeV particles will behave as (higher-dimensional*) black holes.

- They will be created during a collision, and they will decay (democratically) via Hawking radiation.
- Although we do not yet control the details of such processes at LHC energies, we may be faced with such events at LHC

Further reading: start from hep-ph/0111230

Exercise*: Derive the higher-dimensional black-hole solution, by thinking simply about its asymptotic properties. In particular it must satisfy the (higher-dimensional) Poisson equation.

Beyond the Standard Model,

Conclusions

We have seen that we already have experimental data that cannot be explained in the context of the Standard Model,

- Neutrino masses and mixings.
- Dark matter.
- Dark Energy.

We have also seen many ideas that attempt to unify the forces, make a UV stable theory, incorporate gravity, and try to explain the data above.

No theory so far can successfully accommodate all three data above.

We need input from experiments!

Happily, data are still flowing in from cosmological observations, and accelerators like LHC are expected to provide complementary views of the fundamental physical theory.

♦ We do count on your help!

The (old) quest for understanding nature is still on!

Thank you!

Beyond the Standard Model,

The Standard Model: ingredients

A review of the ingredients

Gauge groups

Strong force: $SU(3)_{color} \rightarrow three colors.$

Carriers: gluons are spin-one octets

 \rightarrow (color/anti-color) combinations. (SU(N) \rightarrow N²-1 gauge bosons)

They are confined inside hadrons \Rightarrow "glue".

• The electroweak force: $SU(2) \times U(1)_Y$, it is spontaneously broken to $U(1)_{EM}$ by the Higgs effect.

Carriers: W^{\pm} , Z^{0} (massive), γ (massless)

Beyond the Standard Model,

Standard Model: the quarks

Left-handed:

$$\begin{pmatrix} U_L \\ D_L \end{pmatrix}^a_{\frac{1}{6}}, \qquad \begin{pmatrix} C_L \\ S_L \end{pmatrix}^a_{\frac{1}{6}}, \qquad \begin{pmatrix} T_L \\ B_L \end{pmatrix}^a_{\frac{1}{6}}, \qquad \begin{pmatrix} T_L \\ B_L \end{pmatrix}^a_{\frac{1}{6}},$$

a=red, blue, green

Right-handed:
$$\begin{pmatrix} U_R \end{pmatrix}_{\frac{2}{3}}^a$$
, $\begin{pmatrix} D_R \end{pmatrix}_{-\frac{1}{3}}^a$, $\begin{pmatrix} C_R \end{pmatrix}_{\frac{2}{3}}^a$, $\begin{pmatrix} S_R \end{pmatrix}_{-\frac{1}{3}}^a$, $\begin{pmatrix} T_R \end{pmatrix}_{\frac{2}{3}}^a$, $\begin{pmatrix} B_R \end{pmatrix}_{-\frac{1}{3}}^a$

The SM is a chiral theory.

Beyond the Standard Model,

Standard Model: the leptons

Left-handed:
$$\begin{pmatrix} \nu_e \\ e_L \end{pmatrix}_{-\frac{1}{2}}$$
, $\begin{pmatrix} \nu_\mu \\ \mu_L \end{pmatrix}_{-\frac{1}{2}}$, $\begin{pmatrix} \nu_\tau \\ \tau_L \end{pmatrix}_{-\frac{1}{2}}$
Right-handed $\begin{pmatrix} e_R \end{pmatrix}_{-1}$, $\begin{pmatrix} \mu_R \end{pmatrix}_{-1}$, $\begin{pmatrix} \tau_R \end{pmatrix}_{-1}$

and

$$\left(\begin{array}{c} \nu_e^R \\ \end{array} \right)_0 \quad , \quad \left(\begin{array}{c} \nu_\mu^R \\ \end{array} \right)_0 \quad , \quad \left(\begin{array}{c} \nu_\tau^R \\ \end{array} \right)_0$$

For the neutrino sector you will learn the recent developments from the forthcoming lectures of J. Gomez-Cadenas

All fermions come in three copies called families.

Beyond the Standard Model,

Standard Model: the Higgs

- The SM has interaction carriers with spin-one and "matter" with spin- $\frac{1}{2}$
- There is a spin-0 player as well: the Higgs. It is a (complex)-scalar SU(2) doublet with hypercharge $\frac{1}{2}$. Its "raison d'être" : break the electroweak symmetry spontaneously. As a result it gives masses to matter particles.
- Three of its components

$$H^{\pm}$$
, $Im(H^0)$

become the third components of the massive gauge bosons

$$W^{\pm}$$
 , Z^{0}

after electro-weak symmetry breaking.

• The fourth, $\operatorname{Re}(H^0) \Rightarrow$ physical neutral scalar that we expect to see at LHC.

Beyond the Standard Model,

How parameters affect us: some answers

• $v_F \rightarrow 0$ then p is unstable to decay to neutrons \rightarrow no Hydrogen. The reason:

$$m_n - m_p \simeq m_d - m_u + E_n^{\mathsf{EM}} - E_p^{\mathsf{EM}}$$

The EM mass difference $E_n^{\mathsf{EM}} - E_p^{\mathsf{EM}} \sim -1.7$ MeV is independent of v_F . By lowering v_F we can make $m_d - m_u \simeq (\lambda_d - \lambda_u)v_F > 0$ very small. Then the EM Mass difference dominates and $m_p > m_n$.

• $v_F >> 170 GeV$ n-p mass difference is very large and the nuclear force becomes of shorter range \rightarrow nothing but hydrogen in the universe.

From the GellMann-Oakes-Reines relation $m_{\pi}^2 = (m_u + m_d) \frac{\sigma}{f_{\pi}^2}$. The range of the nuclear force (roughly due to the exchange of pions) is about $1/m_{\pi}$. The deuteron becomes unbound. Eventually, the neutron becomes heavier than proton plus its nuclear binding energy: bound neutrons would decay to protons and complex nuclei cease to exist. Much later only $\Delta^{++} = uuu$ would become the only stable particle See [arXiv:hep-ph/9801253] for more information RETURN

Beyond the Standard Model,

Other parameters

There are others parameters, measured in the SM, whose values are not explained:

• The elements of the Kobayashi-Maskawa matrix: three mixing angles and a phase that controls CP violation. There is a similar matrix for the Neutrino sector.

• A non-perturbative parameter: the θ -angle of QCD: $\sim \theta \int d^4x \ \epsilon^{\mu\nu\rho\sigma} Tr[F_{\mu\nu}F_{\rho\sigma}]$

A non-zero value breaks CP in the strong interactions (contrary to observations.) This is the "strong CP-problem"

Experimentally

$$d_n \lesssim 10^{-25} \ e \ {
m cm} \ o \ heta \lesssim 2 imes 10^{-10}$$
 Return

The compact Newton's law

Assume 3+1 non-compact dimensions, and a single compact direction of radius $R(x^4 \rightarrow x^4 + 2\pi R)$. The Newton's law, obtained by the method of images is

$$F = \frac{M_1 M_2}{M_*^3} \sum_{n \in \mathbb{Z}} \frac{1}{\left[(x^1)^2 + (x^2)^2 + (x^3)^2 + (x^4 + 2\pi nR)^2 \right]^{\frac{3}{2}}}$$
$$r = \sqrt{(x^1)^2 + (x^2)^2 + (x^3)^2}$$

is the usual distance in 3+1 dimensions.

• When $r \ll R$, all other images $n \neq 0$ are far away and can be neglected. Therefore we have 5d gravity.

$$F(r << R) \simeq rac{M_1 M_2}{M_*^3 \ r^3}$$

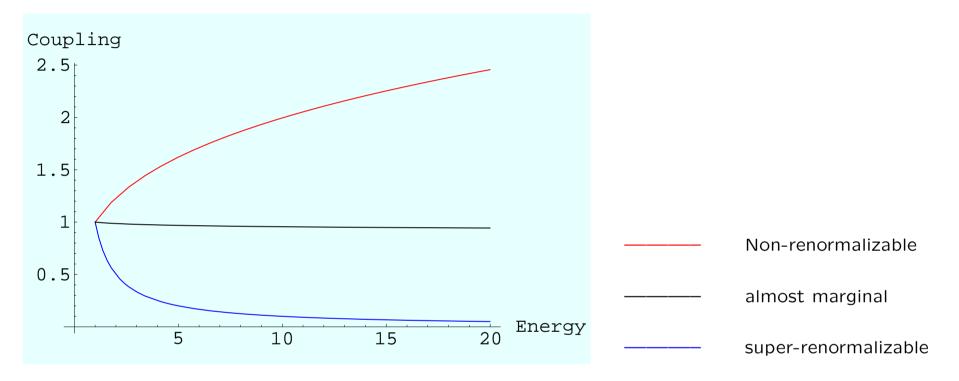
• When r >> R all images give equally important contributions. The result can be obtained by a Poisson resummation

$$\sum_{n \in \mathbb{Z}} \frac{1}{[r^2 + (x^4 + 2\pi nR)^2]^{\frac{3}{2}}} \simeq \frac{1}{\pi Rr^2} \left[1 + \mathcal{O}\left(\frac{R}{r}\right) \right]$$
$$F(r >> R) \simeq \frac{M_1 M_2}{\pi M_*^3 R} \frac{1}{r^2} \quad , \quad M_P^2 = \pi M_*^3 R$$

Beyond the Standard Model,

Renormalization: the coupling constants

• Couplings λ_i depend on energy, E: $\lambda_i(E)$. This dependence is the result of including virtual effects at higher energies than E (shorter distances).



• Couplings can be irrelevant (non-renormalizable),

$$\lambda(E) = \lambda(E_0) \left(\frac{E}{E_0}\right)^{\Delta - 4} , \quad \Delta > 4$$

relevant (super-renormalizable), or almost marginal (renormalizable, log running).

$$\lambda(E) = \frac{1}{\frac{1}{\lambda(E_0)} + b_0 \log \frac{E}{E_0}}$$

• We define a theory (via its couplings) at $E = \infty$ and uniquely determine (by calculating the quantum effects) the couplings at any lower energy (renormalization group flow).

- The reverse is not possible: we cannot guess the high-energy theory from the low-energy couplings. Two distinct theories can have the same low energy theory (universality).
- The couplings $\lambda_i(E)$ define the EFFECTIVE theory at energy E. It captures the low energy physics.
- When we make measurements at accelerators , we measure the effective couplings $\lambda_i(E_{\text{experiment}})$.
- Our goal is to find the UV couplings (complete specification of the theory).

Renormalization: Further reading

The following are introductory texts requiring mostly undergraduate knowledge.

- G. P. Lepage, "What is renormalization", [arXiv:hep-ph/0506330]
- J. Alexandre, "Concepts of renormalization in physics", [arXiv:physics/0508179]
- B. Delamotte, "A hint of renormalization", [arXiv:hep-th/0212049]

For the renormalization group in statistical mechanics:

• H. Maris and L. Kadanoff, "Teaching the renormalization group", Am. J. of Phys. 46 (1978) 652.

RETURN

mGMSB

• There is a source of supersymmetry breaking due to a vev $\langle X \rangle = M + \theta^2 F$ in a hidden (secluded) sector.

• There are messenger superfields in complete SU(5) reps (not to upset gauge coupling unification) Φ_i that couple as $\lambda_{ij} \bar{\Phi}_i X \Phi_j$ both to the secluded and the SSM sector. They modify the GUT scale coupling as

$$\delta \alpha_{GUT}^{-1} = -\frac{N}{2\pi} \log \frac{M_{GUT}}{M} \quad , \quad N = \sum_i n_i$$

• Diagonalize and absorb λ 's into $(M, F) \rightarrow (M_i, F_i)$. Then the gaugino and scalar masses are given by

$$M_{a} = k_{a} \frac{\alpha_{a}}{4\pi} \Lambda_{G} \quad , \quad \Lambda_{G} = \sum_{i} n_{i} \frac{F_{i}}{M_{i}} \quad , \quad k_{Y} = \frac{5}{3} \quad , \quad k_{2} = k_{3} = 1$$
$$m_{i}^{2}(t) = 2 \sum_{a=1}^{3} C_{a}^{i} \quad k_{a} \frac{\alpha_{a}^{2}(0)}{(4\pi)^{2}} \left[\Lambda_{S}^{2} + h_{a} \Lambda_{G}^{2}\right] \quad , \quad h_{a} = \frac{k_{a}}{b_{a}} \left[1 - \frac{\alpha_{a}^{2}(t)}{\alpha_{a}^{2}(0)}\right] \quad , \quad \Lambda_{S}^{2} = N \frac{F^{2}}{M^{2}}$$

• The MSSM soft parameters are here parameterized by $(M, N, \Lambda_G, \tan\beta, \operatorname{sign}(\mu))$ Further reading: $[\operatorname{arXiv:hep-ph/9801271}]$

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Beyond the Standard Model,
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- The idea of anomaly mediated supersymmetry breaking comes from brane realizations of the SM.
- The "hidden" sector where supersymmetry breaks spontaneously is localized on a brane different from the SSM-brane.
- The breaking of supersymmetry is communicated to the SSM via the Weyl anomaly.
- The form of the gaugino and scalar soft masses is of the form

$$M_a = \beta_a M$$
, $m_i^2 = m_0^2 - C_i^a \beta_a M^2$

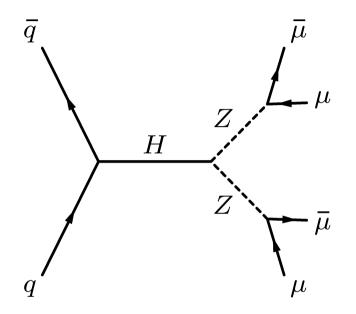
where M is a characteristic energy scale and m_0 a phenomenological parameter and β_a the gauge β -functions.

• This mechanism is still in its infancy and has many obscure points. It is known as mAMSB and characterized by the parameters $(m_0, M, \tan\beta, \operatorname{sign}(\mu))$

Further reading:[arXiv:hep-th/9810155], [arXiv:hep-ph/9810442]

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Beyond the Standard Model,
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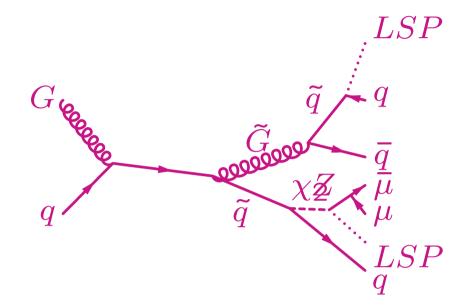
Higgs Event



Higgs \rightarrow ZZ \rightarrow $\mu\mu\mu\mu$ event

Beyond the Standard Model,

First SUSY event



The events were generated by Maria Spiropulu for the following SUSY mSUGRA parameters:

$$aneta=10$$
 , $m_{rac{1}{2}}=285$ GeV , $m_0=210$ GeV , $A=0, {
m sign}(\mu)=+1$

This is known as the LM4 mSUGRA Point.

For these parameters the squark (gluino) masses are about 600 (700) GeV and the lightest neutralino, which escapes direct detection, has a mass of 114 GeV.

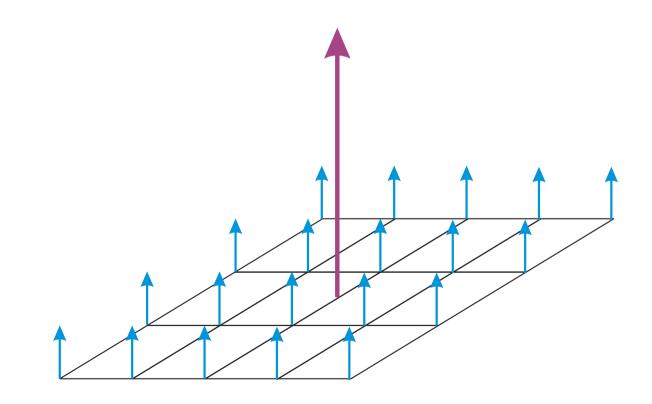
See http://iguanacms.web.cern.ch/iguanacms/gallery-page4.html

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Beyond the Standard Model,
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Effective Field Theory: Wilson's View

A Quantum Field Theory is defined (by e.g. a Lagrangian) at a high energy scale Λ , usually called the "cut-off" scale.

In standard space-time, this means that it is defined at some minimum distance, e.g. on a space-time lattice with a minimum length.



• Once it is defined at this high scale we can compute its (quantum) physics at any lower energy scale E.

This is done by "averaging" over the quantum effects associated with all energies between the cut-off Λ and the energy of interest E. in practice and in perturbation theory this amounts of integrating the internal momenta of Feynman diagrams between Λ and E

Let us take a simple example of a scalar theory that at the high energy cutoff has a Lagrangian

$$L_{\Lambda} = \frac{1}{2} (\partial \phi)^2 + \lambda_2 \phi^2 + \lambda_1 \phi^3 + \lambda_0 \phi^4 + \lambda_{-1} \phi^5 + \cdots$$

 $dim(\phi) = 1 \qquad \Rightarrow \qquad \lambda_n \simeq M^n$

Note that $n \ge 0$ corresponds to what we call renormalizable interactions.

We now want to find the effective theory at a much lower energy scale $E << \Lambda$. By doing the (quantum computations) we can determine the interactions of the effective theory at the energy scale E:

$$L_E = \frac{1}{2} (\partial \phi)^2 + \tilde{\lambda}_2 \phi^2 + \tilde{\lambda}_1 \phi^3 + \tilde{\lambda}_0 \phi^4 + \tilde{\lambda}_{-1} \phi^5 + \cdots$$

All possible terms are generated, compatible with the symmetries!

The $\tilde{\lambda}_n$ are functions of all the λ_n and Λ, E . The transformation that brings us from the high energy couplings to the low energy effective couplings is called a renormalization group transformation. It is determined by the dynamics of the high energy (short distance) theory.

Moreover, generically (exercise),

 $\tilde{\lambda}_n \sim \Lambda^n$

Therefore et low energy $E \ll \Lambda$, high-dimension (non-renormalizable interactions) are suppressed as inverse powers of the high energy scale Λ . For $\Lambda = \infty$, $\tilde{\lambda}_{n < 0} = 0$.

On the other hand, (modulo exceptions), renormalizable interactions become large.

The measurable ("physical") quantities are the low energy ones: $\tilde{\lambda}_n$.

Note an **asymmetry** in this picture:

- A high-energy theory determines all lower-energy theories.
- A low-energy theory DOES NOT determine the higher-energy theories.

There is a similarity between the irreversibility of renormalization group flow and irreversibility in thermodynamics.

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Beyond the Standard Model,
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Unfortunately, we are constrained to to try to built the theory starting from low energy. And for this we built it step by step in energy.

We can equivalently phrase the problem as: We know the theory at energies 200 GeV (and below). What can we say about higher energies?

Renormalization: the old view

In the traditional approach:

- $\Lambda = \infty$. The theory is defined to make sense at all possible energies.
- $\lambda_{n>0}(\infty) = 0$

Since

$$\tilde{\lambda}_n(E) \sim \Lambda^n$$

- Effective dimension > 4 interactions are insensitive to high energy physics.
- Effective dimension \leq 4 couplings are infinite. We must choose carefully the $\lambda_n(\infty)$ so that this infinity cancels.

$$\tilde{\lambda}_2(E) = \lambda_2 + a\Lambda^2 + b\lambda_2 \log \frac{E^2}{\Lambda^2} + \text{finite} \text{ as } \Lambda \to \infty$$

Choose

$$\lambda_2 = -a\Lambda^2 - b\lambda_2 \log \frac{E^2}{\Lambda^2}$$

Beyond the Standard Model,

Renormalized couplings: a concrete example

Consider that there exists at low energy a single scalar ϕ and we write the basic interactions at a high scale Λ . (this is the definition scale. At higher scales the theory may change):

$$S = \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi + \frac{m_0^2}{2} \phi^2 + \lambda_0 \phi^4$$

We now calculate various low energy parameters, at a given scale $E_0 << \Lambda$.

$$m^{2}(E_{0}) = m_{0}^{2} - \xi_{1}\Lambda^{2} + \cdots , \quad \frac{1}{\lambda(E_{0})} = \frac{1}{\lambda_{0}} - b_{0}\log\frac{E_{0}}{\Lambda} + \cdots$$

These are obtained from the two and four-point functions or equivalently from $\sigma_{2\to 2}$. If we now compute a 2 \rightarrow 4 scattering cross section

$$\sigma_{2\to4}(m(E_0),\lambda(E_0),\Lambda) \simeq \frac{\lambda_0^2}{m_0^2} \sim \frac{\lambda(E_0)^2}{m(E_0)^2 + \xi_1 \Lambda^2}$$

From this we can "measure" $\Lambda = \Lambda_*$. If $\Lambda_* \neq \infty$ then the theory must change at $E \sim \Lambda_*$.

If instead we look at a theory like EM with a massive fermion, then both the gauge coupling constant and mass run logarithmically. Smaller sensitivity at the Λ scale.

A simple example of a softly-broken supersymmetric theory

We consider a theory that contains the supersymmetric chiral multiplets, Φ_i , i = 1, 2, 3. Each contains a complex scalar ϕ_i and a Weyl Fermion, ψ_i .

$$\Phi_i \equiv (\phi_i, \psi_i)$$

We will not include gauge interactions. In this case the only interactions will come from the superpotential. It must be written in terms of the chiral multiplets Φ_i but not of their conjugates, $\bar{\Phi}_i \equiv (\phi^*, \psi_c^i)$. We will choose it to be simple:

 $W = h \Phi_1 \Phi_2 \Phi_3$

We fist compute the Yukawa couplings using $\sum_{i,j} \frac{\partial^2 W}{\partial \phi_i \partial \phi_i} \overline{\psi}_i \psi_j$ to find

$$\mathcal{L}_{Yukawa} = h(\phi_2 \ \bar{\psi}_3 \psi_3 + \phi_2 \ \bar{\psi}_1 \psi_3 + \phi_3 \ \bar{\psi}_1 \psi_2) + c.c.$$

We then compute the potential from $V = \sum_i |F_i|^2 = \sum_i \left|\frac{\partial W}{\partial \phi_i}\right|^2$ (there are no D-terms as there is no gauge group and gauge interactions)

$$V = |h|^2 \left[|\phi_1 \phi_2|^2 + |\phi_1 \phi_3|^2 + |\phi_2 \phi_3|^2 \right]$$

It contains only quartic couplings of the scalars. The complete supersymmetric Lagrangian is therefore

$$\mathcal{L} = \mathcal{L}_{\text{kinetic}} + \mathcal{L}_{\text{Yukawa}} - V$$

where $\mathcal{L}_{\text{kinetic}}$ contains the standard kinetic terms

$$\mathcal{L}_{\text{kinetic}} = \frac{1}{2} \sum_{i=1}^{3} \partial_{\mu} \phi_{i} \partial^{\mu} \phi_{i}^{*} + \sum_{i=1}^{3} \bar{\psi}_{i} \partial \psi_{i}$$

We will now add all allowed soft terms that would be present id supersymmetry is broken:

• Masses \tilde{m}_i for the scalars of the chiral multiplets.

$$\mathcal{L}_{\text{mass}}^{\text{soft-sb}} = \frac{1}{2} \sum_{i=1}^{3} \tilde{m}_{i}^{2} \phi_{i} \phi_{i}^{*}$$

• Cubic couplings for the scalars proportional to the superpotential couplings: The only superpotential non-zero coupling is $\Phi_1 \Phi_2 \Phi_3$ so

$$\mathcal{L}_{\text{cubic}}^{\text{soft-sb}} = A(\phi_1^* \phi_2 \phi_3 + \phi_1 \phi_2^* \phi_3 + \phi_1 \phi_2 \phi_3^*) + c.c.$$

• Gaugino masses are also soft, but there are no gaugini in this simple theory.

Exercise so that you see if you understood the above:

Exercise 1:Consider now the same theory with the following superpotential $W = \sum_{i=1}^{3} \left[h_i \ \Phi_i^3 + \mu_i \Phi_i^2 + \zeta_i \Phi_i \right]$ Repeat the procedure above to produce the softly broken supersymmetric actionExercise 2:Go back now to the MSSM superpotential derive the Yukawa couplings and the potentialand the soft breaking terms.

Beyond the Standard Model,

SSB: Heavy gravitino mass

- Here the supersymmetry breakings happens in a "hidden sector".
- It is communicated to the observable sector by the gravitational interaction

$$\lambda_I \sim \frac{\Lambda_S^2}{M_P^2}$$
 , $\Lambda_S \sim \sqrt{(\Delta m)M_P} \sim 10^{10} - 10^{11} \text{ GeV}$, $m_{3/2} \sim 1 \text{ TeV}$

Taking the limit $M_P \rightarrow \infty$ to recover the EFT, we obtain the MSSM with typically universal soft terms.

- Such breaking can be realized in supergravity and in superstring vacua where susy is broken by hidden gaugino condensation.
- The EFT is MSSM and is valid up to close the Planck scale.
- There is another "mechanism" in this class: Anomaly Mediated Susy Breaking.

Further reading: http://doc.cern.ch/cernrep/1998/98-03/98-03.html

Beyond the Standard Model,

SSB: Light gravitino mass

This may be realized when supersymmetry is broken in a hidden sector, and is communicated to the observable sector by gauge or Yukawa interactions. Here $\lambda_I \sim \mathcal{O}(1)$.

• To obtain the desired mass splittings, $\Lambda_S \sim \text{TeV}$ and therefore $m_{3/2} \sim 10^3 - 10^{-5} \text{ eV}$.

• A class of models realizing this supersymmetry breaking pattern are known as messenger or gauge mediated supersymmetry breaking models. They contain apart from the observable sector, the "messenger" sector and the "hidden" sector.

• Here the gravitino is part of the low energy spectrum and its Goldstino component couples to the low energy fields with strength that ranges from order the gauge couplings to several orders smaller.

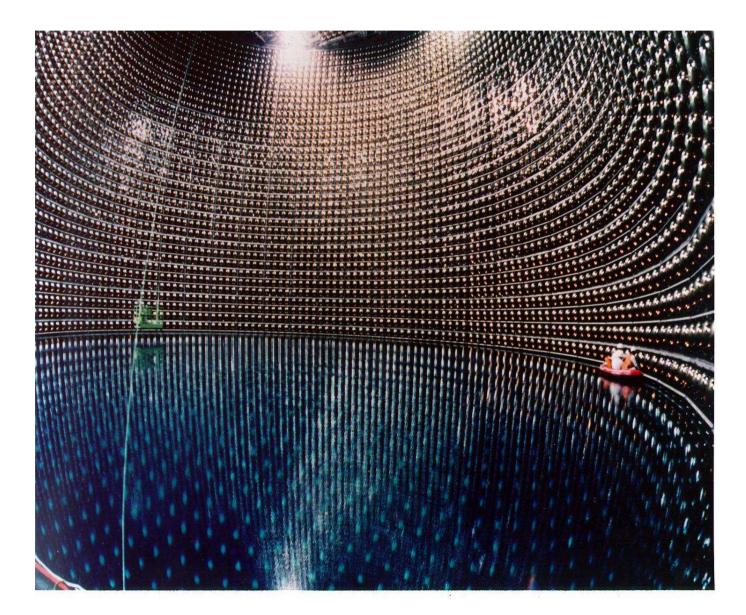
- Such theories have new physics well below the Planck scale.
- The LSP is the gravitino.

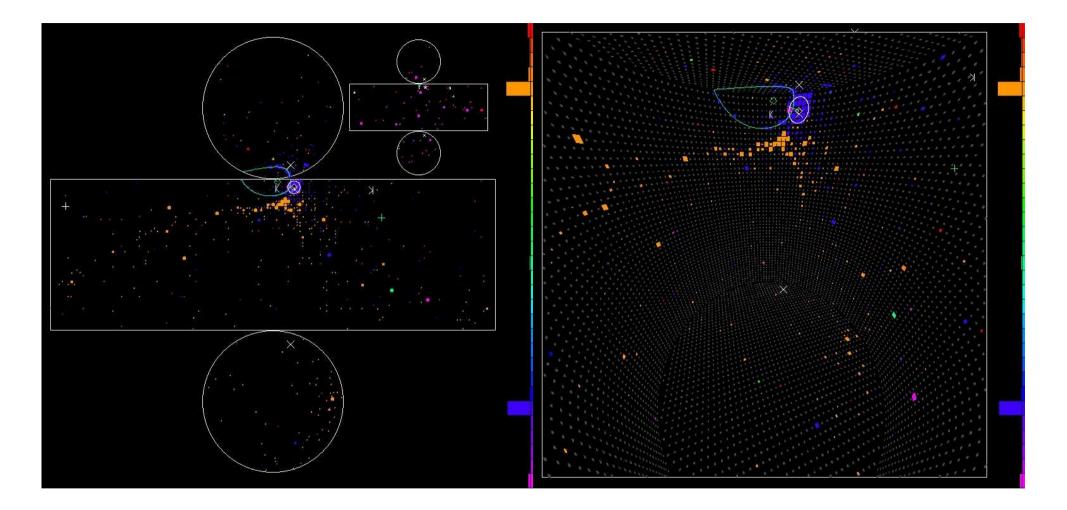
Further reading: http://doc.cern.ch/cernrep/1998/98-03/98-03.html

Beyond the Standard Model,



Large detectors (known today also as "neutrino telescopes") search for signals from the decay of protons.





Neutrino event inside the SKM detector. It could come from one of the potential decay channels of the proton. RETURN

Beyond the Standard Model,

Proton decay channels

In standard GUTs the nucleon decay channels are as follows:

 $p \to \pi^{0} + e^{+} \quad \text{or} \quad p \to \pi^{0} + \mu^{+}$ $p \to K^{+} + \bar{\nu}$ $p \to K^{0} + e^{+} \quad \text{or} \quad p \to K^{0} + \mu^{+}$ $n \to K^{0} + \bar{\nu}$

See http://arxiv.org/pdf/hep-ph/0211024 RETURN

Beyond the Standard Model,

Hypercharge normalization

We have seen that

$$Y = \frac{1}{6} \begin{pmatrix} 2 & 0 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 & 0 \\ 0 & 0 & 0 & -3 & 0 \\ 0 & 0 & 0 & 0 & -3 \end{pmatrix}$$

But we use matrices normalized to 1/2 to define the gauge theory

$$T_Y = \xi \ Y \quad , \quad Tr[T_Y T_Y] = \frac{1}{2} \quad , \quad \xi = \sqrt{\frac{3}{5}}$$

so that

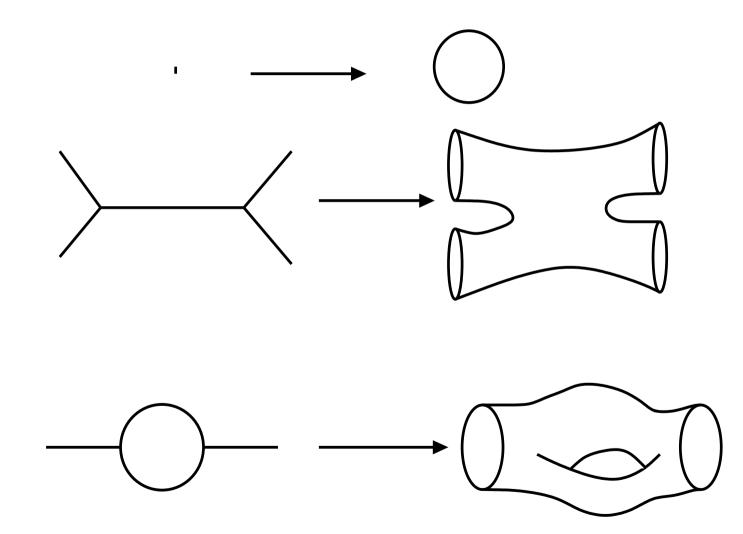
$$A_{\mu} = T_Y B_{\mu} \quad , \quad \delta L = -\frac{1}{2} Tr[F_A]^2 + g_{GUT} Tr[A_{\mu}J^{\mu}] = -\frac{1}{4} F_B^2 + \xi g_{GUT} Tr[Y B_{\mu}J^{\mu}]$$

$$g_Y = \xi \ g_{\text{GUT}} = \sqrt{\frac{3}{5}} \ g_{\text{GUT}}$$

Beyond the Standard Model,

String Theory, Vol III

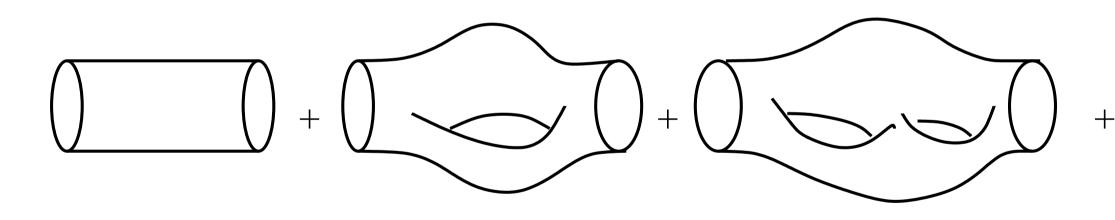
• In perturbation theory, standard QFT Feynman diagrams are replaced with string diagrams (two-dimensional surfaces)



Beyond the Standard Model,

♣ In QFT perturbation theory is formulated using Feynman diagrams.

♠ In string theory we have Riemann surfaces. For closed strings, each order contains a single diagram. At low energy, they reduce to the (many) QFT Feynman diagrams.



• String theory diagrams, when appropriately defined, give finite amplitudes in the UV. Quantum gravity, which is part of string theory is essentially finite.

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Beyond the Standard Model,
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Kaluza-Klein states in string theory

In string theory the KK spectrum is more complex: beyond the usual KK states, the string can wind around the circle, m times. This gives an extra contribution to the energy:

$$\sim T (2\pi m R)$$
 , $m \in \mathbb{Z}$, $T = \frac{1}{2\pi \ell_s^2}$

The spectrum of KK masses now becomes

$$M^{2} = \frac{n^{2}}{R^{2}} + (2\pi TR)^{2}m^{2} = \frac{n^{2}}{R^{2}} + \ell_{s}^{4}R^{2}m^{2} \quad , \quad m, n \in \mathbb{Z}$$

• The spectrum of stringy KK states is invariant under T-duality

$$m \leftrightarrow n$$
 , $R \leftrightarrow \frac{\ell_s^2}{R}$

There is no circle with $R < \ell_s$ in string theory!

Beyond the Standard Model,

LHC cross-sections for KK-gravitons

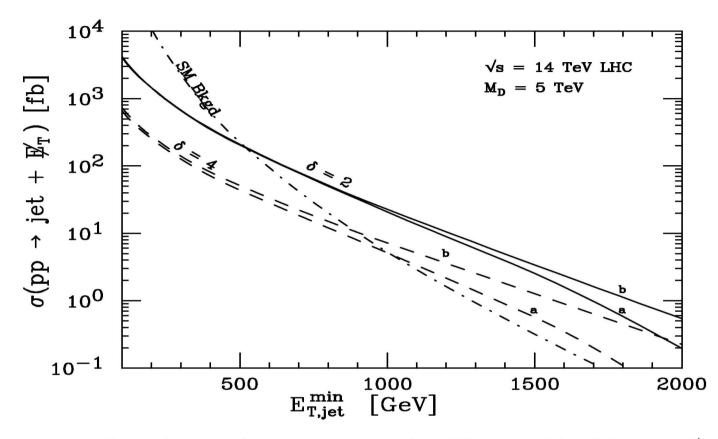


Figure 3: The total jet + nothing cross-section at the LHC integrated for all $E_{T,jet} > E_{T,jet}^{\min}$ with the requirement that $|\eta_{jet}| < 3.0$. The Standard Model background is the dash-dotted line, and the signal is plotted as solid and dashed lines for fixed $M_D = 5$ TeV with $\delta = 2$ and 4 extra dimensions. The **a** (**b**) lines are constructed by integrating the cross-section over $\hat{s} < M_D^2$ (all \hat{s}).

From Giudice, Rattazzi and Wells [arXiv:hep-ph/9811291]

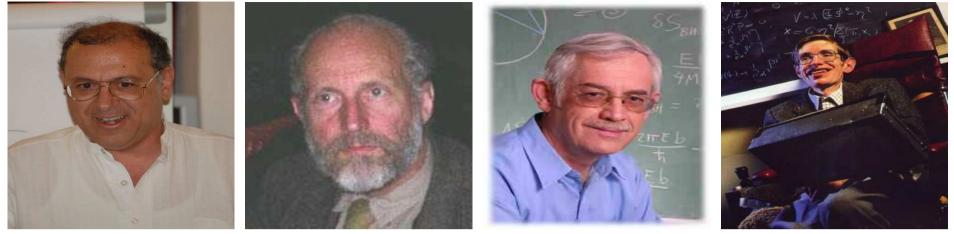
RETURN

Black holes and the information paradox

♠ SURGEON'S WARNING: The following descriptions are very qualitative and gloss over several important details. They are meant to convey the spirit of the current progress in understanding the black hole paradoxes in string theory



• General Relativity predicts black hole solutions. They are sinks of energy. They are surrounded by a horizon. Classically they are the ultimate vacuum cleaners. • Black holes follow the laws of thermodynamics!!! Christodoulou, Carter, Bekenstein, Hawking, 1970-72



- The simplest black hole solution (found by Schwarzschild) is characterized only by its mass M.
- We may define the Hawking temperature and the Bekenstein-Hawking entropy as :

$$T_{H} \equiv \frac{\hbar c^{3}}{8\pi k} G M$$

$$S_{B} \equiv 4\pi \frac{G}{\hbar c} M^{2} = \frac{1}{4} \frac{\text{Area of the horizor}}{\ell_{P}^{2}}$$

Beyond the Standard Model,

Black hole thermodynamics

O-th law: gravitational equilibrium = constant temperature

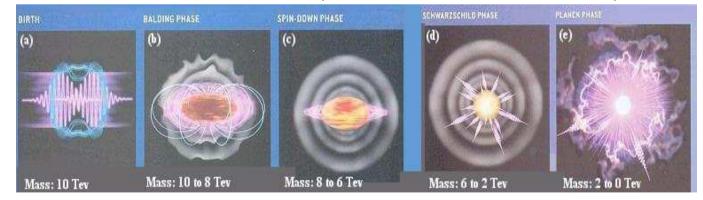
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1st law: \Delta E = T \Delta S + WORK DONE
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2nd law: $\Delta S \geq 0$

3rd law: No finite physical process can bring T = 0.

• The presence of such laws was a mystery

• In 1974 Hawking showed that if we treat matter around a black hole quantum mechanically (but gravity classically), the black hole evaporates emitting particles with a black-body spectrum at temperature T_H (the Hawking temperature)



A simulation of black-hole evaporation

Where are the microstates?

• In quantum statistical mechanics entropy is a measure of the possible different mi-

crostates available to the macroscopic system, (N).

 $S \sim \log[N]$

• What are the microstates that give rise to the Bekenstein-Hawking entropy?

• All reasonable arguments give:

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Entropy \sim volume
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and not \sim surface as in the black-hole case.

• What is the fundamental microscopic explanation of black-hole thermodynamics?

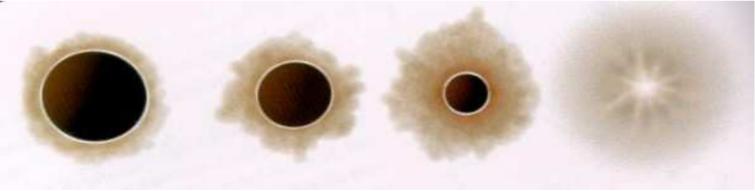
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Beyond the Standard Model,
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The information paradox

• According to quantum mechanics information is conserved: (pure states evolve to pure states).

But....

• A black hole that is created by matter+information (a pure initial state), radiates à la Hawking thermal radiation (that does not carry information), and evaporates leaving nothing behind.



Where did the original information go?

Interlude

- Hawking in 1974 conjectured that the information is lost permanently and therefore quantum mechanics must be modified in the presence of (strong) gravity.
- Last year he accepted defeat by embracing the solution given by the holographic description of string theory and paid his lost bet to John Preskill



Some string theory answers, I

• We may theoretically construct microscopic black-holes from (many) D-brane bound states. Strominger+Vafa, 1996

• When the string coupling constant is small $g_s \ll 1$, these bound states look like heavy composite particles without a horizon.

• In this case we can compute the possible microscopic quantum states and the answer agrees with the (gravitational) Bekenstein-Hawking entropy

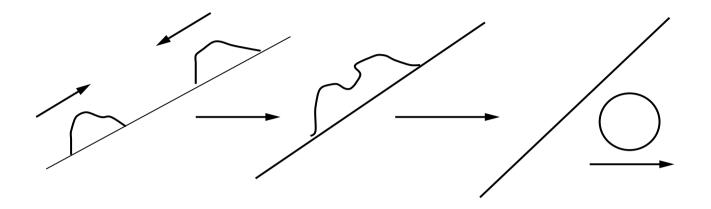
• If we now extrapolate to $g_s >> 1$, the composite particle becomes a heavy black hole with a macroscopic horizon.

• Do we trust our calculations when $g_s >> 1$? Yes! (in special cases that are "protected" by supersymmetry



Some string theory answers, II

• We can also microscopically produce the Hawking radiation

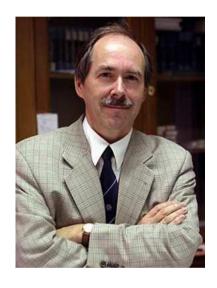


• Open string degrees of freedom describe the fluctuations of D-branes and therefore those of their bound states. When such open string scatter on the surface of the bound-state they may combine to form a closed string and leave the bound state. This process can be modeled and computed from first principles n string theory (in some interesting limits).

- This detailed microscopic string theory calculation agrees with the semiclassical Hawking result in their common area of validity.
- This gives us confidence that this is the correct picture of black-hole microstates (at least for special black holes)!
- It also suggests that information is not lost. Beyond the Standard Model,

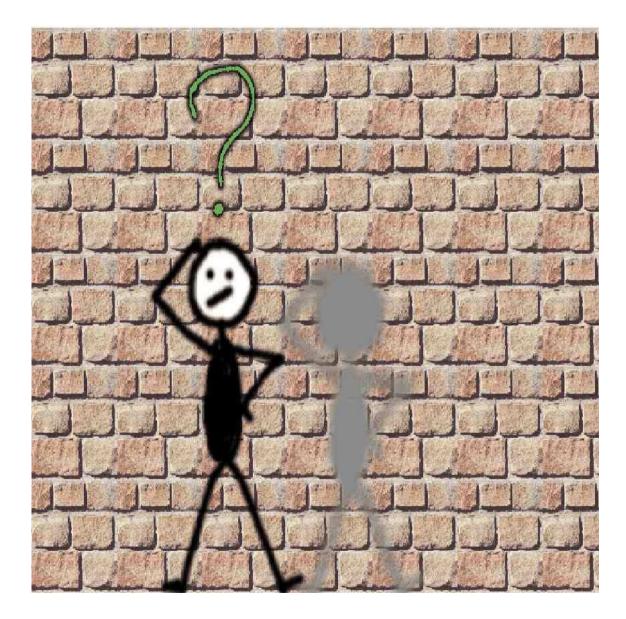
Gravity and Holography

- In standard dynamical systems entropy is proportional to the volume.
- In black hole systems it is proportional to the (horizon) area
- This suggests that the gravitational degrees of freedom are much less in number that what we thought (based on QFT).
- The surface degrees of freedom seem to capture all the information about the volume they surround. (holographic property)



• 't Hooft (1992) : The holographic property is a general property of any consistent theory of quantum gravity.

This property reminds us of "Plato's cave"



Holographic gauge theory/string theory correspondence

- Recently concrete examples have been found where the holographic correspondence can be understood.
- A gauge theory living on the boundary of a space-time corresponds holographically to the string theory that lives in the bulk of the space-time. *Maldacena*, 1997
- This opens the door for a deeper understanding of the puzzles of quantum gravity using gauge theory dynamics.
- It is also suggests that information is not lost from black-holes as the dual description in terms of the gauge theory is explicitly unitary.



• Recently holographic techniques start making an impact as a tool to understand strong coupling dynamics in QCD both zero temperature, as well as for the physics of the quark gluon plasma.

Beyond the Standard Model,

- Introductory general relativity: http://www.phys.uu.nl/~thooft/lectures/genrel.pdf
- Black holes: [arXiv:gr-qc/9707012]
- Introduction to black-hole thermodynamics: http://www.glue.umd.edu/~tajac/BHTlectures/lectures.ps

• Introductory descriptions on the counting of black-hole microstates and the holographic (bulk-boundary) correspondence can be found in the following string theory books:

- C. Johnson, "D branes"
- ► K+M. Becker, John Schwarz, "String theory and M-theory
- E. Kiritsis, "String theory in a nutshell

RETURN

Beyond the Standard Model,



- Title page 1 minutes
- Quote 1 minutes
- Preview 1 minutes
- Preview:Higgs 2 minutes
- Preview:Supersymmetry 5 minutes
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- The purpose of these lectures 11 minutes
- Suggested reading 12 minutes
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- High Energy Units 13 minutes

- The Standard Model: principles 16 minutes
- Standard Model: Open Problems 18 minutes
- Standard Model: Open Problems II 20 minutes
- SM patterns and parameters 22 minutes
- The pattern of masses 24 minutes
- How parameters affect us 26 minutes
- Renormalization: Integrating out high-energy d.o.f 30 minutes
- The effective field theory 32 minutes
- Effective couplings: the Fermi Theory paradigm 36 minutes
- Irreversibility 39 minutes
- Running Couplings 42 minutes
- Renormalization Summary 46 minutes
- End of lecture 1

- The hierarchy problem:Introduction 49 minutes
- Fermion masses 54 minutes
- Gauge boson masses 57 minutes
- The Higgs mass term 60 minutes
- The hierarchy problem 63 minutes
- Avoiding the hierarchy problem 64 minutes
- Technicolor 69 minutes
- Supersymmetry 72 minutes
- Supersymmetry, Vol II 74 minutes
- The supersymmetric multiplets (representations) 76 minutes
- The Supersymmetric Standard Model 80 minutes
- The quantum numbers 83 minutes
- The supersymmetric interactions 90 minutes
- End of lecture 2
- R-parity 93 minutes
- Missing Energy 94 minutes
- Missing Energy (Atlas simulation) 95 minutes
- A link to dark matter 98 minutes

- Supersymmetry Breaking 103 minutes
- Supersymmetry Breaking, II 107 minutes
- The soft supersymmetry breaking terms 114 minutes
- Spontaneous Supersymmetry Breaking 120 minutes
- Grand Unification: The idea 125 minutes
- SU(5): the matter 128 minutes
- Proton decay 131 minutes
- Coupling Unification 135 minutes
- End of lecture 3
- The gravitational coupling 137 minutes
- Gravity versus other interactions 139 minutes
- The running of all couplings 141 minutes
- Gravity and the SM 143 minutes
- Gravity at short distances? 146 minutes
- Gravity and String Theory 149 minutes

- What is String Theory? 151 minutes
- String Theory, Vol II 153 minutes
- Extra space-time dimensions 156 minutes
- "Small" compact dimensions 159 minutes
- Kaluza-Klein states 164 minutes
- Branes and large extra dimensions 174 minutes
- Black holes at colliders? 178 minutes
- Conclusions 180 minutes
- End of lecture 4

Appendices

- The Standard Model: ingredients
- Standard Model: the quarks
- Standard Model: the leptons
- Standard Model: the Higgs
- How parameters affect us: some answers
- Other parameters in the SM
- Renormalization: the coupling constants
- The compact Newton's law
- mAMSB
- mGMSB
- Higgs event
- First SUSY event
- Proton Decay Channels
- Effective Field Theory: Wilson's View
- Renormalization: the old view
- renormalized couplings: an example

- A simple example of a softly-broken supersymmetric theory
- SSB: Heavy gravitino mass
- SSB: Light gravitino mass
- Proton Decay Experiments
- Proton decay channels
- Hypercharge normalization
- String Theory, Vol III
- String perturbation theory
- Kaluza-Klein states in string theory
- LHC cross-sections for Kaluza-Klein graviton production
- Black holes and the information paradox
- Black hole thermodynamics
- Where are the microstates?
- The information paradox
- Interlude
- Some string theory answers, I
- Some string theory answers, II
- Gravity and Holography
- Holographic gauge theory/string theory correspondence
- Further reading

Beyond the Standard Model,