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# *String Physics at LHC*

Elias Kiritsis

Ecole Polytechnique  
and  
University of Crete

# Bibliography: Reviews

- [arXiv:hep-th/0310001]

Review on orientifold/brane model building (to appear in Physics Reports)

- The effective theory of LSOM

By Coriano, Irges and Kiritsis (to appear this week)

# Plan of the talk

- Introduction: the goals
- Orientifolds, some rough characteristics
- Low scale Orientifold models
- What is there to be done?

# Plan of the presentation

- Title page 1 minutes
- Bibliography 2 minutes
- Plan 3 minutes
- Introduction 5 minutes
- Orientifolds 7 minutes
- Compact Orientifolds 12 minutes
- Some goals 15 minutes
- The gauge groups of Orientifold vacua 17 minutes
- The particle Zoo in Orientifolds:D-branes 21 minutes
- The particle Zoo in Orientifolds: Bulk 23 minutes
- LOW STRING SCALE VACUA 29 minutes
- Important issues in mLSOM 31 minutes
- Neutrino Masses 34 minutes
- The SM gauge group 35 minutes

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- The fate of anomalous  $U(1)$ 's 2 minutes
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- Anomalous  $U(1)$  masses 3 minutes
- $Z$ - $Z'$  mixing 3 minutes
- The Higgs Sector 2 minutes
- Axions and Axi-Higgs 3 minutes
- The bulk  $U(1)'$  3 minutes
- SURGEON'S WARNING !!!!! 2 minutes

# Introduction

- String theory owes its popularity to its treatment of quantum gravity.
- It can accommodate the basic ideas and contexts of the SM interactions (gauge theories , chirality, supersymmetry)
- It is very difficult to search and build detailed models where the spectrum and interactions are carefully selected. This is because, the building tool , CFT is poorly understood in the general case, and the procedure cannot be easily made algorithmic.
- A fruitful arena in the past ten years, was open string theory, and orientifolds
- Open string theory: natural separation between the “SM sector” (branes) and the gravity sector (bulk closed strings).

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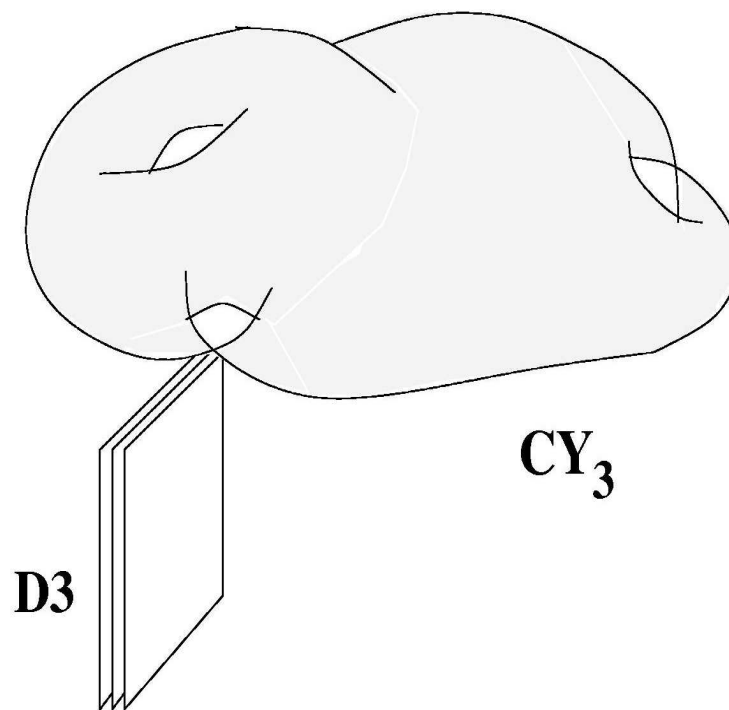
Closed strings cannot accommodate the SM perturbatively.

Brane model building can be made “modular”. The modules are local collections of stacks of branes.

- Orientifolds lead to calculable vacua.

# Orientifolds

BCFT describes a new class of vacua of string theory, which on top of a partly compactified space-time, contain also D-branes that stretch along the four Minkowski directions and may or may not wrap some internal dimensions.



Since D-branes carry gauge bosons as well as matter fermions they contribute to the gauge group and matter content of the particular ground-state.



# Compact Orientifolds

The compactification estimates for orientifolds. For gravity :

$$S_{10} \sim \frac{M_s^8}{g_s^2} \int d^{10}x R_{(10)} \rightarrow \frac{V_6 M_s^8}{g_s^2} \int d^4x R_{(4)}$$

Consider however a (p+3)-brane wrapping a compact cycle of volume  $V_{||}$ . Then

$$\frac{M_s^p}{4g_s} \int d^{p+3}x \text{Tr}(F_{\mu\nu})^2 \rightarrow \frac{V_{||} M_s^p}{4g_s} \int d^4x \text{Tr}(F_{\mu\nu}^2)$$

We may then read: ( $V_6 = V_{||} V_{\perp}$ )

$$M_P^2 = \frac{V_6 M_s^8}{g_s^2}, \quad \frac{1}{g_U^2} = \frac{V_{||} M_s^p}{g_s}$$

$$\Rightarrow \frac{M_s^2}{M_P^2} = \frac{g_s}{V_{\perp} M_s^{6-p}} g_U^2, \quad \text{with} \quad g_U \sim 0.2$$

For large internal volume  $V_{\perp} M_s^{6-p} \gg 1$

$$M_s \ll M_P$$

Continued...

Therefore the string scale can be as low (or as high) as we like.

◇ If  $M_s \sim M_P$  we need low energy SUSY (or split susy, but fine tuning).

♠ If  $M_s \sim \text{TeV}$  there is no need for SUSY (but we need a mechanism to generate large dimensions). Since string theory is always supersymmetric in the UV, SUSY is broken at  $M_s$  in this case.

In this talk I will review:

♡ Low scale Orientifold vacua: (LSOM) with ( $M_s \sim 1 - 100 \text{ TeV}$ )

*Antoniadis+Kiritsis+Tomaras*

*Antoniadis+Kiritsis+Rizos+Tomaras*

♠ There are also orientifolds realizing **split susy**. I might not have time to review them.

*Antoniadis+Dimopoulos*

## Some goals

There are several open problems in this direction that are interlinked.

They stem from the fact that “string model building” is notoriously difficult. There are few quasi-realistic models, and none that is fully realistic.

There are two axes of necessary effort.

- **Construct promising string vacua.** A guide is needed to tell from rough data and structure (gauge group, charges, selection rules) and BEFORE calculating the full tree level potential and finding minima, masses etc., which models have reasonable chance of being realistic.

*ex: Anastasopoulos, Dijkstra, Kiritsis, Schellekens*

- **Analyze/parametrize the low energy effective field theory (LEEFT).**

(a) This gives a rough idea whether such vacua have a chance of being realistic (useful for string model search)

(b) This defines the parameters and observables for searches, and constrains from existing experimental results.

# The gauge groups of Orientifold vacua

- They are the classical groups:  $U(N)$  from a stack of D-branes,  $Sp(N)$  or  $SO(N)$  from D-branes reflected from an O-plane. No exceptional groups possible perturbatively.
- Representations: "bi-fundamentals" = all reps that can be build from two "fundamental indices" = endpoints of the string. They are bi-fundamentals  $(n, n)$  or  $(n, \bar{n})$ , two index symmetric/antisymmetric.
- Unified vs "splinter groups":
  - (a) Unification is desired in field theory model building, because it lowers the number of unrelated parameters.
  - (b) This is not a priori true in string theory. Parameters are vevs, fixed by the potential.Therefore in ST: we might as well go for SM gauge group  $\times$  hidden group.

Some unified groups are not possible:

- $E_6$  cannot appear
- $SO(10)$  cannot have a spinor.
- $SU(5)$  is possible, (we have found a susy string model with the correct chiral spectrum)

Therefore we go for small product groups.

- $SU(3)_c$  must be embedded minimally in  $U(3)$  or higher ( $U(4)$  .....
- $SU(2)$  could be  $Sp(2)$  or  $U(2)$  (or higher)
- $U(1)_Y$  can be any linear combination of  $U(1)$ 's or other (broken) non-abelian generators.

Search for stringy patterns:

$$U(3) \times (U(2) \text{ or } Sp(2)) \times G_1 \times G_2$$

*Anastasopoulos, Dijkstra, Kiritsis, Schellekens*

**Question:** Which  $G_1 \times G_2$  have in principle the potential of giving realistic models (including hierarchies of masses and mixings)?

# The particle Zoo in Orientifolds

## D-brane sector

Except the SM particles :

- **Extra massive U(1) which are "anomalous"**. Their masses can be from  $M_s$  to  $\ll M_s$ . They are unavoidable.
- **Higgs doublets** Can be 2, 4, 6, ..... depending on the model.
- **Superpartners**. Masses depended on susy breaking and  $M_s$ . Very model dependent
- **Hidden matter and interactions**. Although there are string examples with none, they are useful for breaking supersymmetry and potentially confining fractional charges.
- **Brane KK modes**. When  $M_s \sim M_P$  they have masses of order  $M_s$  relevant only for precision threshold calculations. When  $M_s \sim TeV$ , they can be produced in LHC, the lightness of neutrinos can be associated with large dimensions and there is non-trivial mixing with them.  
*Antoniadis+Kiritsis+Rizos+Tomaras*  
*Matias+Burgess*
- **Brane stringy modes**.  $M_s \sim M_P$ , relevant for thresholds.  $M_s \sim TeV$  could be produced, give measurable tree and loop corrections to processes.

# The bulk sector (closed strings)

- 4D Gravitons
- Other “low lying” vectors, scalars and fermions. They will be heavy if closed-string moduli are stabilized appropriately. Perturbative Brane matter is uncharged under bulk vectors (RR) except for KK+Winding states.
- Bulk KK states. Same comments as on branes: can be produced when  $M_s$  very low.
- Bulk stringy states. Same comments as on branes: can be produced when  $M_s$  very low.

# Low string scale vacua

Important issues in such vacua:

- For stringers: **find them explicitly**. They need very particular hypercharge embeddings and two (very) large extra dimensions.
- **Define benchmark LEEFTs** that parameterize effectively the low energy physics.

There are two options here:

- ♣ Since susy breaks at  $M_s$ , in a class of models, the anomalous (massive) U(1)s will be substantially lighter than standard superpartners.

This motivates the **simplest “benchmark” LEEFT**: **mLSOM<sub>a</sub>**

It is characterized by:

- (1) **The particle content**: SM particles, right-handed neutrinos, 2 Higgses, 3 anomalous U(1)'s and their associated bulk axions, and the light KK modes, coming from the two large dimensions which play an important role in neutrino mixing.
- (2) An index taking four values and running over **different charge structures** of the SM particles under the extra U(1) symmetries.



- The explicit  $m\text{LSOM}_a$  effective action is being developed

*Coriano+Irges+Kiritsis to appear*

- Some interesting effects have been partly considered

Constraints on  $g - 2$ :

*Anastasopoulos+Kiritsis*

Constraints on  $\rho$ -parameter :

*Ghilencea+Irges+Ibanez+Quevedo*

**But the most interesting work both on constraints and new effects at LHC remains to be done** (more later)

♠ The second “benchmark” LEEFT:  $s\text{LSOM}_a$ . Here the superpartners are kept, as well as the soft susy breaking terms.

This is an extended version of the MSSM, including 3 extra anomalous U(1) multiplets plus KK states.

**Writing and analysing this LEEFT is an open problem.**

There are some theoretical issues that do not occur in MSSM and need some clarification.

They are associated with

- The supersymmetric couplings of the anomalous U(1) multiplets in the globally supersymmetric limit
- The analogue of soft terms for anomalous U(1)’s (usual susy analysis does not apply here).

# Important issues in mLSOM

$$(M_s \sim 1 - 100 TeV)$$

- Here, two out of six dimensions have sub-millimeter size

♣ Since the “unification” scale is low, GOOD lepton number and baryon number symmetries are CRUCIAL.

Lepton and baryon number will be gauged (anomalous) symmetries

♠ We utilize the existence of large dimensions to produce naturally light neutrino masses.

♡ Families can be generated from multiple brane intersections

# Neutrino Masses

Consider the left-handed neutrino  $\nu_L$  being a fluctuation of a 3-brane. Consider also a right-handed neutrino  $\nu_R$  being a fluctuation of a  $(p+3)$ -brane wrapping a  $p$ -dimensional internal large volume  $V_p$ .

*Dienes+Dudas+Gherghetta*

We have the following action

$$S \sim \int d^{p+4}x \left( \bar{\nu}_R \not{\partial} \nu_R \right) + g \int d^4x \left( \bar{\nu}_R H \nu_L \right)$$

which upon compactification and symmetry breaking becomes

$$S \rightarrow \int d^3x \left[ V_p \left( \bar{\nu}_R \not{\partial} \nu_R \right) + m \bar{\nu}_R \nu_L \right]$$

$m = g v \sim M_Z$  Normalizing kinetic terms by  $\nu_R \rightarrow \nu_R / \sqrt{V_p}$  we obtain

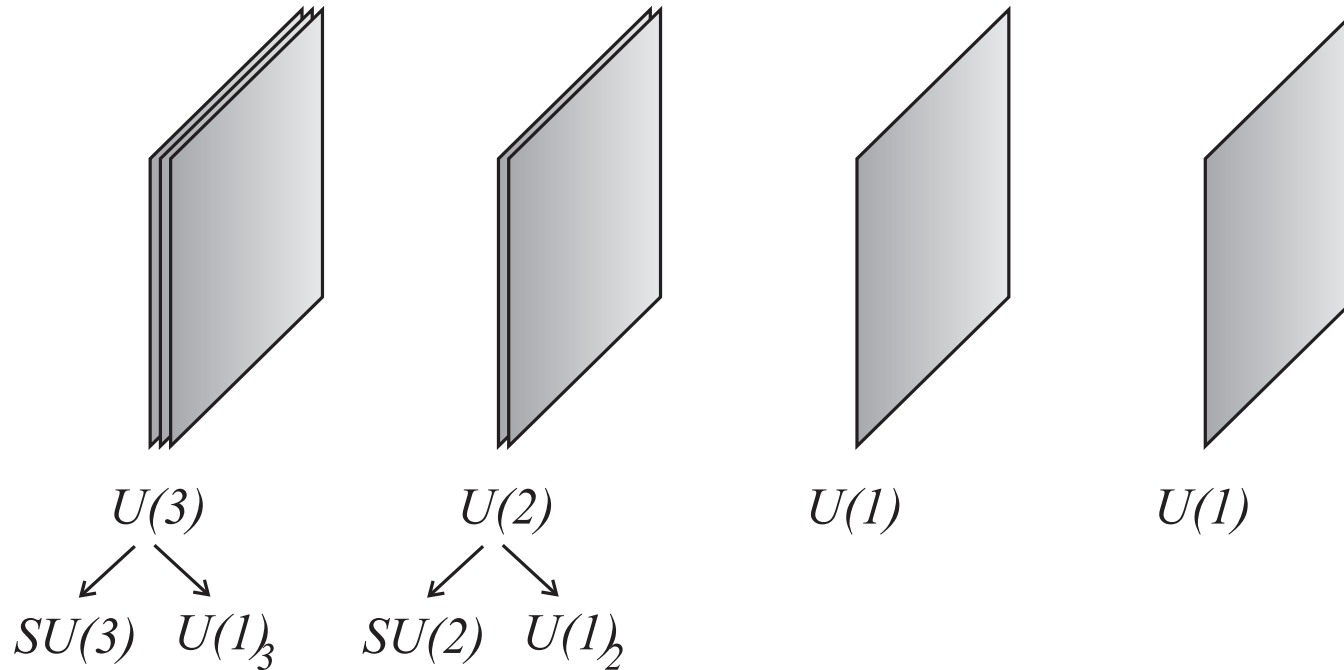
$$S \sim \int d^3x \left[ \bar{\nu}_R \not{\partial} \nu_R + \frac{m}{\sqrt{V_p}} \bar{\nu}_R \nu_L \right]$$

$$m_\nu \sim \frac{M_Z}{\sqrt{V_p}} \sim M_Z \left( \frac{M_s}{M_P} \right) \sqrt{g_s} g_U$$

This gives  $m_\nu \sim 10^{-6} - 10^{-3}$  eV.

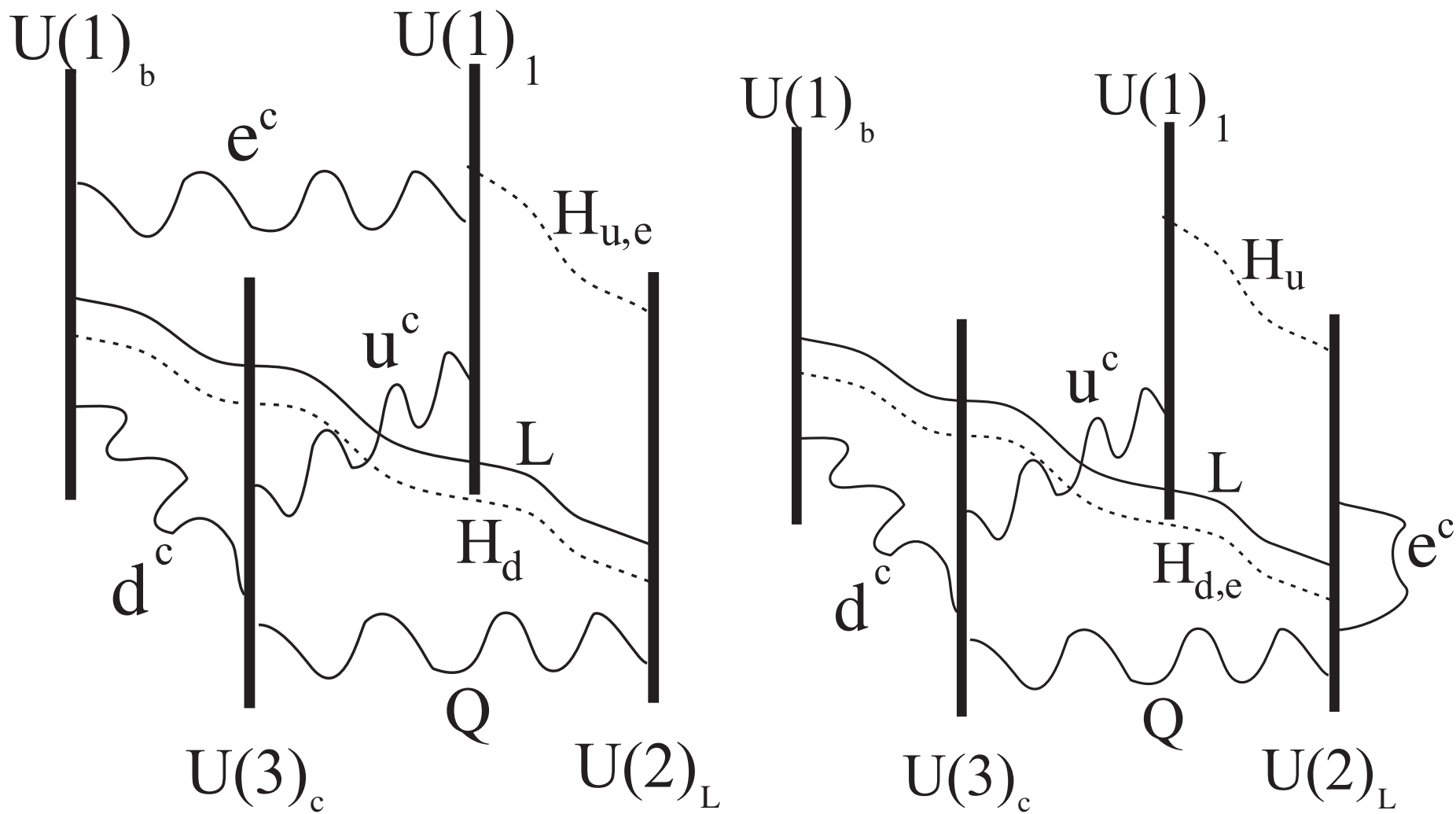
# The SM gauge group

For a low string scale the minimal choice is  $U(3) \times U(2) \times U(1) \times U(1)'$ .



## Models $mLSOM_A$ and $mLSOM_{A'}$

SM particle	$U(1)_3$	$U(1)_2$	$U(1)$	$U(1)'$
$Q(\mathbf{3}, \mathbf{2}, +\frac{1}{6})$	+1	-1	0	0
$u^c(\bar{\mathbf{3}}, \mathbf{1}, -\frac{2}{3})$	-1	0	-1	0
$d^c(\bar{\mathbf{3}}, \mathbf{1}, +\frac{1}{3})$	-1	0	0	-1
$L(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$	0	+1	0	-1
$e^c(\mathbf{1}, \mathbf{1}, +1)$	0	0(2)	1(0)	1(0)
$H_u(\mathbf{1}, \mathbf{2}, +\frac{1}{2})$	0	1	1	0
$H_d(\mathbf{1}, \mathbf{2}, +\frac{1}{2})$	0	-1	0	-1
$\nu^c(\mathbf{1}, \mathbf{1}, 0)$	0	0	0	$\pm 2$



## Models $mLSOM_A$ and $mLSOM_{A'}$ : continued

Hypercharge:

$$Y = -\frac{1}{3}Q_3 - \frac{1}{2}Q_2 + Q_1$$

Global symmetries:

$$\text{Baryon Number } B = \frac{1}{3}Q_3$$

$$\text{Lepton Number } L = \frac{1}{2}(Q_3 + Q_2 - Q_1 - Q'_1)$$

$$\text{Peccei – Quinn } PQ = -\frac{1}{2}(Q_3 - Q_2 - 3Q_1 - 3Q'_1)$$

All  $U(1)$ 's except  $Y$  are “anomalous” and therefore massive. All except  $PQ$  remain as good global symmetries.

Gauge couplings and string scale:  $g_2(M_s)$  and  $g_3(M_s)$  are determined by data. By varying  $g_1(M_s)$  we can determine  $M_s$  from  $\alpha_Y(M_Z)$ :

$$V_1 = V_2 \quad , \quad M_s \simeq 800 \text{ GeV}$$

$$3V_1 = 2V_2 + 2V_3 \rightarrow M_s \simeq 1.5 \text{ TeV}$$

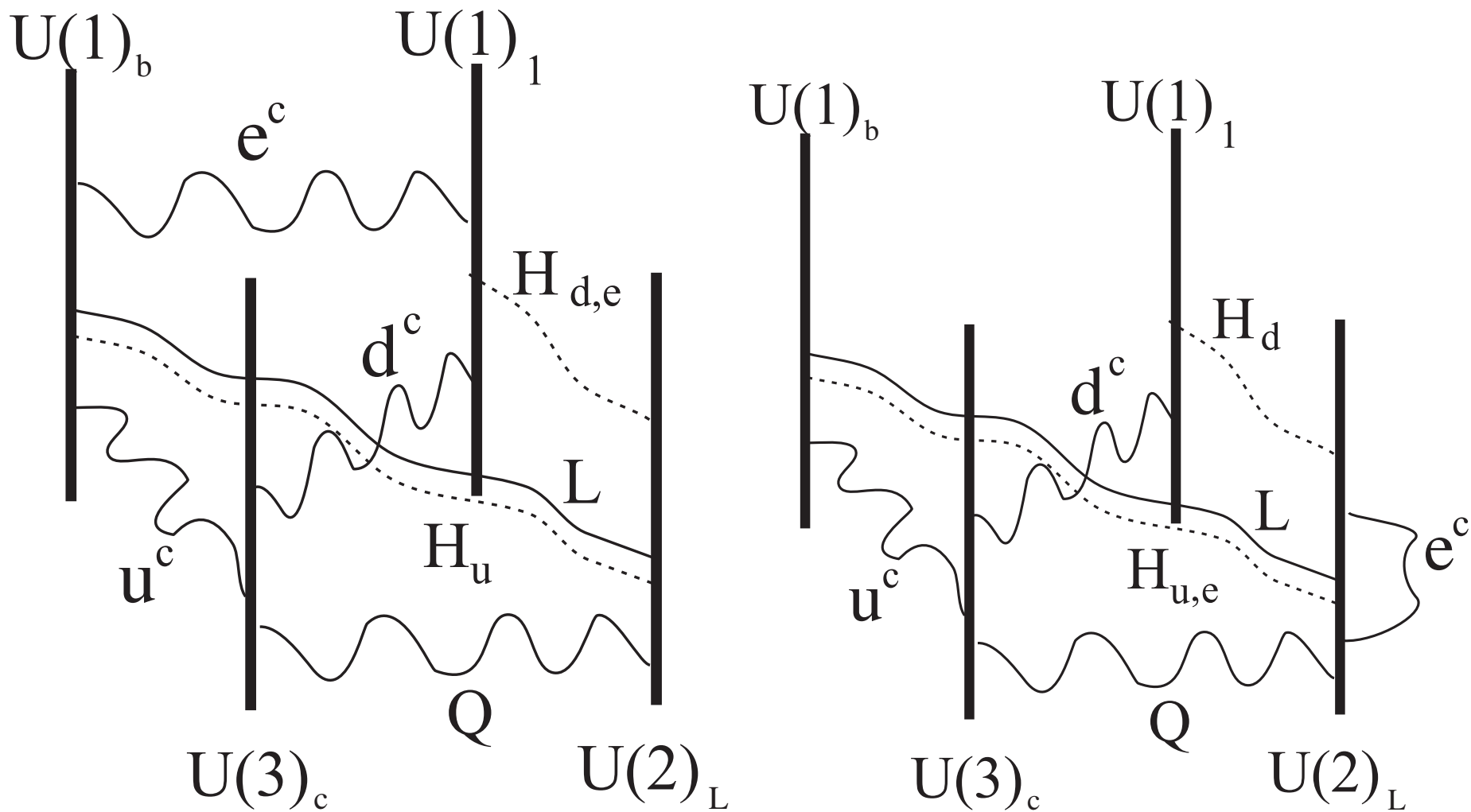
$$2V_1 = V_2 + V_3 \rightarrow M_s \simeq 56 \text{ TeV}$$

Remember: at  $M_s$ ,  $1/g_i^2 = V_i/g_s$ .



## Models $m\text{LSOM}_B$ and $m\text{LSOM}_{B'}$

SM particle	$U(1)_3$	$U(1)_2$	$U(1)$	$U(1)'$
$Q(\mathbf{3}, \mathbf{2}, +\frac{1}{6})$	+1	-1	0	0
$u^c(\bar{\mathbf{3}}, \mathbf{1}, -\frac{2}{3})$	-1	0	0	1
$d^c(\bar{\mathbf{3}}, \mathbf{1}, +\frac{1}{3})$	-1	0	1	0
$L(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$	0	+1	0	-1
$e^c(\mathbf{1}, \mathbf{1}, +1)$	0	0(2)	1(0)	1(0)
$H_u(\mathbf{1}, \mathbf{2}, +\frac{1}{2})$	0	-1	0	-1
$H_d(\mathbf{1}, \mathbf{2}, +\frac{1}{2})$	0	1	1	0
$\nu^c(\mathbf{1}, \mathbf{1}, 0)$	0	0	0	$\pm 2$



Hypercharge:

$$Y = \frac{2}{3}Q_3 - \frac{1}{2}Q_2 + Q_1$$

Gauge couplings and string scale:

$$V_1 = V_3 \quad , \quad M_s \sim 7 \text{ TeV}$$

$$3V_1 = V_2 + V_3 \quad , \quad M_s \sim 3.5 \text{ TeV}$$

Global symmetries:

Baryon Number  $B = \frac{1}{3}Q_3$

Lepton Number  $L = -\frac{1}{2}(Q_3 - Q_2 + Q_1 + Q'_1)$

Peccei – Quinn  $PQ = \frac{1}{2}(-Q_3 + 3Q_2 + Q_1 + Q'_1)$

All U(1)'s except  $Y$  are “anomalous” and therefore massive. All except PQ remain as good global symmetries.

# Parameters of mLSOM

Apart from the usual SM parameters we have

- Potential new parameters in the Higgs potential (maximum 5 more are allowed by the gauge symmetry but are seriously constrained)
- The UV mass matrix of the U(1)s:  $Y$  and 3 anomalous ones.  $Y$  corresponds to a zero eigenvalue and a known eigenvector. We are left with three non-zero eigenvalues and three (real) mixing angles.
- The radii of the large and small compact dimensions
- In the neutrino sector there are two possibilities:
  - (a) Mixing with one flavor of bulk neutrino, and its KK states (fewer parameters than the SM)
  - (b) Mixing with three flavors of bulk neutrinos (as in the usual extension of SM)

# New Physics of mLSOM

- The new particles (beyond the SM) here are:

(a) The 3 massive anomalous  $U(1)$ s  $\rightarrow$   $Z$ 's

(b) The extra particles coming from the Higgs sector plus bulk axions. They are the same as in the MSSM, but without the usual supersymmetric constraints on the Higgs potential.

(c) KK modes of particles sensitive to the large dimensions (R-neutrinos, gravitons,  $U(1)'$  gauge bosons)

Several observables to be computed and ...

(1) Parameters constrained by existing data

(2) Predicting possible signals for LHC

# Z' observables

- There are the standard ones: Drell-Yan cross sections and FB asymmetry. No news here, the data are the same as in other models
- Because the Higgses are charged under the Z's, there is mixing between the  $Z^0$  and photon, and  $Z'_i$  of order  $\mathcal{O}(M_Z^2/M_s^2) \sim 10^{-3} - 10^{-4}$ .

(1) Constraints from LEP on couplings of  $Z^0$  and  $\rho$ -parameter

(2) New interactions for the  $\gamma$ ,  $Z^0$ , and  $Z'_i$  because of the existence of the anomaly (triangle diagram)

In particular there are non-abelian-like three-point vertices with a suppressed coupling  $\mathcal{O}(M_Z^2/M_s^2)$

- Could provide new channels for  $Z^0$  decay (to be computed)
- Gives new channels for observing  $Z'$  by decaying to  $\gamma - \gamma$  or  $Z^0 - \gamma$  final states (to be computed)

## Other experimental implications

- The neutrinos come from large dimensions. Their mixing with KK descendants with

$$\frac{1}{R} \simeq 10 - 100 \frac{M_s}{M_P} \sim 10^{-5} - 10^{-2} \text{ eV}$$

might be observable. This has been partly analyzed , but the main work remain still undone.

- The KK states of the bulk fields (graviton et al.) are those of two large extra dimensions with all the known implications for LHC.
- One of the  $Z'$  is unusual. This is the one mainly coming from the  $U(1)'$ . Its coupling is almost of gravitational strength

$$g'_1 \sim \frac{M_s}{M_P} \sim 10^{-15}$$

Its mass must be larger than 50 MeV, to avoid astrophysical constraints. It has graviton-like KK states.

# mLSOM summary

- mLSOM effective theories parameterize a novel and phenomenologically interesting class of orientifold vacua.
- Analysis of several issues is important since it will already constrain parameters and will compute potential processes for LHC
- A novel feature is the presence of three massive abelian gauge bosons, with string scale masses which mix with  $\gamma$  and  $Z^0$ , and have effective non-abelian three-point couplings.
- The Higgs sector is MSSM like but a bit more general.
- Neutrino physics is interesting and not fully analyzed
- They have the usual tower of KK states expected in ADD.



# Gauge couplings

The hypercharge gauge coupling is given by

$$\frac{1}{g_Y^2} = \frac{6k_3^2}{g_3^2} + \frac{4k_2^2}{g_2^2} + \frac{2k_1^2}{g_1^2} + \frac{2k_1'^2}{g_1'^2} \quad , \quad \frac{1}{g_i^2} = \frac{V_i}{g_s}$$

$k_1'$  must be zero because  $V_1' \gg 1$  so that  $g_1' \ll 1$ .

We may now determine  $k_i$  and the possible charge assignments by asking:

- The hypercharge values of the SM particles are correct (This is anomaly freedom up to an overall scale).
- Lepton number is one of the gauge U(1) symmetries
- That the gauge couplings fit the data with a low  $M_s$ .

This selects two models  $A, B$ , each coming in two slightly different versions ( $A', B'$ ).

We will call them **minimal Low Scale Orientifolds** (mLSO). We will label them as  $mLSO_{A,A',B,B'}$  for simplicity.

# Quark and Lepton masses

For the 3rd generation the structure of masses is:

$$M_{\text{model}} \mathbf{A}' = \lambda_u Q u^c H_u + \lambda_d Q d^c H_d^\dagger + \lambda_e L e^c H_d^\dagger + \lambda_\nu L H_d \nu_R$$

(tree level, trivial moduli dependence and a particular brane configuration  $D_5$ - $D_5$ - $D_5$ )

$$\lambda_u = \lambda_e = \sqrt{2}g_2, \quad \lambda_d = \sqrt{2}g_s, \quad \lambda_\nu = \sqrt{2}g'_1 \ll 1.$$

Fitting  $m_b \simeq 4$  GeV we get

$$m_t \simeq 162 \text{ GeV} \quad (\text{not so bad!})$$

$$\frac{m_b}{m_\tau} = \frac{\sqrt{g_s}}{g_2} \simeq \frac{g_3}{g_2} \Rightarrow m_\tau(M_s) = 1.75 \text{ GeV}$$

This is not very far from the measured value  $m_\tau(M_Z) = 1.46$  GeV and in fact running gets it closer.

The neutrino masses are in the range  $10^{-5} = 10^{-3}$  eV.

For the model A

$$M_{\text{model A}} = \lambda_u Q u^c H_u + \lambda_d Q d^c H_d^\dagger + \lambda_e L e^c H_u^\dagger + \lambda_\nu L H_d \nu_R$$

Again the top comes out right.

But  $m_\tau \sim m_t$  which is unrealistic. Several ways out:

- (a) to have  $\lambda_e = 0$  at tree level so that the  $\tau$  mass is generated from higher order terms.
- (b) Non-trivial moduli alter the values of Yukawa's

# The fate of anomalous U(1)s

◇ All U(1)s except  $Y$  have anomalies: mixed abelian-non-abelian anomalies with SU(2) and SU(3) and (abelian)<sup>3</sup> anomalies.

♣ These anomalies are cancelled by the GS mechanism.

The gauge boson is now **massive** and the associated gauge symmetry **broken**.

♠ For symmetric values of bulk moduli **the global U(1) symmetry remains intact**.

♥ The global symmetry is broken however beyond perturbation theory by instantons. In the case of Baryon and Lepton number, these are the SU(2) instantons, and such a rate (calculated by 't Hooft) is VERY small. This need not be the case for the PQ symmetry.

To summarize, the remaining global U(1) symmetry remains a good symmetry if the instanton effects are small and the bulk moduli have special values.

# The fate of anomalous U(1)s:continued

♣ Example: A U(1) gauge symmetry that has a mixed triangle anomaly (e.g.  $\zeta = \text{Tr}[QT^aT^a] \neq 0$ ) The one-loop fermionic determinant induces a non-invariance to U(1) gauge transformations

$$A_\mu \rightarrow A_\mu + \partial_\mu \epsilon \quad , \quad \delta L_{1\text{-loop}} = \epsilon \zeta \text{Tr}[G \wedge G]$$

This is cancelled by a non-invariance of the classical (tree level action).

$$\mathcal{L}_{\text{class}} \sim -\frac{1}{4g^2} F_{\mu\nu}^2 + \frac{M^2}{2} (\partial_\mu a + A_\mu)^2 + \zeta a \text{Tr}[G \wedge G]$$

The axion now transforms

$$a \rightarrow a - \epsilon \quad , \quad \mathcal{L}_{\text{class}} \rightarrow \mathcal{L}_{\text{class}} - \zeta \epsilon \text{Tr}[G \wedge G]$$

and the anomaly is **cancelled**.

- The D-term-like potential is of the form

$$V \sim \left( s + \sum_i q_i |\phi_i|^2 \right)^2$$

where  $s$  is a bulk modulus. In SUSY Theories it is the chiral partner of the axion “eaten up” by the anomalous U(1) gauge boson. If  $\langle s \rangle = 0$ , **the global U(1) symmetry remains intact**.

# Anomalous U(1) masses

There are two sources for the masses of anomalous U(1)s:

- The UV mass-term responsible for anomaly cancellation

$$L_{UV} \sim \frac{1}{2} M^2 (\partial_\mu a + A_\mu)^2$$

This is computable only in string theory. It turns out that

$$M \sim g \frac{M_s}{\sqrt{V}}$$

Depending on  $V$  it can be  $\sim M_s$  or  $\ll M_s$  (unlike the heterotic string).

- contributions from spontaneous symmetry breaking. The standard Higgses when they get vevs they break also the U(1) symmetries In total:

$$M \simeq \sqrt{M^2 + g^2 v^2} \simeq \sqrt{M^2 + M_Z^2}$$

In this class of models, such Z's are generic, their low energy couplings fixed by charges and anomalies and only  $M$  depends on UV physics.

## Z-Z' mixing

After the Higgs mechanism, the three mass eigenstates, the photon  $A$ , the  $Z^0$ , and the  $Z'$ -bosons, are specific linear combinations of  $W^3$ ,  $Y$  and  $A^i$  gauge bosons. Inversely

$$\begin{pmatrix} W^3 \\ Y \\ A^i \end{pmatrix} = \begin{pmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{pmatrix} \begin{pmatrix} A_\gamma \\ Z^0 \\ Z' \end{pmatrix}$$

We have

$$c_{11}, c_{12}, c_{21}, c_{22}, c_{33} \sim \mathcal{O}(1) \quad , \quad c_{13}, c_{23}, c_{31}, c_{32} \sim \mathcal{O}\left(\frac{M_Z}{M_s}\right) < 10^{-4}$$

The  $\rho$ -parameter,  $\rho = \frac{M_W^2}{M_Z^2 \sin^2 \theta_W}$ , is no more equal to the standard model value

$$\frac{\Delta\rho}{\rho_0} \sim \frac{M_Z}{M_s} < 6 \times 10^{-4}$$

and there are small modifications of the  $Z^0$  couplings to the fermions.

# The Higgs sector

Although the low energy spectrum is non-supersymmetric, we have a Higgs sector reminiscent of the MSSM.

Here a priori more general terms are allowed.

- If the breaking of supersymmetry is due to internal magnetic fields, then all quartic terms can a priori appear at tree level. This changes the bounds on the lightest Higgses.
- If supersymmetry breaks via the branes sitting at singularities, then the tree-level terms in the potential are the usual supersymmetric D-terms that align the vev's of the Higgses. However, as in the SM, at loop level all terms will be generated.
- The PQ symmetry is broken by the potential. This is important in order to give a mass to the associated PQ axion. The dimension-2 term with this property is the  $\mu$ -term of the MSSM



$$H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix} \quad H_d = \begin{pmatrix} H_d^+ \\ H_d^0 \end{pmatrix}$$

$$V_{PQ}(H_u, H_d) = \sum_{a=u,d} \left( \mu_a^2 H_a^\dagger H_a + \lambda_{aa} (H_a^\dagger H_a)^2 \right) - 2\lambda_{ud} (H_u^\dagger H_u) (H_d^\dagger H_d) + 2\lambda'_{ud} |H_u^T \tau_2 H_d|^2.$$

$$V_{PQb} = B (H_u^\dagger H_d e^{-i \sum_I (q_u^I - q_d^I) \frac{a'_I}{M_I}}) + \lambda_1 (H_u^\dagger H_d e^{-i \sum_I (q_u^I - q_d^I) \frac{a'_I}{M_I}})^2 \\ + \lambda_2 (H_u^\dagger H_u) (H_u^\dagger H_d e^{-i \sum_I (q_u^I - q_d^I) \frac{a'_I}{M_I}}) + \lambda_3 (H_d^\dagger H_d) (H_u^\dagger H_d e^{-i \sum_I (q_u^I - q_d^I) \frac{a'_I}{M_I}}) + c.c.$$

Correspondence with MSSM parameters:

$$\mu_{u,d} \rightarrow \mu_{1,2} \quad , \quad \lambda_{uu} = \lambda_{dd} = -\frac{1}{2}\lambda_{ud} = \frac{1}{8}(g_1^2 + g_2^2) \quad , \quad \lambda'_{ud} = \frac{g_2^2}{4} \quad , \quad \lambda_{1,2,3} = 0$$

# Axions and Axi-Higgs

To indicate the problem consider

$$S = -\frac{1}{4g^2} F_{\mu\nu}^2 - \frac{1}{2} (k\partial_\mu a + M A_\mu)^2 + \mathcal{A}_i a \text{Tr}[G_i \wedge G_i] - \frac{1}{2} |\partial_\mu H + ie A_\mu H|^2 + V(|H|) + \gamma H \psi \bar{\psi}$$

where  $\mathcal{A}_i$  is the mixed anomaly  $\text{Tr}[Q T_i^a T_i^a]$ . Diagonalizing and gauge fixing we obtain

$$S = -\frac{1}{4g^2} F_{\mu\nu}^2 - \frac{M^2 + e^2 v^2}{2} A_\mu^2 - \frac{1}{2} (\partial_\mu \chi)^2 - \frac{\mathcal{A}_i e v}{k \sqrt{M^2 + e^2 v^2}} \chi \text{Tr}[G_i \wedge G_i] + \gamma v e^{\frac{iM \chi}{v \sqrt{M^2 + e^2 v^2}}} \psi \bar{\psi}$$

Putting the anomaly into the fermion phase the linearized Yukawa coupling of the axion  $\chi$  to the fermions is

$$\gamma_\psi \simeq \frac{m_\psi M}{v \sqrt{M^2 + e^2 v^2}} + \frac{\mathcal{A}_i m_\psi e v}{k \sqrt{M^2 + e^2 v^2}}$$

$$\frac{1}{g^2} = \frac{V_c V_A}{g_s} \quad , \quad M^2 = \frac{V_c}{V_a} M_s^2 \quad , \quad k^2 = \frac{V_c V_a}{g_s^2} \quad , \quad \mathcal{A}_i \sim \frac{a_i}{M_s}$$

For  $M \gg M_Z$  the first term is important for heavy quarks.

For  $M \ll M_Z$ , both factors can be small, but then the  $Z'$  must be unobservable. This will happen for  $g \ll 1$  which needs four large dimensions, and then there is trouble with supernovae energy loss.

# The bulk U(1)'

We have seen that U(1)' wraps the two large dimensions. Therefore its gauge boson has finely spaced KK states, like the KK gravitons. The only other SM field that feels the large dimensions is the right-handed neutrino

An estimate of its coupling is

$$g^2 \simeq (4\pi\alpha_{\text{strong}}) \frac{M_s^2}{M_P^2} \sim 5 \times 10^{-31}$$

if its UV mass is  $M \sim M_s$  then its physical mass is

$$M_{\text{phys}} = gM_s \sim 5 \times 10^{-3} \text{ eV}$$

Although this is allowed by table-top experiments it is excluded by Supernova data because

$$\frac{P_A}{P_g} \sim \frac{1}{g_s} \left( \frac{M_s}{T} \right)^2 \sim 10^8 - 10^{10}$$

Therefore, this gauge boson must take a mass from an N=2 sector.

$$\frac{1}{g^2} = \frac{V_c V_A}{g_s} \quad , \quad M^2 = \frac{V_c}{V_a} M_s^2 \quad ,$$

This corresponds to  $V_c \gg 1$ ,  $V_a, V_A \sim 1$  which would imply  $M_{\text{phys}} \sim M_s$  which is acceptable.

# SURGEON'S WARNING !!!!!

- ♣ There are orientifold models with light spectrum only the one I presented (SM, 2 Higgses, right-handed neutrinos plus extra U(1)s)
- ♣ There are orientifold models with large compactification manifold, as advocated here.
- ♠ There are orientifold models where SUSY is broken at the String scale without closed or (unrealistic) open string tachyons.
- ♠ There are orientifold models where SUSY is broken completely and which are in equilibrium at tree level (cancelled tadpoles → cancellation of UV divergences in open theory)
- ◇ There are orientifold models, with all moduli (including the dilaton) are stabilized.
- ♥ There are orientifold models, with no fractional charged particles.
- ♥ There are orientifold models with no SM exotics.

There are combinations of the above.

HOWEVER, THERE IS NO STRAIGHT

(♣◇♠♥)

YET!