

The decay width of stringy hadrons

with Dorin Weissman

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In memory of Ioannis Bakas

On integrable models from pp-wave string backgrounds

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Abstract

We construct solutions of type IIB supergravity with non-trivial Ramond-Ramond 5-form in ten dimensions by replacing the transverse flat space of pp-wave backgrounds with exact $N = (4, 4)$ $c = 4$ superconformal field theory blocks. These solutions, which also include a dilaton and (in some cases) an anti-symmetric tensor field, lead to integrable models on the world-sheet in the light-cone gauge of string theory. In one instance we demonstrate explicitly the emergence of the complex sine-Gordon model, which coincides with integrable perturbations of the corresponding superconformal building blocks in the transverse space. In other cases we arrive at the supersymmetric Liouville theory or at the complex sine-Liouville model. For axionic instantons in the transverse space, as for the (semi)-wormhole geometry, we obtain an entire class of supersymmetric pp-wave backgrounds by solving the Killing spinor equations as in flat space, supplemented by the appropriate chiral projections: as such, they generalize the usual Novikov-Schwarz five-

Introduction

- The **stringy** description of **hadrons** has been thoroughly investigated during the sixties and seventies. What are the reasons to go back to “**square one**” and revisit this idea?
- (i) Up to date properties like the **hadronic spectrum**, their **decay width**, scattering cross section are **hard** to get from QCD and **easy** from a **string model**
- (ii) **Holography, gauge/string duality**, provides a bridge between the underlying theory of **QCD** (in certain limits) and a **bosonic string** model of mesons baryons and glueballs.
- (iii) The passage from the **holographic string regime** to **strings in reality** is still a tremendous challenge

Introduction

- (iv) up to date we lack a full exact procedure of **quantizing a rotating string with massive endpoints.**
(which is mandatory for the stringy hadrons)
- (v) There is a wide range of **heavy mesonic, baryonic** and **exotic** resonances that have been discovered in recent years. A clear identification of **glueballs** have not been yet achieved.

Introduction

- The **holographic duality** is an equivalence between certain bulk **string theories** and boundary field theories.
- Practically most of the applications of holography is based on relating **bulk fields (not strings)** and **operators** on the dual boundary field theory.
- This is based on the usual limit of $\alpha' \rightarrow 0$ with which we go for instance from a **closed string theory to a gravity** theory .
- However, to describe hadrons in reality it seems that we need **strings** since after all in reality the string tension is not very large (λ **of order one**)

Introduction

- The main theme of this talk is that there is a wide sector of **hadronic physical observables** which cannot be faithfully described by bulk fields but rather **require dual stringy phenomena**
- It is well known that this is the case for **Wilson, 't Hooft and Polyakov lines, very low x DIS** and also **Entanglement entropy**
- We argue here that in fact also the **spectra, decays** and other properties of hadrons:
mesons, baryons and **glueballs**
can be recast only by holographic **stringy hadrons**

Introduction

- The **major argument** against describing the **hadron spectra** in terms of fluctuations of fields like bulk fields or modes on **probe branes** is that they generically **do not admit** properly the **Regge behavior** of the spectra.
- For M^2 as a function of J we get from flavor branes only $J=0, J=1$ mesons and there will be a **big gap of order λ** in comparison to high J mesons if we describe the latter in terms of strings.
- The attempts to get the linearity between M^2 and n basically face problems whereas for **strings** it is an **obvious property**.
- The result of this work is that also to account for the **decay width** one needs strings and not fields

Outline

- Introduction
- A brief review of the **HISH** model and the **hadronic spectra**
- The **decay** of the hadronic string
- The **exponential suppression** of the pair quark creation
- The decay process of various types of hadrons
- Spin, isospin and flavor symmetry
- Facing **experimental data**
- Summary



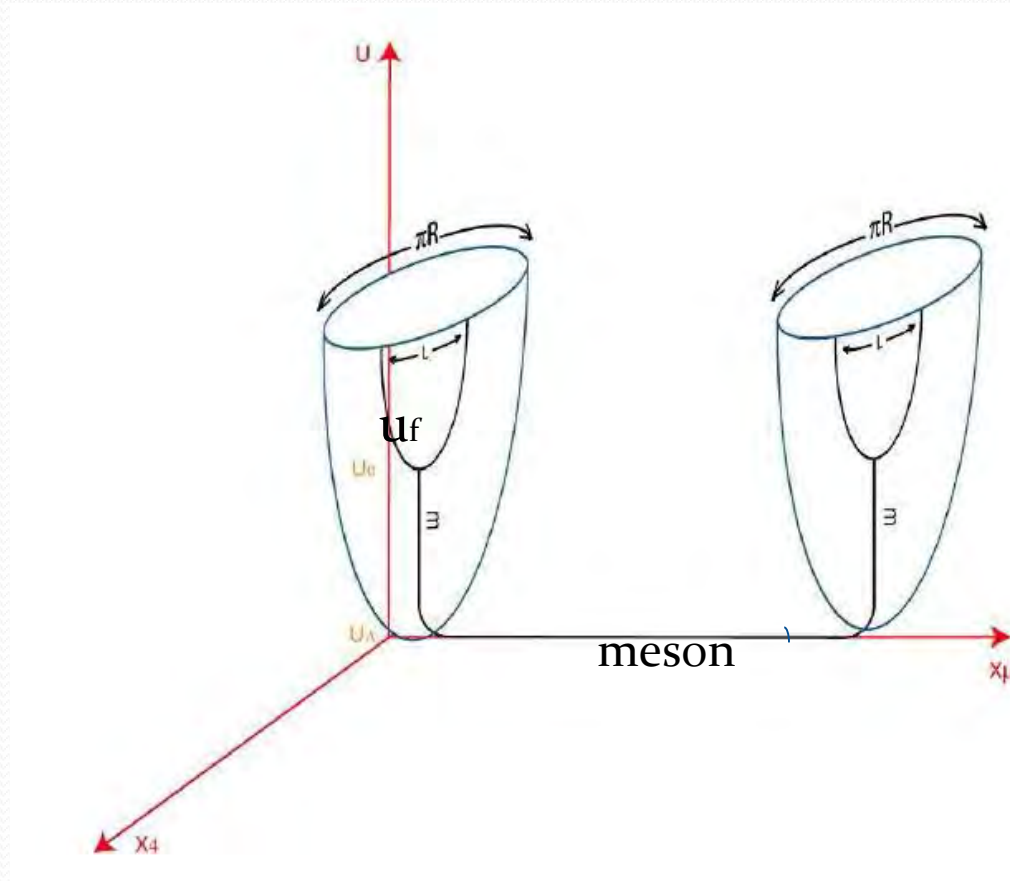
A brief review of **Holography**
Inspired stringy
hadron model

HISH

- The construction of the HISH model is based on the following steps.
- (i) Analyzing string configurations in **confining holographic string models** that correspond to hadrons,
- (ii) devising a transition from the holographic regime of large N_c and large λ to the real world that **bypasses** expansion $\frac{1}{N_c}$ and $\frac{1}{\lambda}$
- (iii) proposing a model of stringy hadrons in **flat four dimensions** that is **inspired** by the corresponding **holographic strings**,
- (iv) confronting the outcome of the models with the **experimental data** .

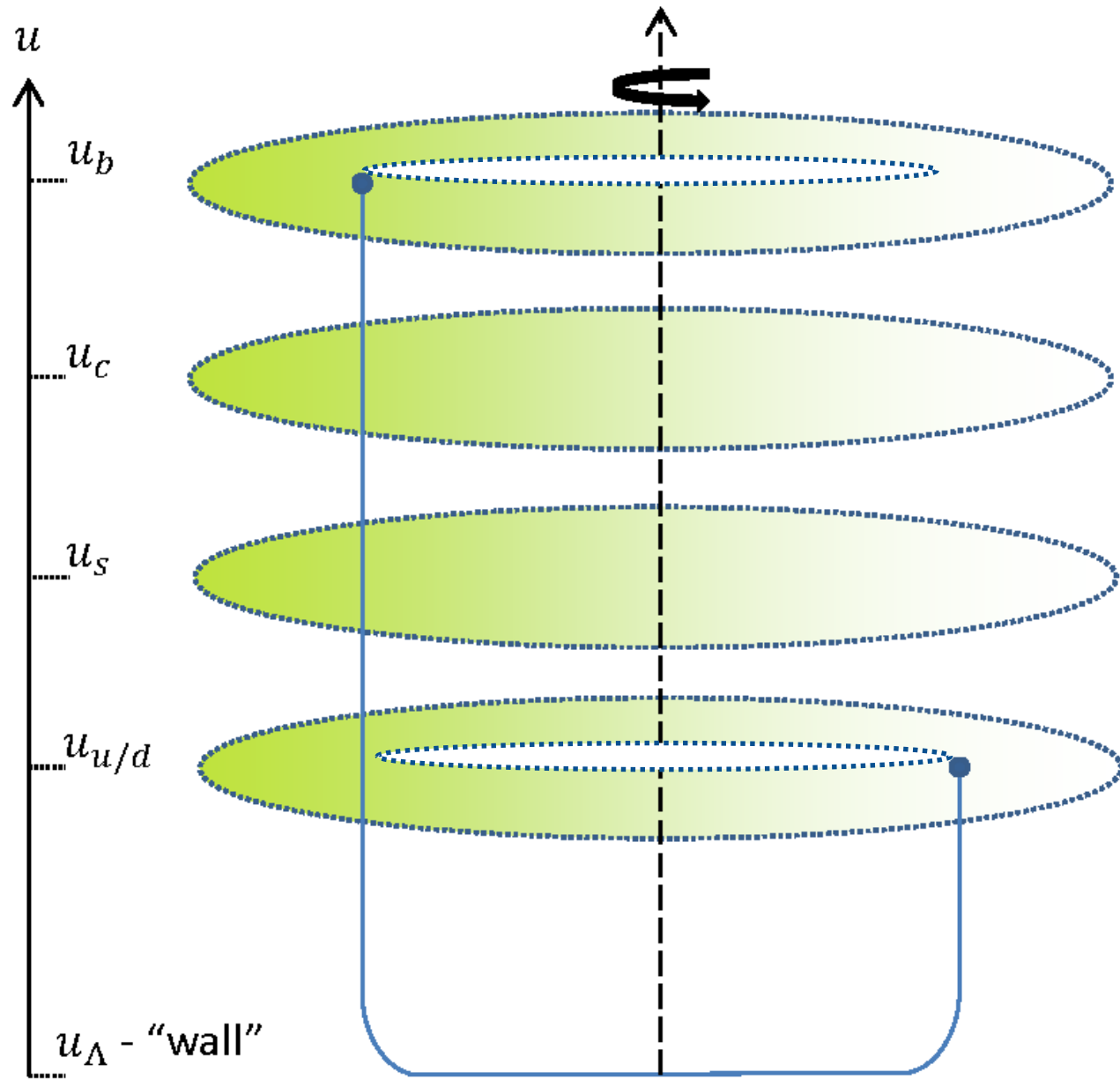
Stringy meson in U shape flavor brane setup

- In the **generalized Sakai Sugimoto** model the meson looks like



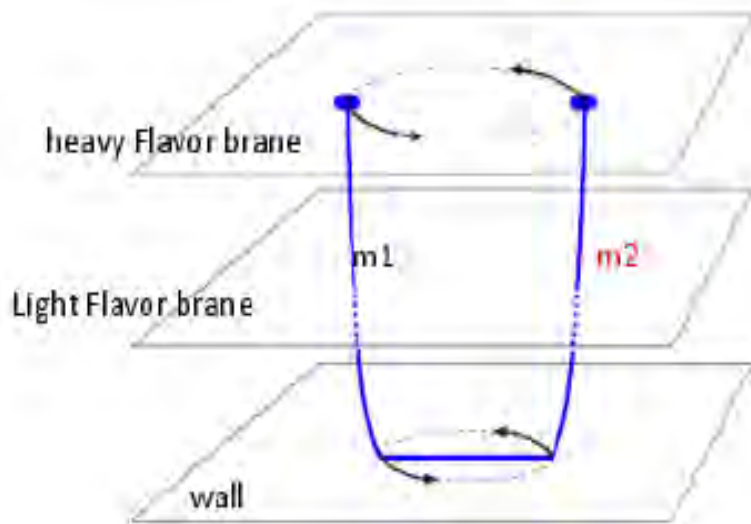
- We now **rotate** this string configuration

Example: The B meson

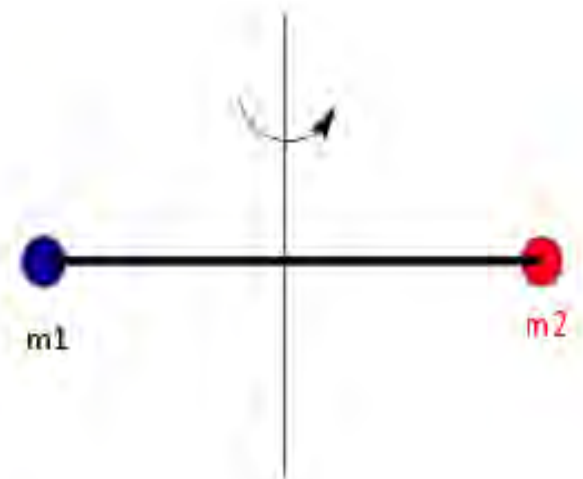


HISH

- The **vertical segments** of the holographic hadronic string can be mapped to **massive particles** at the



Rotating holographic string



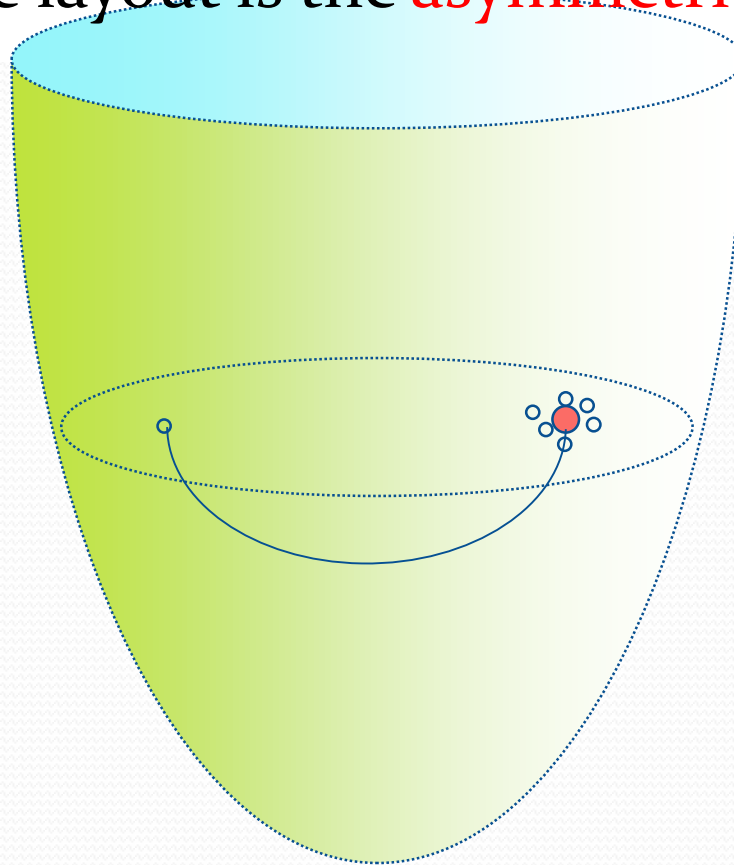
Rotating string in flat space-time with massive endpoints

end of the string with **mass**

$$m_{sep} = T \int_{u_0}^{u_f} g(u)$$

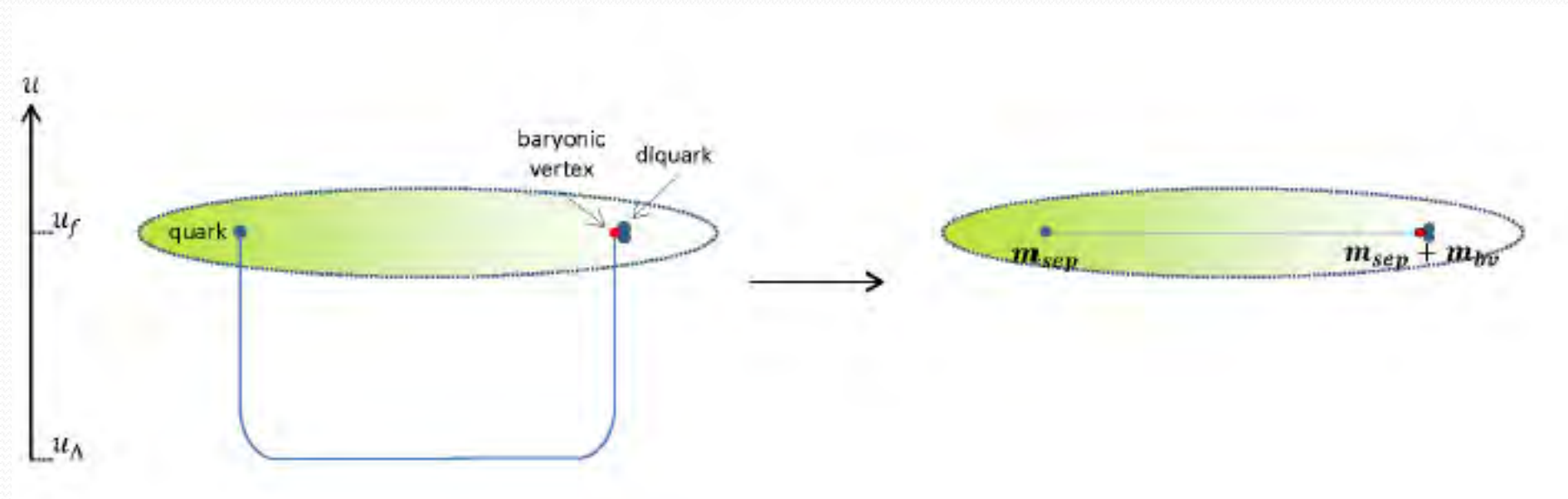
HISH Baryon

- In holography a baryon is a **baryonic vertex** which is a wrapped Dp brane on a p cycle and is connected with Nc strings to a flavor brane.
- The preferable layout is the **asymmetric** one.



HISH

- In **HISH** the holographic baryon is mapped into a single string that connects a quark on one side and a diquark on the other side



- For strings with **massive endpoints** one determine the solution of the classical EOM that corresponds to a rotating string
- The **classical energy and angular momentum**

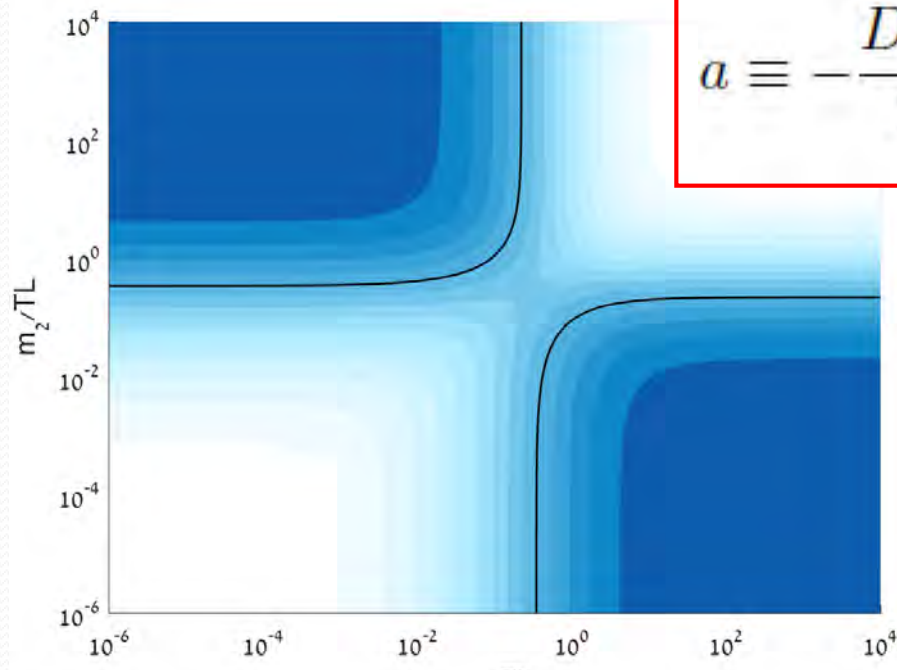
$$E = \sum_{i=1,2} \left(\gamma_i m_i + T l_i \frac{\arcsin \beta_i}{\beta_i} \right)$$

$$J = \sum_{i=1,2} \left[\gamma_i m_i \beta_i l_i + \frac{1}{2} T l_i^2 \left(\arcsin \beta_i - \beta_i \sqrt{1 - \beta_i^2} \right) \right]$$

- The **quantum intercept for a static string** $J \rightarrow J - a$.

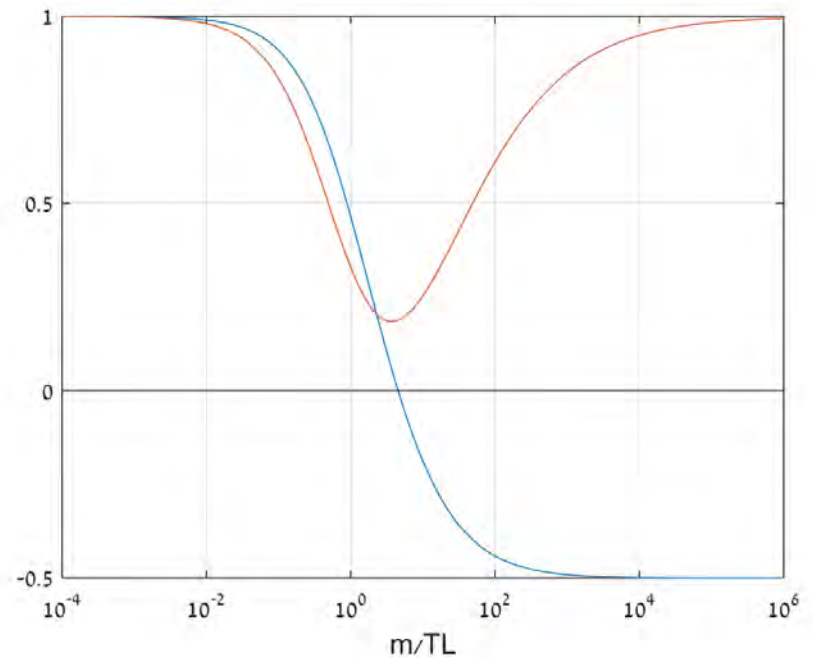
$$\hat{a}(q_1, q_2) = \frac{1}{2\pi^2} \int_0^\infty dz \log \left[1 - e^{-2z} \left(\frac{q_1 - z}{q_1 + z} \right) \left(\frac{q_2 - z}{q_2 + z} \right) \right]$$

The intercept for a string with massive endpoints



$$a \equiv -\frac{D-2}{2\pi} \sum_{n=1}^{\infty} \omega_n$$

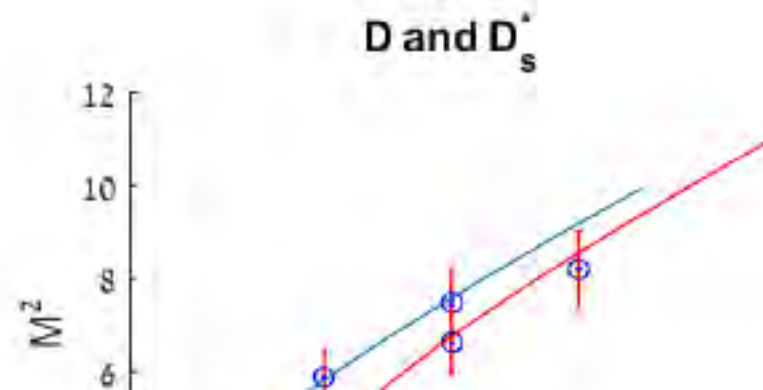
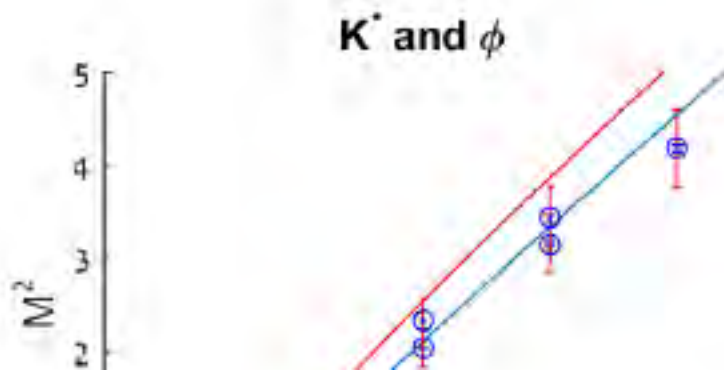
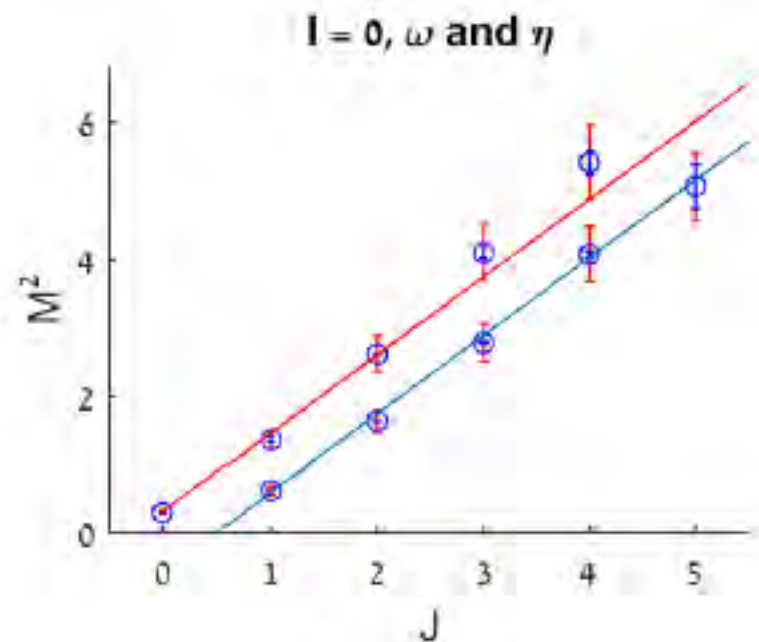
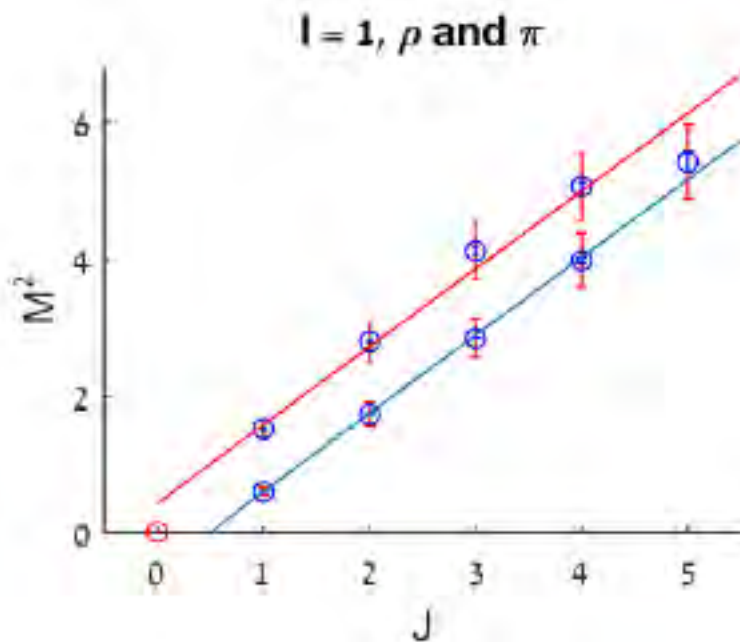
The intercept of a static string
as a function of the mass



$$\tan(\omega_n) = \frac{2q\omega_n}{q^2\omega_n^2 - 1}$$

The spectra fits

- The **best fits** of HISH to **meson states**

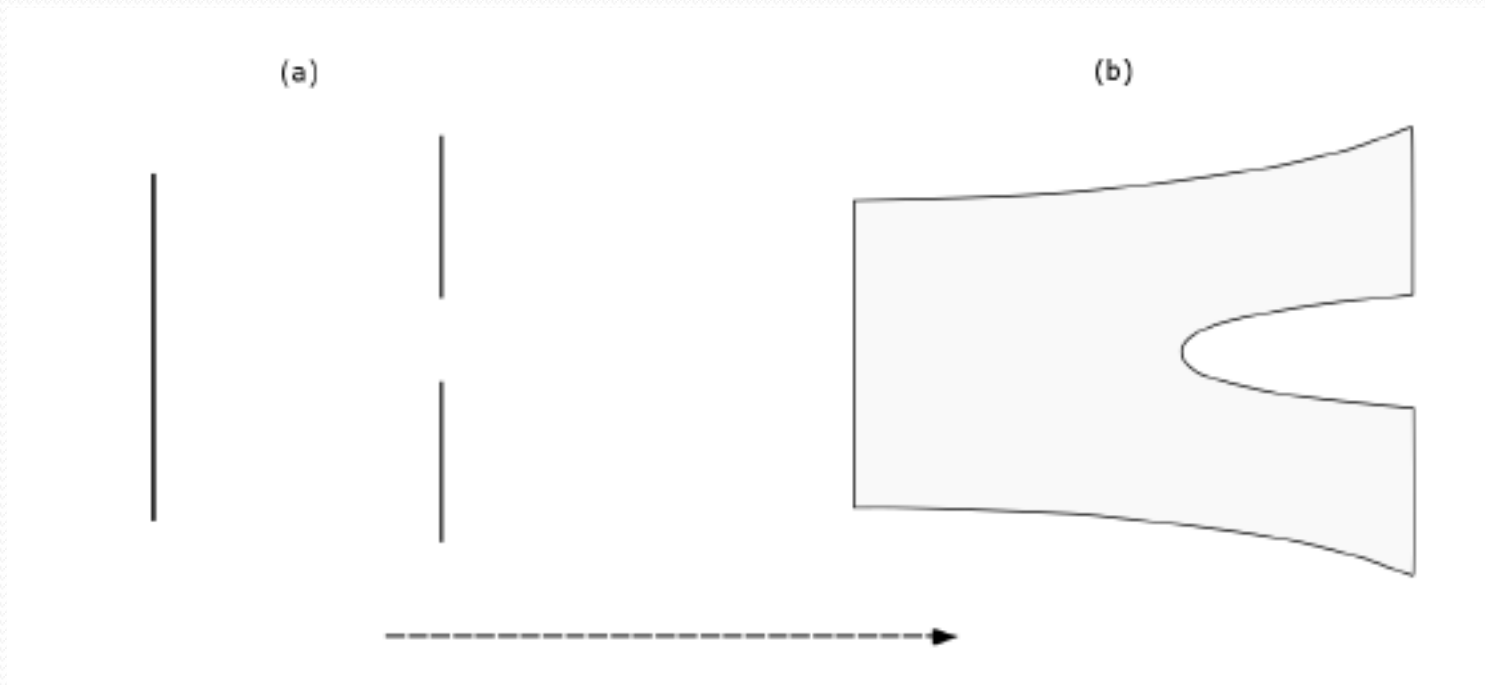




The decay of the hadronic string

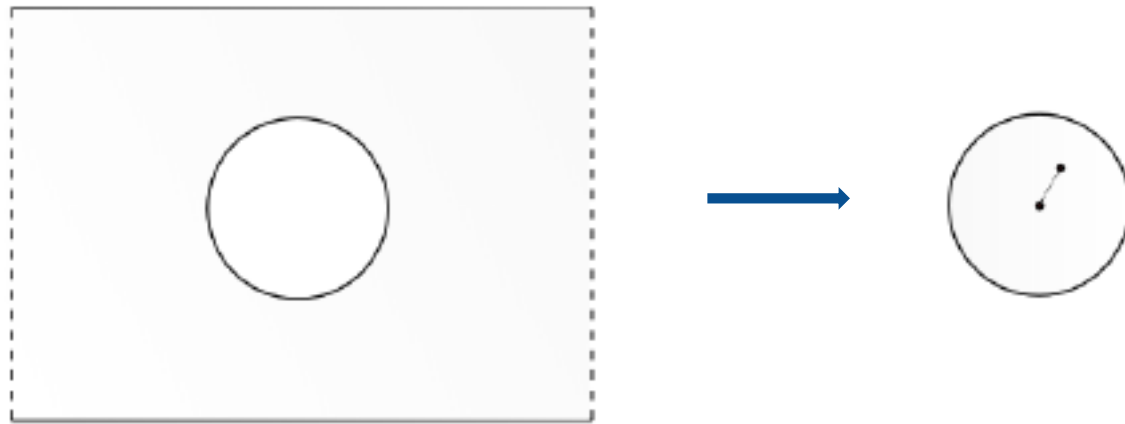
The decay of a long string in flat space-time

- The decay of a hadron is in fact the **breaking of a string into two strings**
- Obviously a type I open string can undergo such a split



The decay of a long string in flat space-time

- The **total decay width** is related by the **optical theorem** to the **imaginary part of the self-energy diagram**
- A trick that **Polchinski** et al used is to **compactify one space coordinate** and consider incoming and outgoing strings that wrap this coordinate so one can use the **simple vertex operator of a closed string**



The decay of a long string in flat space-time

- We would like to determine the dependence of the **string amplitude** on the **string length L**

$$i\mathcal{A}_2 = \frac{iTN}{g^2} L \left[\frac{\kappa}{2\pi\sqrt{\alpha'}} \right]^2 \int_{|z|<1} d^2z \langle : e^{ip \cdot X(0)} :: e^{-ip \cdot X(z)} : \rangle$$

open string
coupling

Zero mode

Gravitational
coupling

Normalization
Of the vertex

Vertex operator

The decay of a long string in flat space-time

- A further dependence on L comes from the energy and momenta

$$P_L = (E, LT, 0) \quad P_R = (E, -LT, 0) \quad E = \sqrt{(TL)^2 - 8\pi T}$$

For open strings $\frac{a}{\alpha'} = 2\pi T a = \frac{D-2}{24} = 1$

For closed strings the tension and intercept are twice

The decay of a long string in flat space-time

- Using the **vertex operator**

$$e^{iP \cdot X} = e^{i(P_L \cdot X_L + P_R \cdot X_R)}$$

and the **standard OPE**

$$\begin{aligned} \langle : e^{iP \cdot X(0)} :: e^{iP \cdot X(z)} : \rangle &= z^{-\frac{P_R^2}{4\pi T}} \bar{z}^{-\frac{P_L^2}{4\pi T}} (1 - z\bar{z})^{-\frac{P_R \cdot P_L}{4\pi T}} \\ &= |z\bar{z}|^{-2} (1 - z\bar{z})^{\tilde{J}} \end{aligned}$$

$$\tilde{J} \equiv \frac{L^2 T}{2\pi} - 2$$

The decay of a long string in flat space-time

- After substituting the amplitude reads

$$i\mathcal{A}_2 = \frac{iTN\kappa^2}{2\pi g^2} \lim_{t \rightarrow 0} \frac{\Gamma(t-1)\Gamma(1-\tilde{J})}{\Gamma(t-\tilde{J})}$$

$$= \frac{iTN\kappa^2}{2\pi g^2} \left(\tilde{J} \partial_{\tilde{J}} \ln[\Gamma(-\tilde{J})] + \lim_{t \rightarrow 0} \frac{\tilde{J}}{t} \right)$$

regulator

- The imaginary part $\sum_k \pi k \delta(J-k)$ for $k = 1, \dots$

$$\text{Im}\mathcal{A}_2 = -\frac{iTN\kappa^2}{2g^2} \tilde{J}$$

The decay of a long string in flat space-time

- Since A_2 is the **mass square shift** the **total decay width**

$$\Gamma = -\text{Im}\delta(m) = -\text{Im}\frac{1}{2m}\delta(m^2) = \frac{TN\kappa^2}{4g^2} \frac{\tilde{J}}{E}$$

- The **leading behavior** for string in $d=26$ is

$$\frac{\Gamma}{L} = \frac{g^2 T^{13} N}{4(4\pi)^{12}}$$

$$\Gamma = \frac{TN\kappa^2}{4g^2} \left[L_{tot} + \frac{4\pi}{T} \frac{1}{L_{tot}} \right]$$

$$L_{tot} = \sqrt{L^2 - \frac{8\pi}{T}}$$

The decay of rotating and excited strings

- For a rotating string due to time dilation we get

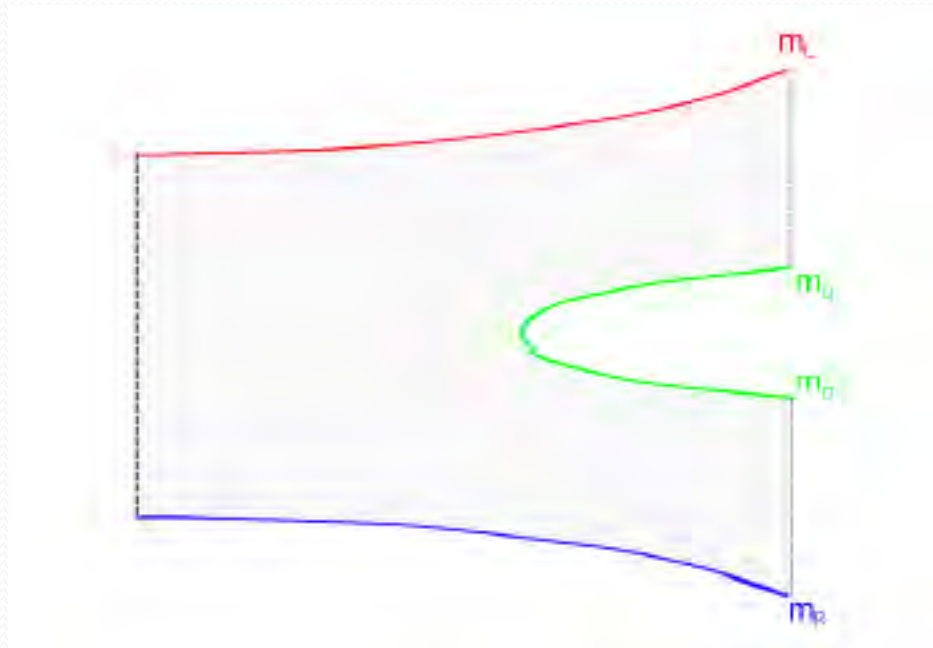
$$\Gamma = \left(\frac{\Gamma}{L}\right)_{\text{stat}} \int_{-L/2}^{L/2} d\sigma \sqrt{1 - (\sigma w)^2} = \frac{\pi}{4} \left(\frac{\Gamma}{L}\right)_{\text{stat}} L$$

- For nth excited string

$$\Gamma_n = \left(\frac{\Gamma}{L}\right) \sqrt{\frac{2\pi(n-a)}{T}}$$

The decay width of a string with massive endpoints

- The decay of a string with **massive particles on its ends**

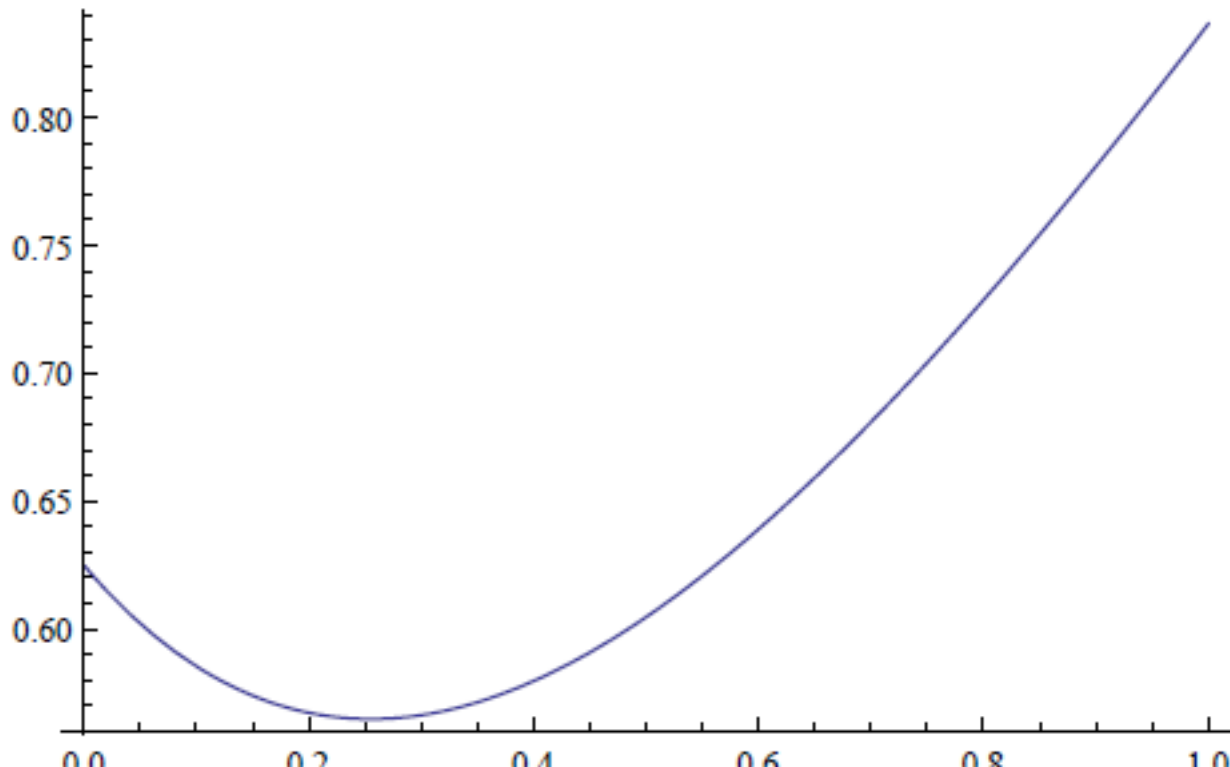


- The dependence on the masses:
 - (a) The **length** $L(m_1, m_2)$
 - (b) The **boundary conditions** (not anymore Neuman)

The decay width of a string with massive endpoints

- For **small endpoint masses** we can expand *

$$\Gamma \propto \frac{\pi}{4}TL + \frac{\pi}{4}m - \frac{2\sqrt{2}}{3}m^{3/2}(TL)^{-1/2} + \mathcal{O}(L^{-3/2})$$



The decay width in non-critical dimensions

- N. Turok et al analyzed the decay width of **open string in d dimension**. They got

$$\Gamma \sim L^{\frac{D-14}{12}} = L^{\frac{D-2}{12}-1}$$

- Thus linearity for $d=26$ but $\Gamma \sim L^{-\frac{5}{6}}$ in $D=4$.
- But this analysis took only the **transverse modes**.
Their result follows from

$$\text{Im}[\delta(m^2)] \sim t^{\frac{D-2}{24}} = t^a$$

- It was shown by **Hellerman** et al that the **intercept**

$$a = a_{cr} + a_{PS} = \frac{(D-2)}{24} + \frac{(26-D)}{24} = 1$$

- Thus for **any d dimension**

$$\Gamma \sim \frac{t^a}{E} \sim L^1$$

The decay of a stringy hadron

- We just argued that the **intercept** of a string at D dim
 $a=1$

- In fact **experimental** value of the intercept a_{exp} is negative

$$a_{exp} = -|a_{exp}|$$

- Thus the leading order width of a string with no massive endpoints

$$\Gamma \sim \frac{N\kappa^2}{4g^2} TL \left[1 + \frac{4|a_{exp}|^2}{\alpha'^2 (TL)^4} + \dots \right]$$

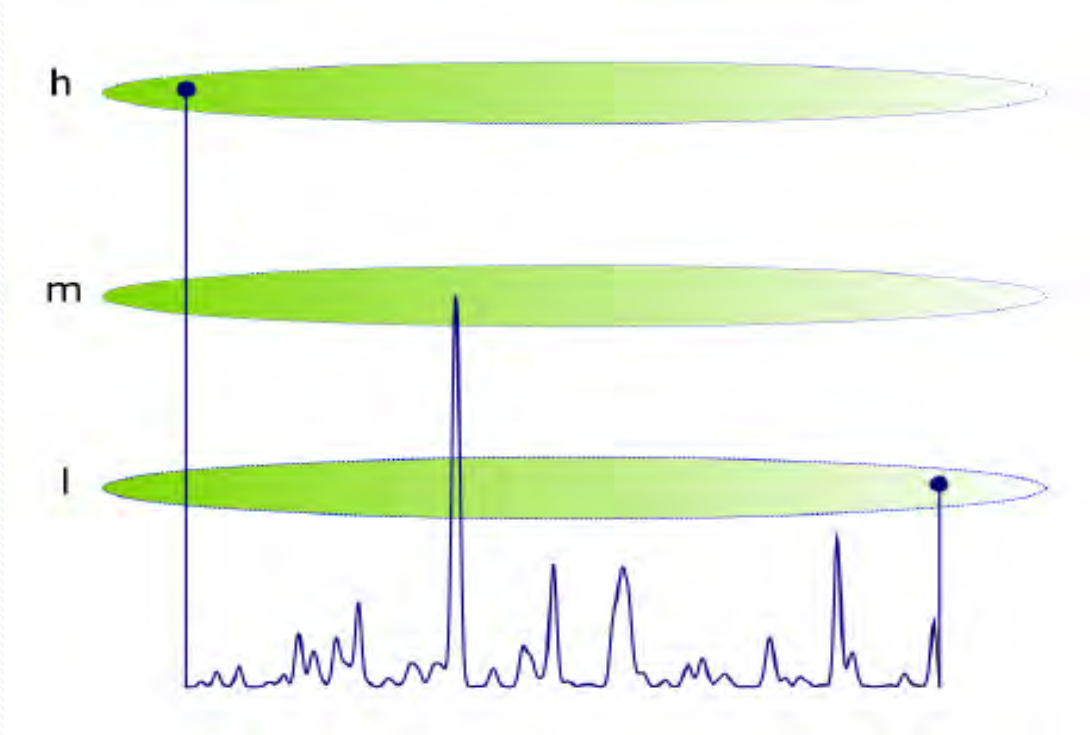
- With massive endpoint we combine this with *



Exponential
suppression of pair
creation

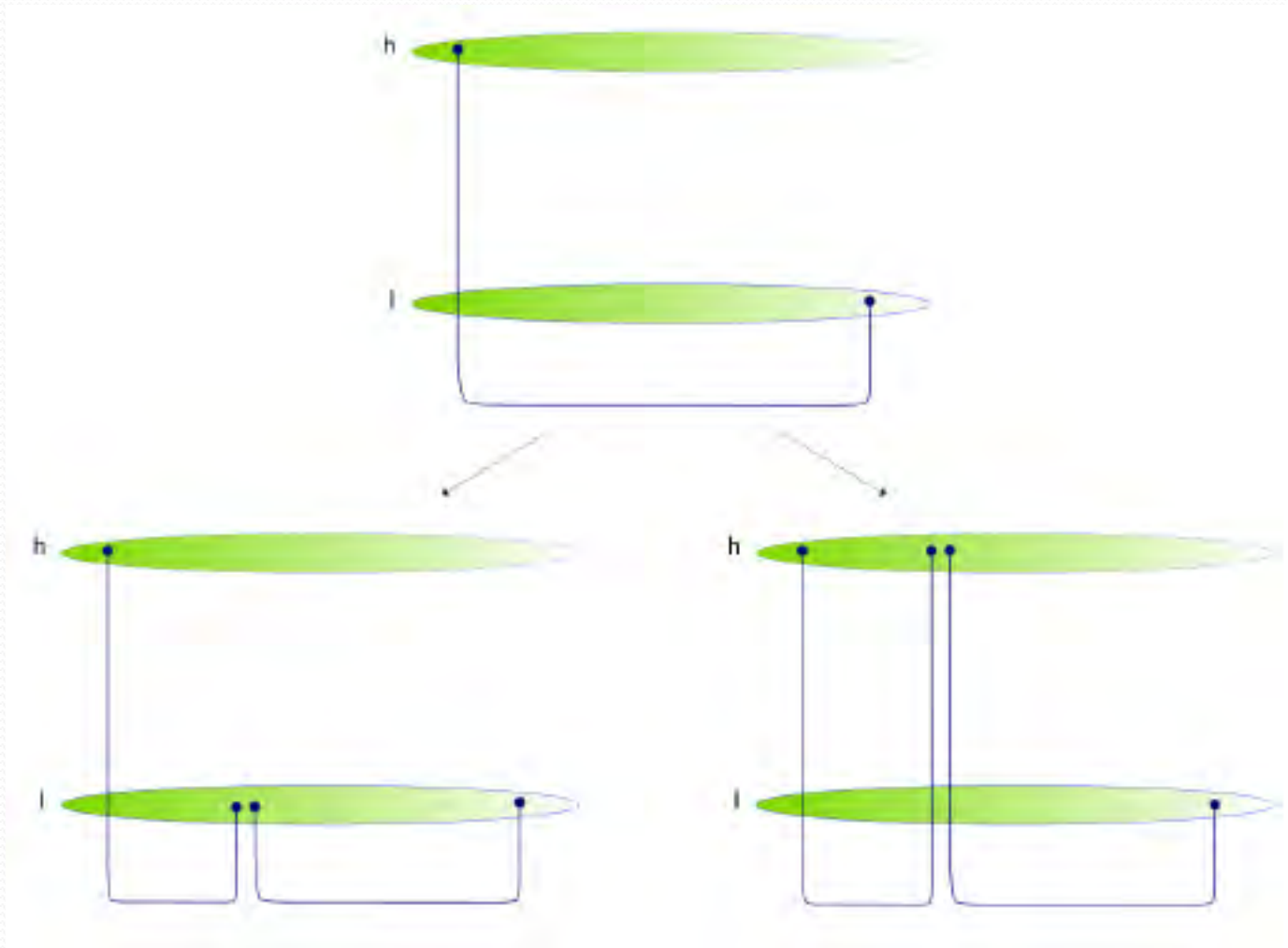
The suppression factor for stringy holographic hadrons

- The horizontal segment of the stringy hadron **fluctuates** and can reach flavor branes
- When this happens the string may **break up**, and the two new endpoints connect to a flavor brane



The suppression factor for stringy holographic hadrons

- There are in fact several possible **breakup patterns**



Determination of the suppression factor

- Assuming first that the string stretches in flat space-time we found (J.S, K. Peeters , M. Zamamklar) using both a **string beads model** and a **continues** one that

$$\Gamma = \text{const.} \cdot \exp \left(-1.0 \frac{z_B^2}{\alpha'_{\text{eff}}} \right) \cdot T_{\text{eff}} \mathcal{P}_{\text{split}} \cdot L$$

$$\exp \left(-1.0 \frac{z_B^2}{\alpha'_{\text{eff}}} \right) = \exp \left(-2\pi \frac{m_{\text{sep}}^2}{T_{\text{eff}}} \right)$$

- There are further corrections due to the **curvature** and due to the **massive endpoints**.

$$\Gamma = \exp \left(-2\pi C(T_{\text{eff}}, M, m_i) \frac{m_{\text{sep}}^2}{T_{\text{eff}}} \right)$$

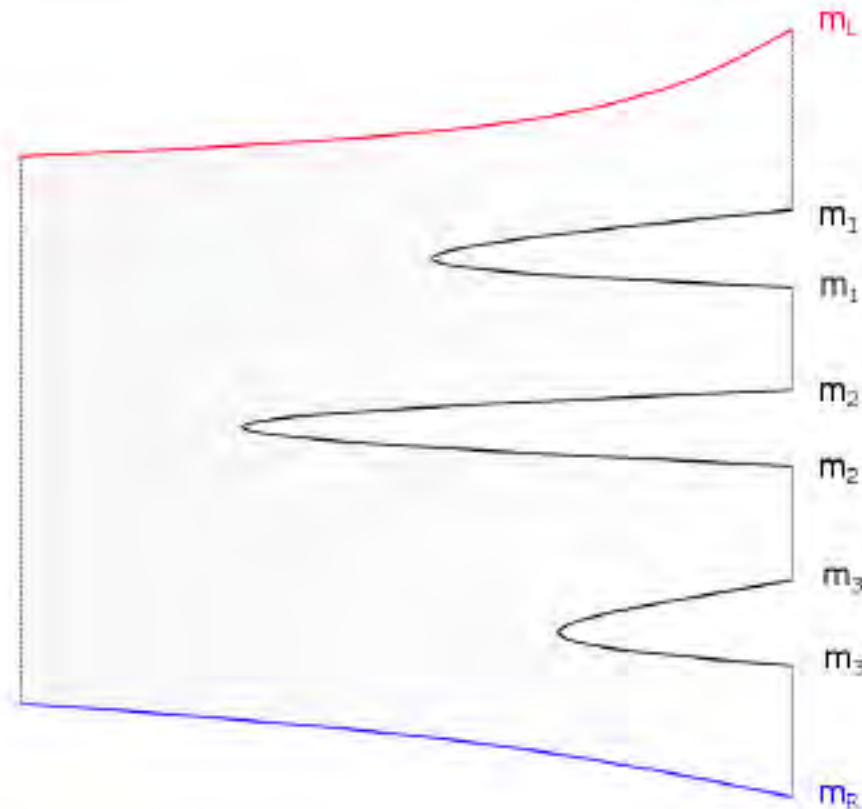
$$C(T_{\text{eff}}, M, m_i) \approx 1 + c_c \frac{M^2}{T_{\text{eff}}} + \sum_{i=1}^2 c_{m_i} \frac{m_i}{M}$$

Multi string breaking and string fragmentation

- The basic process of a string splitting into two strings can of course repeat itself and thus eventually describe a decay of a single string into **n strings**
- The probability for a multi-decay

$$\mathcal{P} = \frac{T_{\text{eff}}^2}{\pi^3} \sum_i \sum_{\omega_n=1}^{\infty} \frac{1}{\omega_n^2} \exp\left(-2\pi C \frac{m_{\text{sep}_i}^2 \omega_n}{T_{\text{eff}}}\right).$$

This mechanism is believed to be the **generator of jets**. It is incorporated in Pithya

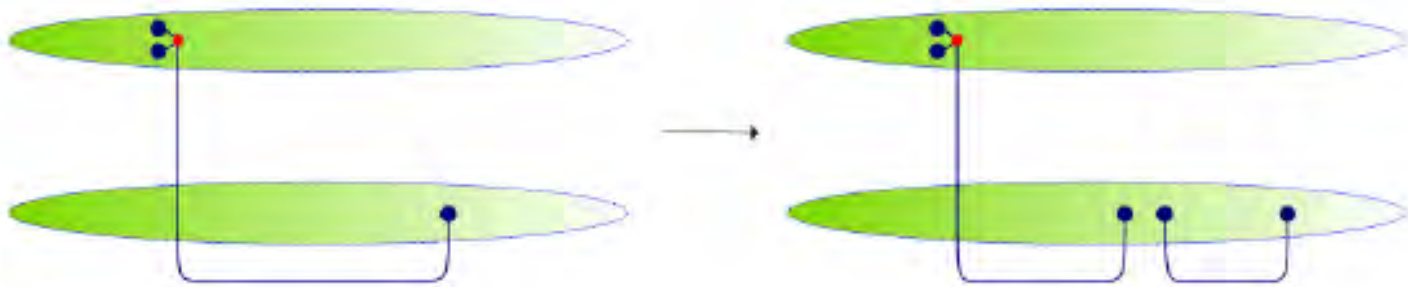




The Decay process of the different types of hadrons

The decay process of Baryons

- A baryon in HISH is a string connected to a **quark and to a di-quark** so its decay is also by a string splitting

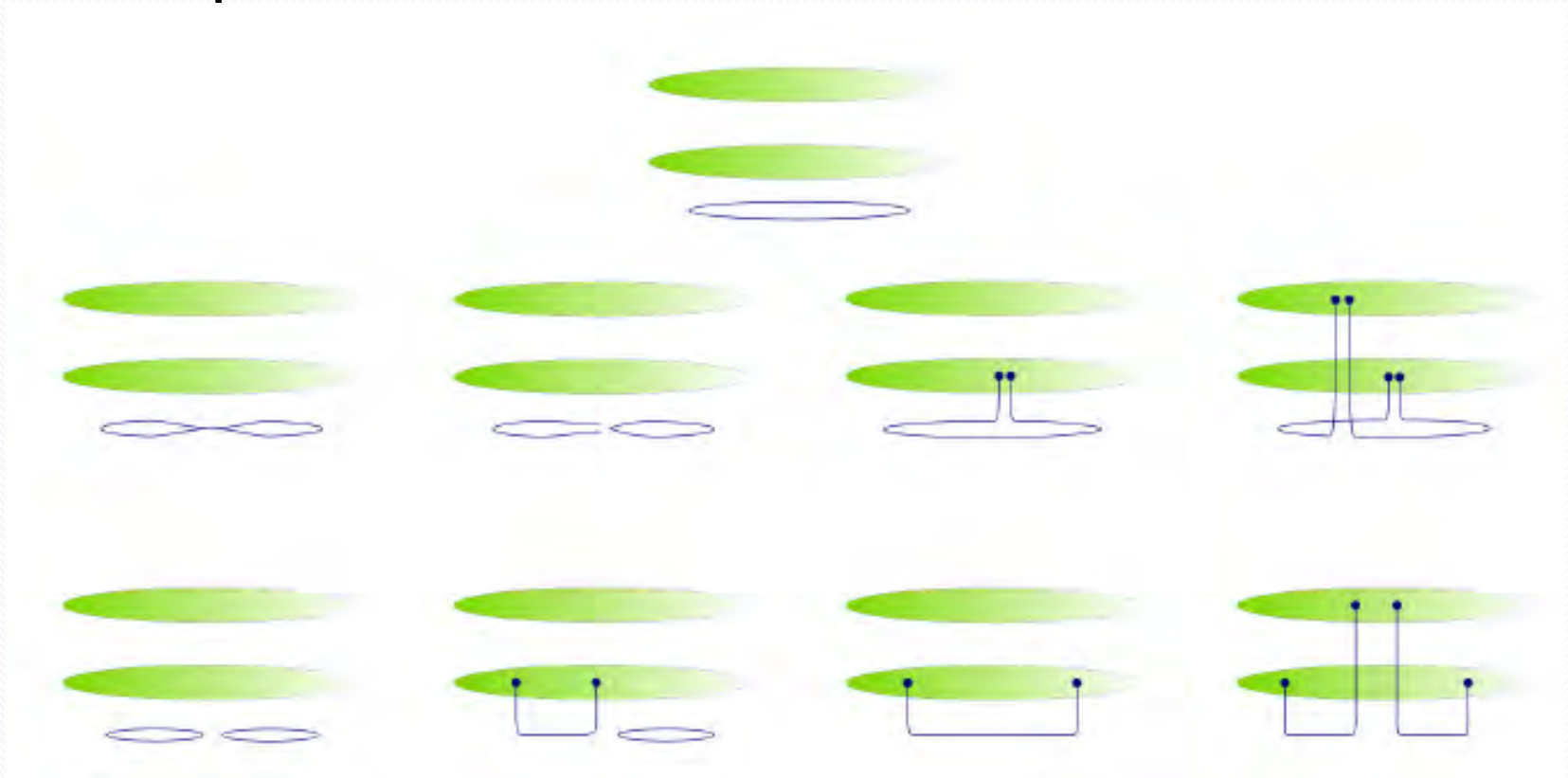


- A way to **determine what is the diquark pair** and which is the stand-alone quark is by identifying the decay products

$[(q_1 q_2) q_3]$	$[(q_1 q_3) q_2]$	$[(q_2 q_3) q_1]$
↓	↓	↓
$[(q_1 q_2) Q_i] [\bar{Q}_i q_3]$	$[(q_1 q_3) Q_i] [\bar{Q}_i q_2]$	$[(q_2 q_3) Q_i] [\bar{Q}_i q_1]$

Decay of glueballs

- The glueball which is a folded rotating closed string



- The width

$$\Gamma_a \sim L\Gamma_{\text{cross}}$$

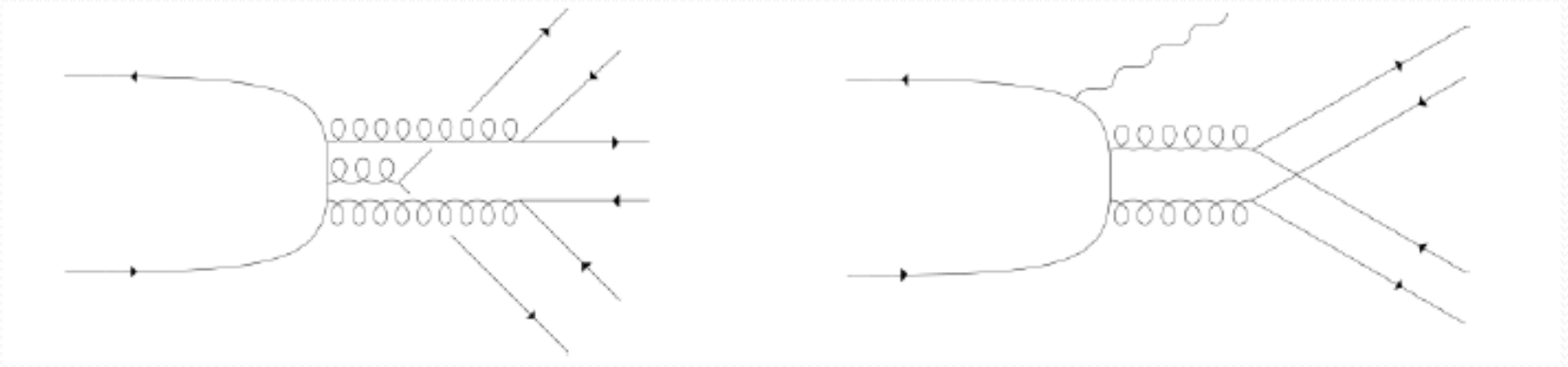
$$\Gamma_c \sim L e^{-2\pi C m_{\text{sep}}^2 / T}$$

$$\Gamma_b \sim L\Gamma_{\text{cross}} e^{-2\pi C m_{\text{sep}}^2 / T}$$

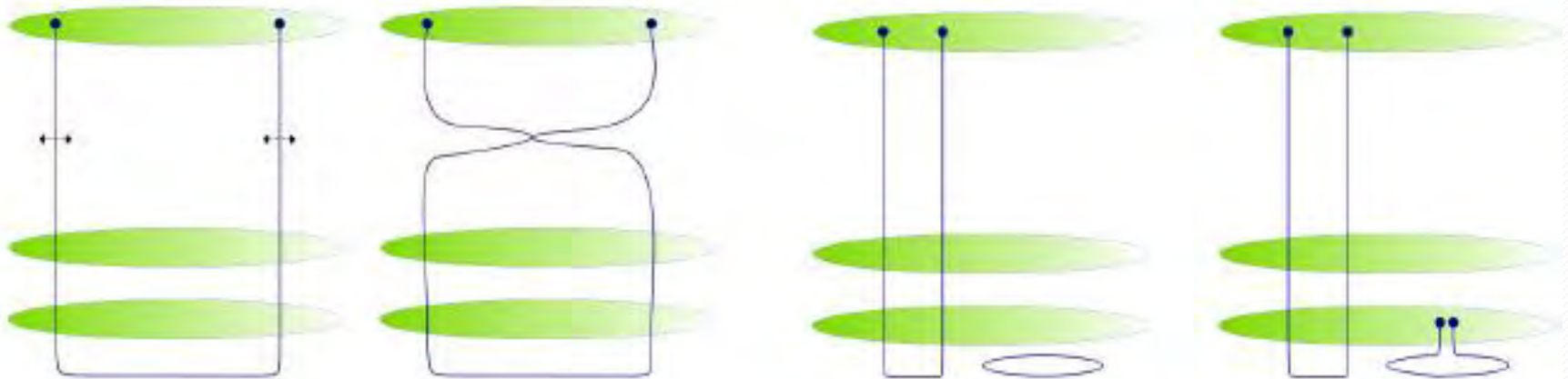
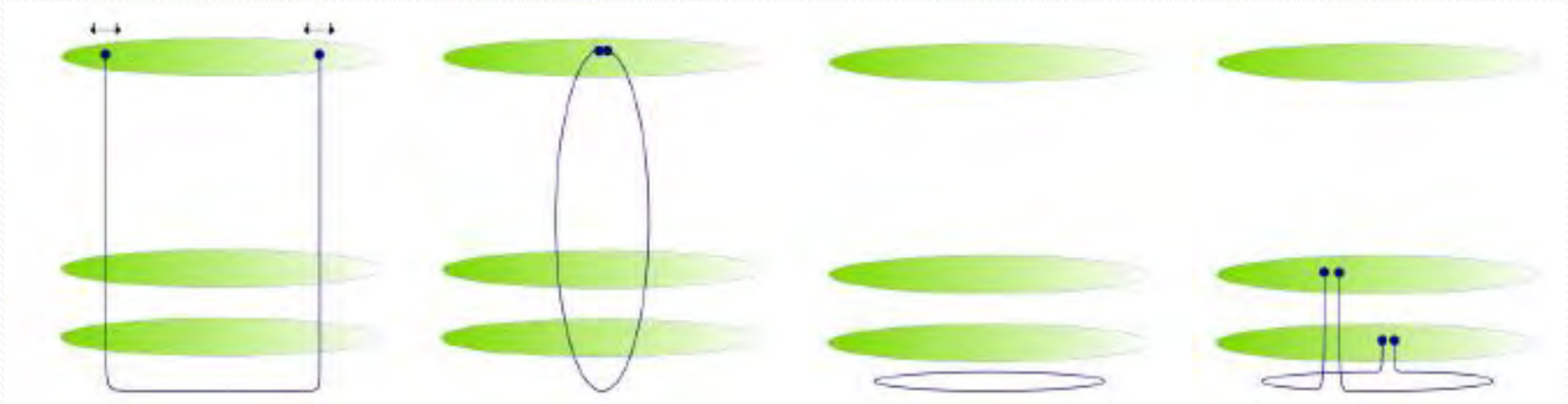
$$\Gamma_d \sim L^2 e^{-2\pi C m_{\text{sep}}^2 / T} e^{-2\pi C m_{\text{sep}}'^2 / T}$$

Zweig suppressed decay channels

- Certain heavy **quarkonia mesons**, build out of $c\bar{c}$ or $b\bar{b}$, **cannot decay** via the mechanism of breaking apart of the horizontal string
- In QCD the decay based of the **annihilation of the pair** into 3 gluons or e 2 gluons and a photon



Zweig suppressed decay channels

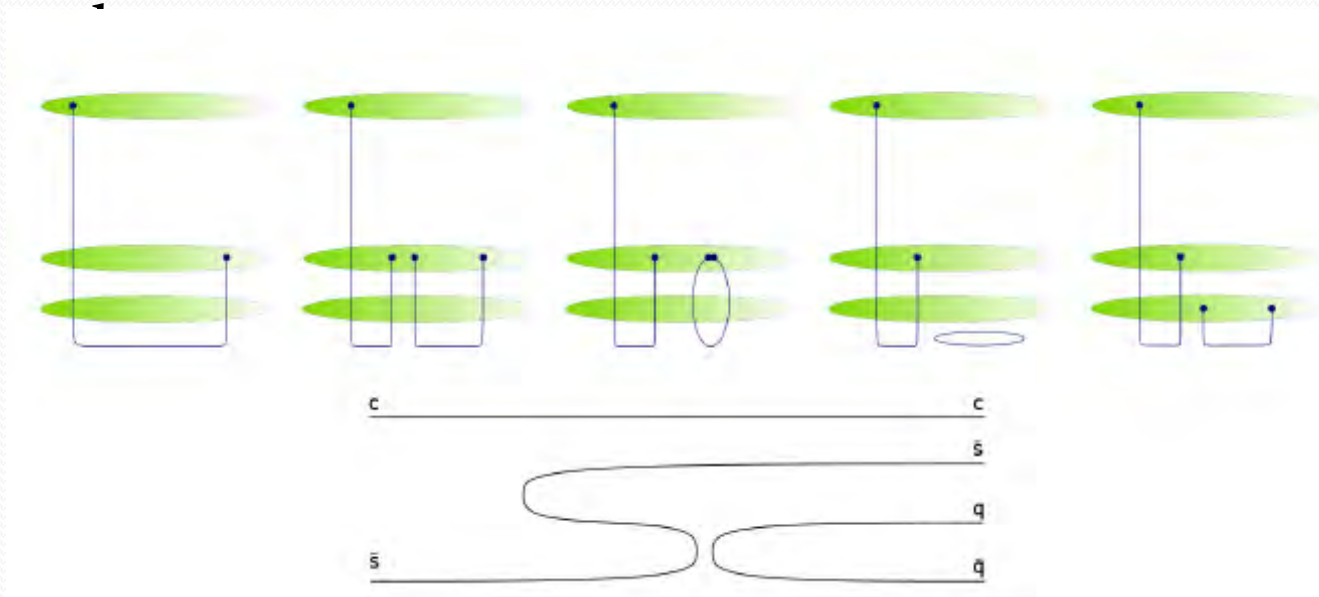


Zweig suppressed decay channels

- An approximation for probability of process a

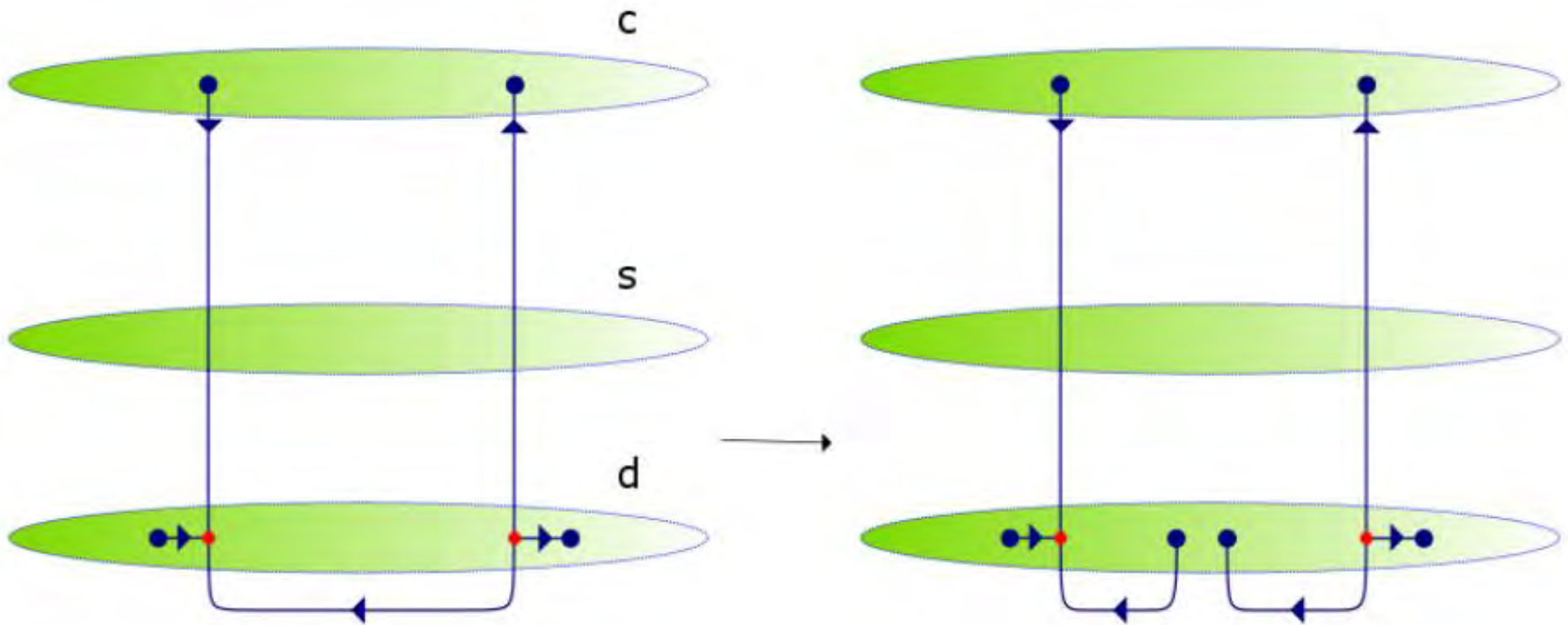
$$\begin{aligned}
 \mathcal{P} &= \int_{-\infty}^{\infty} dx \psi(x - L/2)\psi(x + L/2) = \\
 &= \int_{-\infty}^{\infty} dx \exp[-T_{av}(x - L/2)^2] \exp[-T_{av}(x + L/2)^2] = \\
 &= \sqrt{\frac{\pi}{2T_{av}}} e^{-T_{av}L^2/2} = \sqrt{\frac{\pi}{2T_{av}}} e^{-\frac{4(M-2m)^2}{9T_{av}}}
 \end{aligned}$$

- Virtual pair** combined with a **Zweig suppressed**



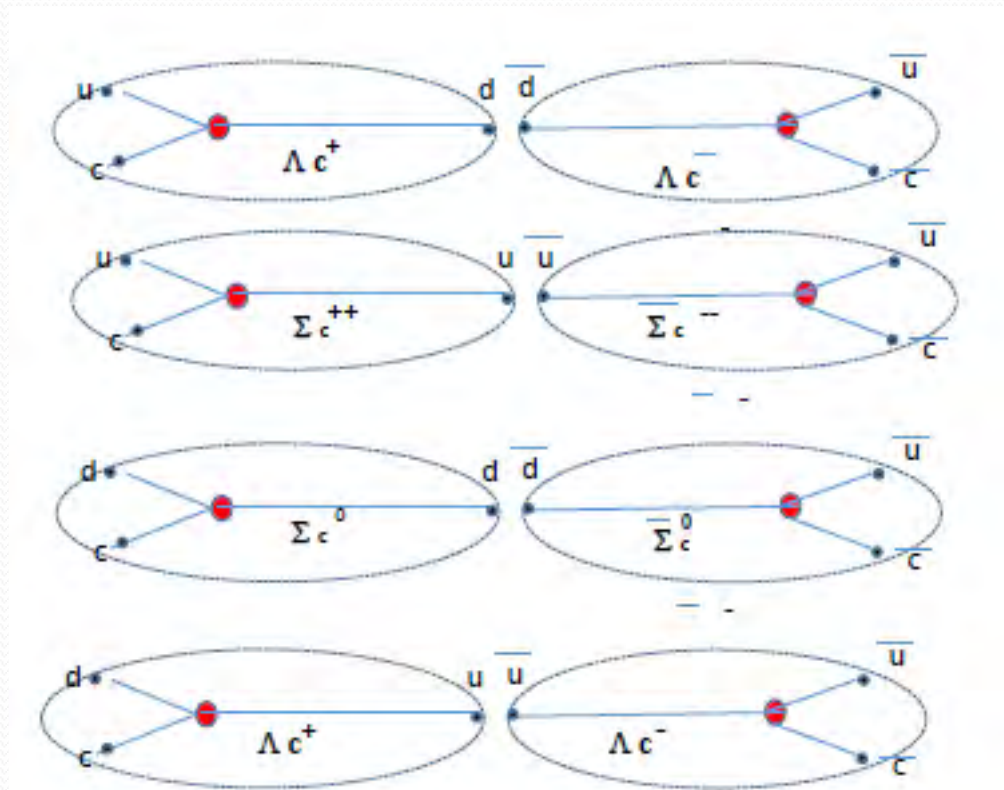
Decays of exotic hadrons

- An **exotic tetraquark** built from a string connecting a di-quark and an anti di-quark will decay predominantly to a **baryon anti-baryon**



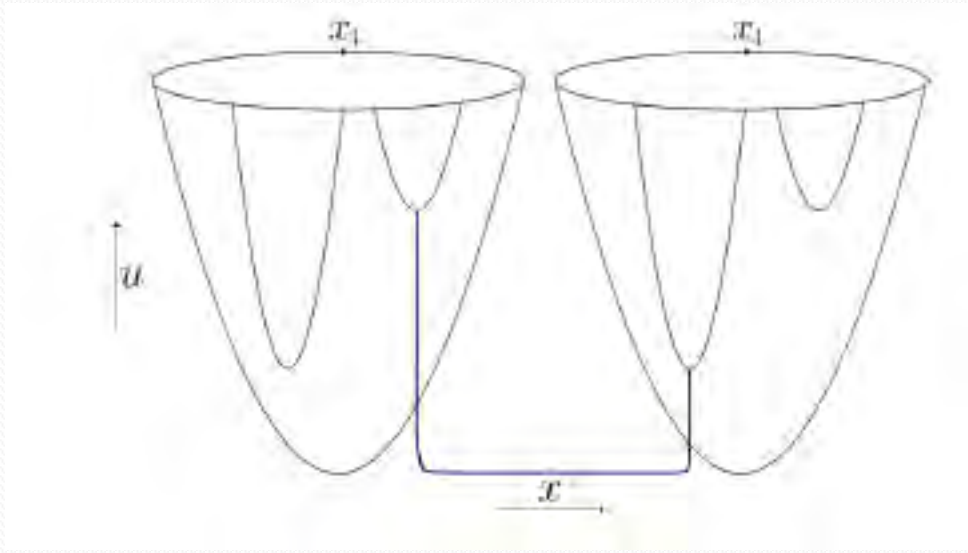
Decays of exotic hadrons

- The HISH picture of possible decays



Decays via breaking of the vertical segment

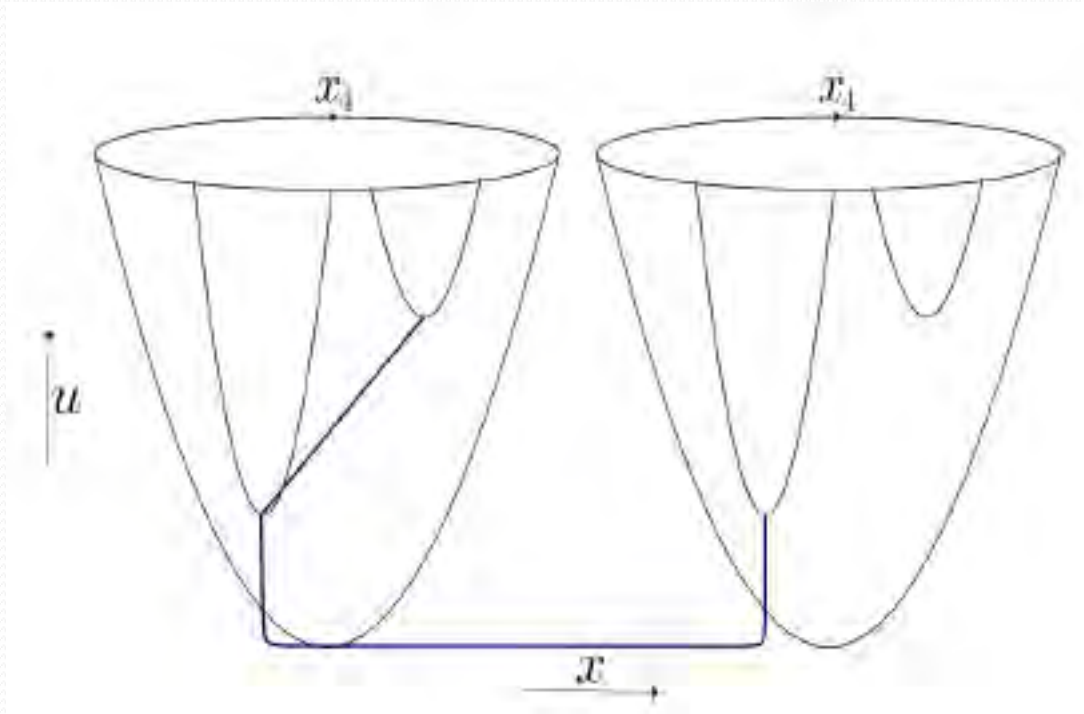
- Nothing prevents a breaking of the **vertical segments**. What is the hadronic interpretation of it?
- We first clarify the holographic set up of hadrons



- So the vertical segment of a heavy flavor **does not cross** that of a lighter flavor brane.

Decays via breaking of the vertical segment

- The **vertical segment** can split as follows



- We get a meson plus a string that stretches only in the radial and x_4 but **not is space-time coordinates**

Decays via breaking of the vertical segment

- In a similar way to the computation of the width associated with the breaking of the horizontal segment, the width associated with the **breaking of a vertical segment** should be

$$\Gamma_{\text{vertical}} \sim \int_{u_{\Lambda}}^{u_B} du \exp \left(-C_v \frac{(\Delta_{x_4}(u))^2}{\alpha'(u)} \right)$$

- The interpretation of the decay processes associated with the vertical breaking is **not well understood**.
- One possibility is that the vertical string segments that are “particles” from the space-time point of view are the **Goldstone boson mesons** pions and kaons.



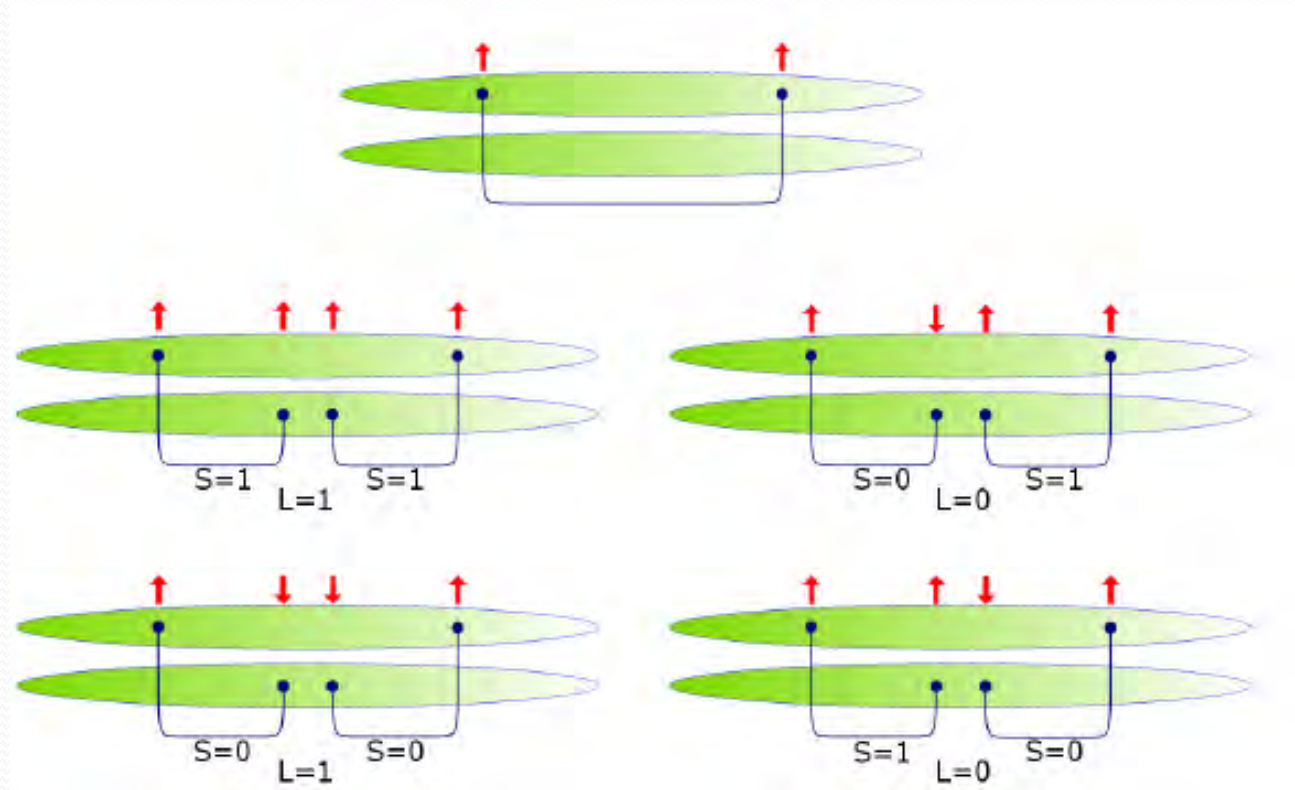
The Decay modes spin and flavor symmetry

Decay modes, spin, and avor symmetry

- Considerations of **spin and isospin** or more generally flavor symmetry of the initial and final states are very important in determining which decays are **forbidden** and the **relative decay** width of the allowed ones.
- How are such considerations been realized in the holographic decay mechanism of stringy hadrons.
- The **spectra** of hadrons is slightly affected by spin and isospin via the **dependence of the intercepts** .
- This issue has to be further studied

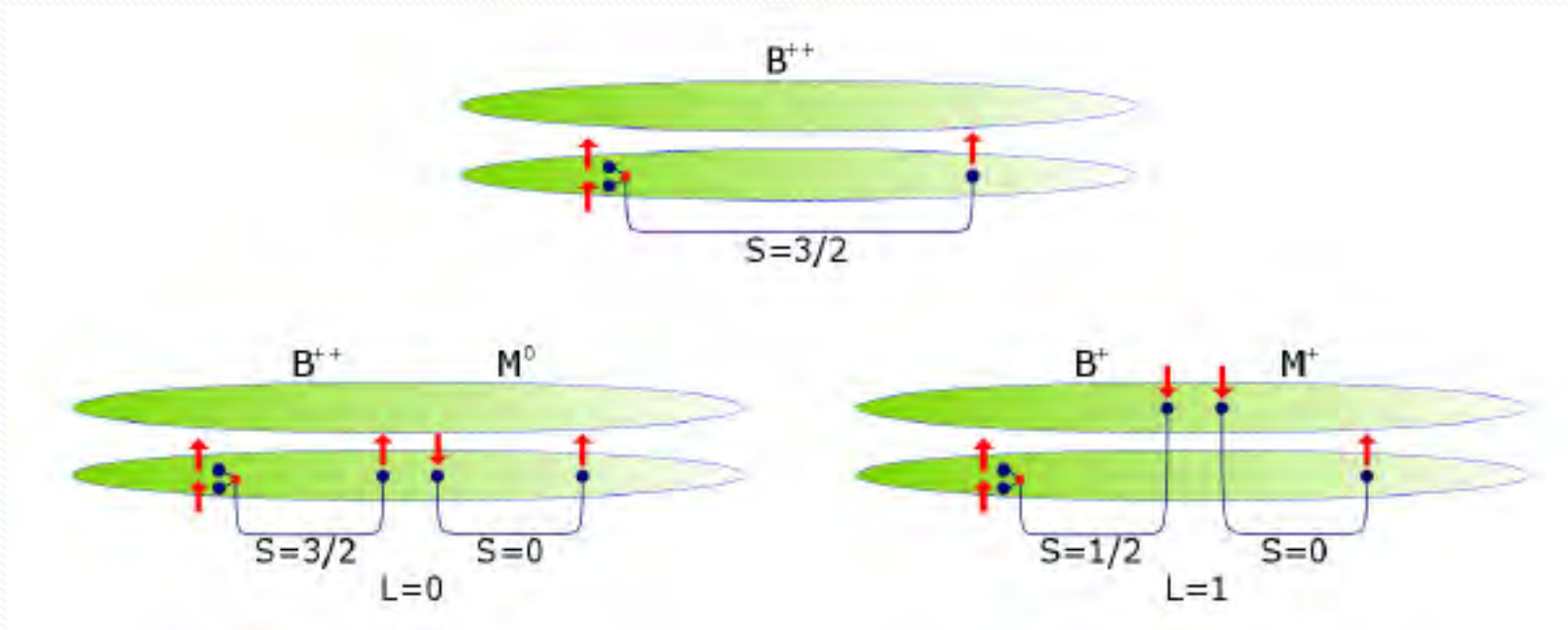
The spin structure of the stringy decays

- We assume that the **spin** degrees of freedom are carried by the **particles** that are on the string endpoints
- The spin structure of allowed decays of a neutral meson M_0 with spin $S=1$ into M_+ and M_- mesons. The arrows indicated the values of S_z



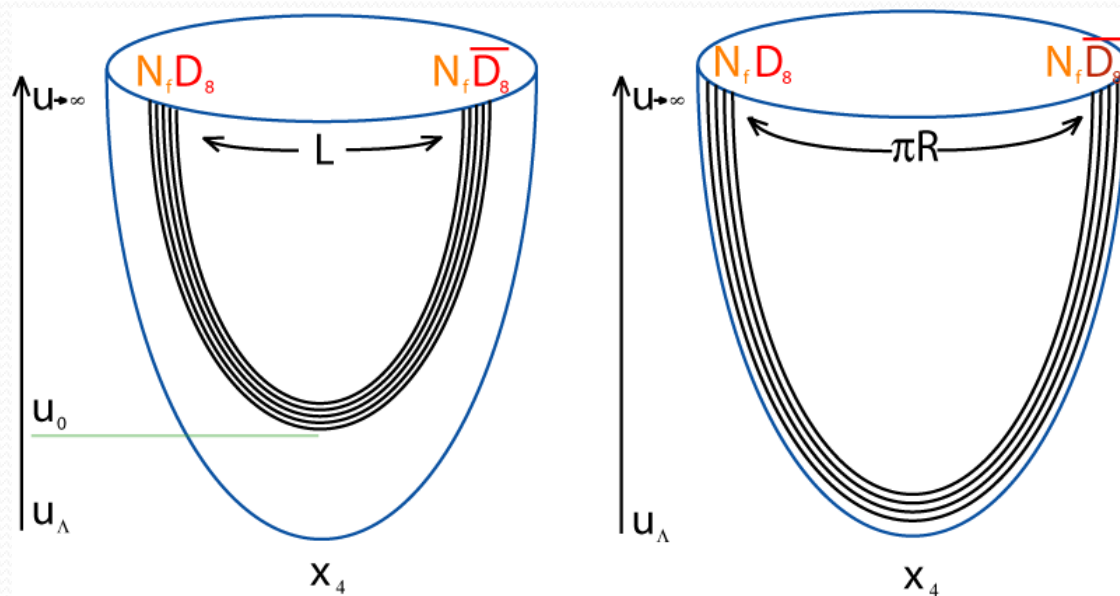
The spin structure of the stringy decays

- The spin structure of allowed decays of doubly charged baryon B^{++} with spin $S = 3/2$ into a baryon and a meson.



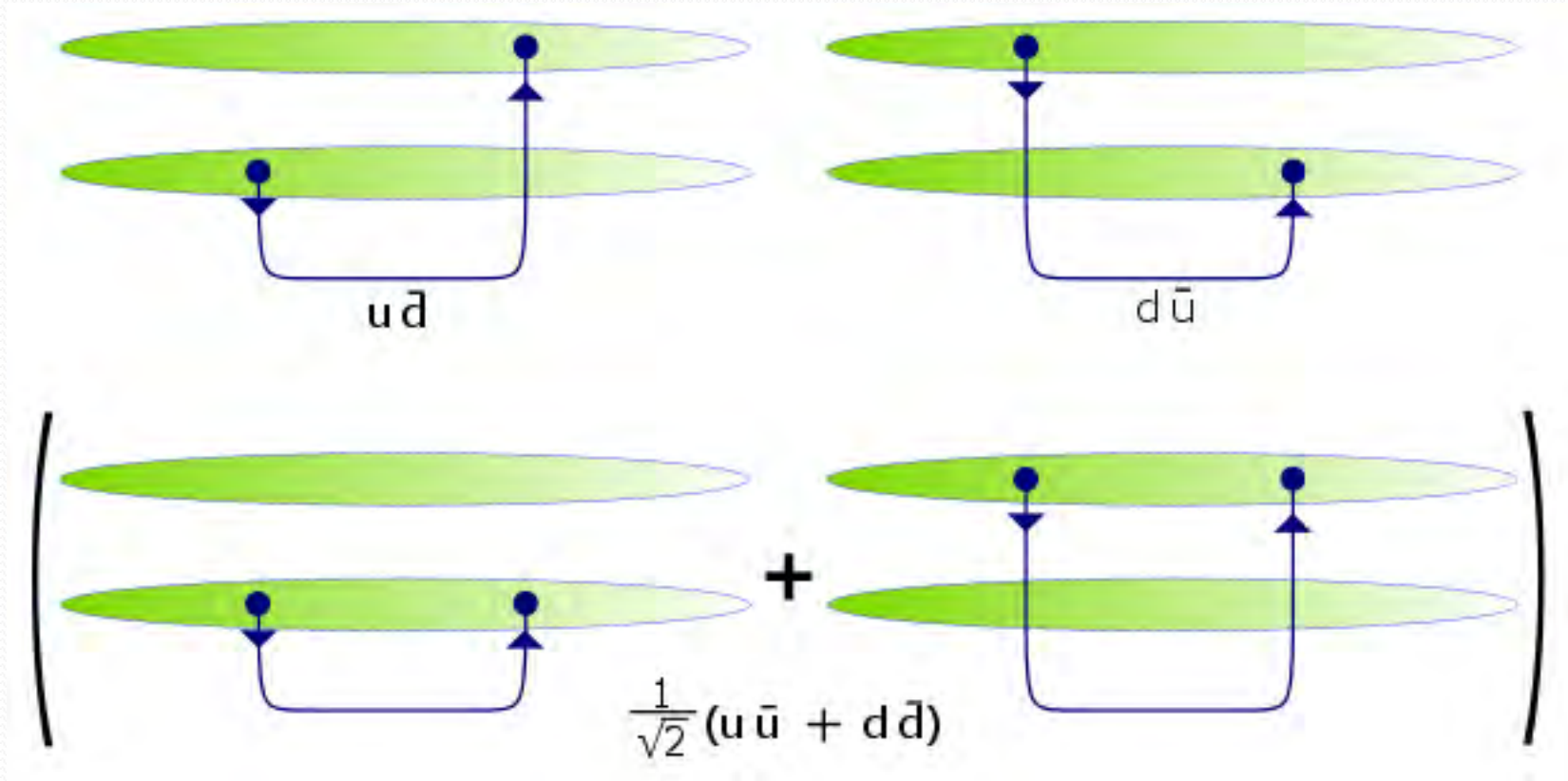
Isospin constraints on decays of stringy mesons

- **Isospin** approximate symmetry is realized in holography by the fact that the u and d flavor branes are **located at roughly the same** holographic radial coordinate.
- The world volume of a stack of N_f coincident flavor branes is characterized by a $U(N_f)$ flavor gauge symmetry.
- In fact we can have $U_L(N_f)U_R(N_f)$ that is geometrically **spontaneously broken** in the IR to $U_D(N_f)$



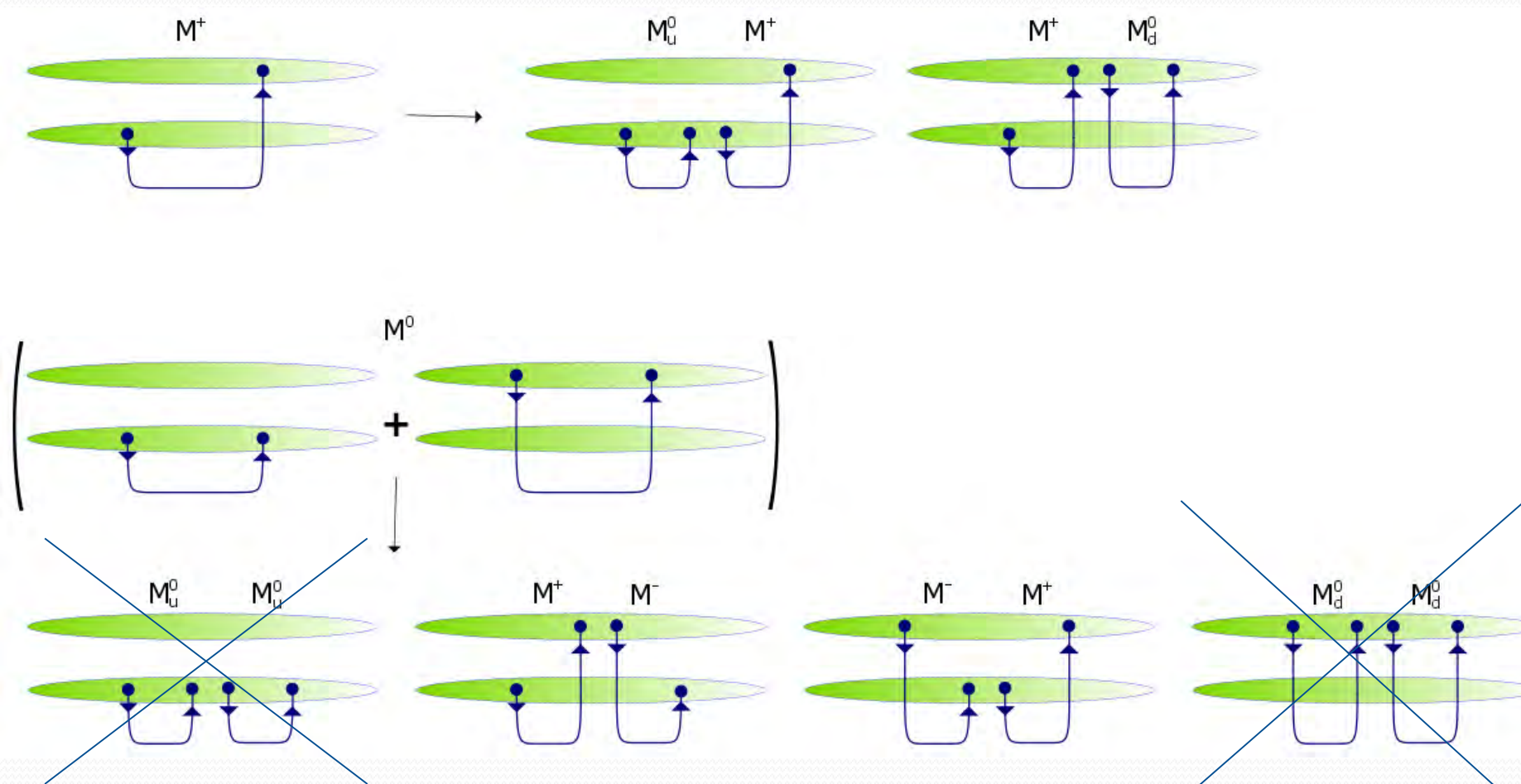
Isospin constraints on decays of stringy mesons

- The stringy mesons of the isospin triplet.



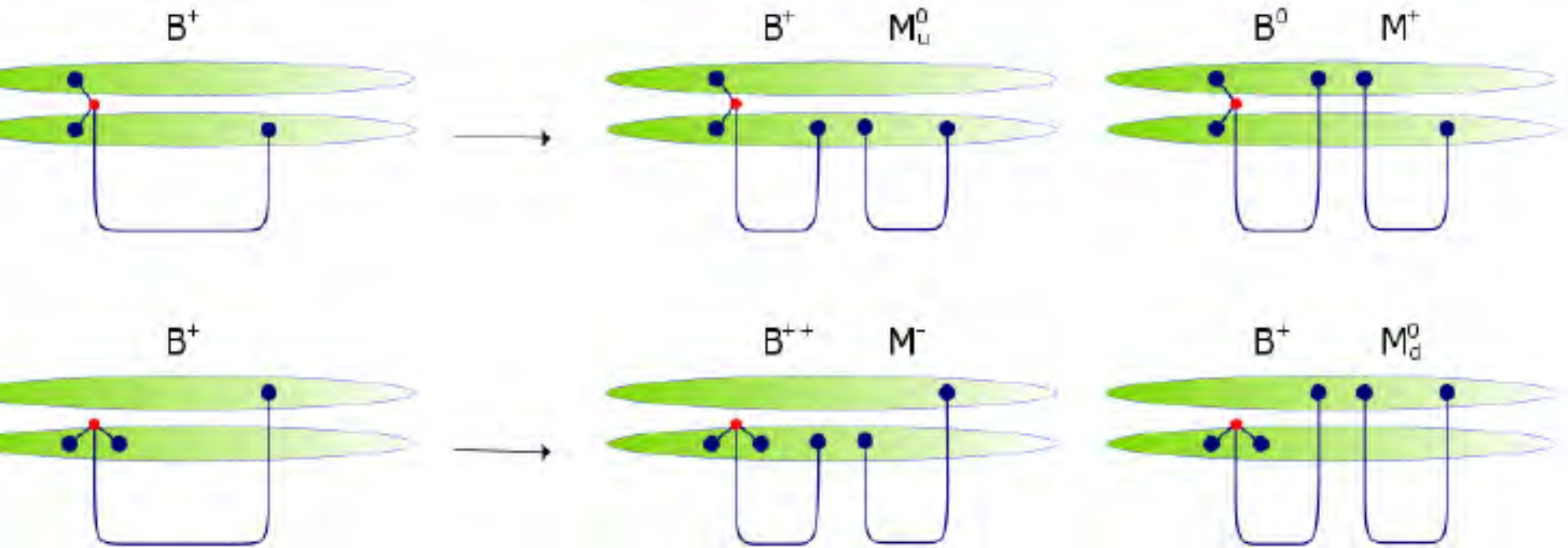
Isospin constraints on decays of stringy mesons

- The decay processes of mesons involve the breaking apart of the horizontal string and the attachment of its endpoints to either the **u** or the **d** flavor branes.



Isospin constraints on decays of stringy baryon

● Possible decays of B^+





Facing experimental data

String length and the phenomenological intercept

- Hadrons admit **modified Regge trajectories** even for **no orbital angular momentum!!**
- This is due to the fact that there is a **quantum length** caused by a **repulsive Casimir force**.

$$F_C = -2a/L^2$$

$$L^2 = L_{cl}^2 + L_0^2$$

- The quantum length is related to the intercept

$$L_0^2 = -C \frac{a}{T}$$

- There are different ways to determine C .
- Our approach is to extract it from the fits.

Check of the linear dependence on L

- Is the **experimental data** admit the **linear dependence on L**

$$\Gamma = \frac{\pi}{2} A T L(M, m_1, m_2, T).$$

- For short strings with important role of the massive endpoints we add a **phase space factor**

$$\Gamma = \frac{\pi}{2} A \times \Phi(M) \times T L(M, m_1, m_2, T).$$

- The phase space factor

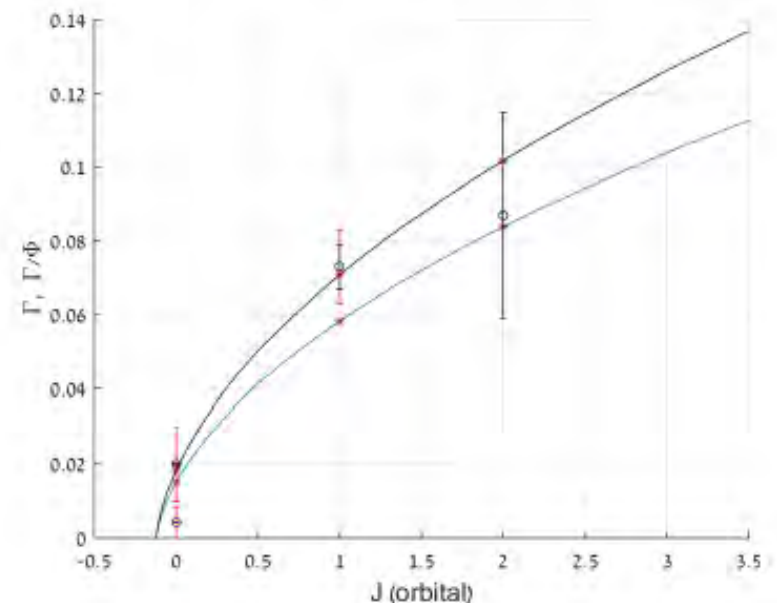
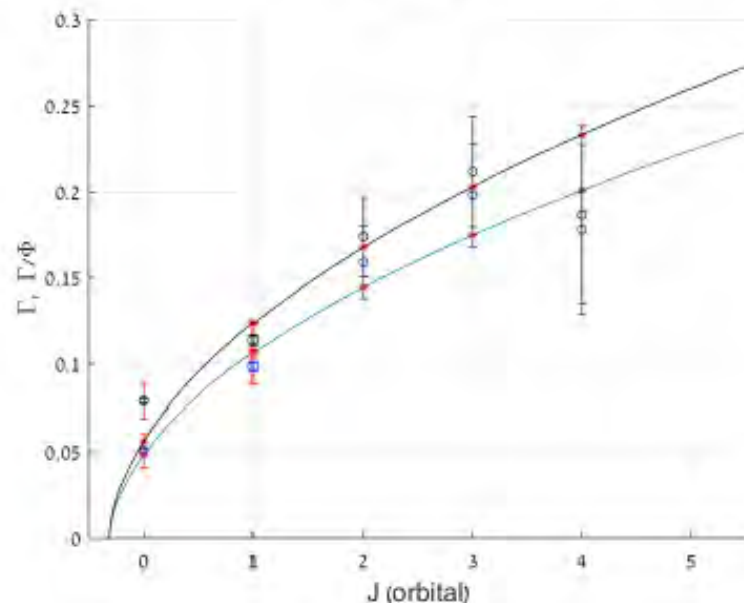
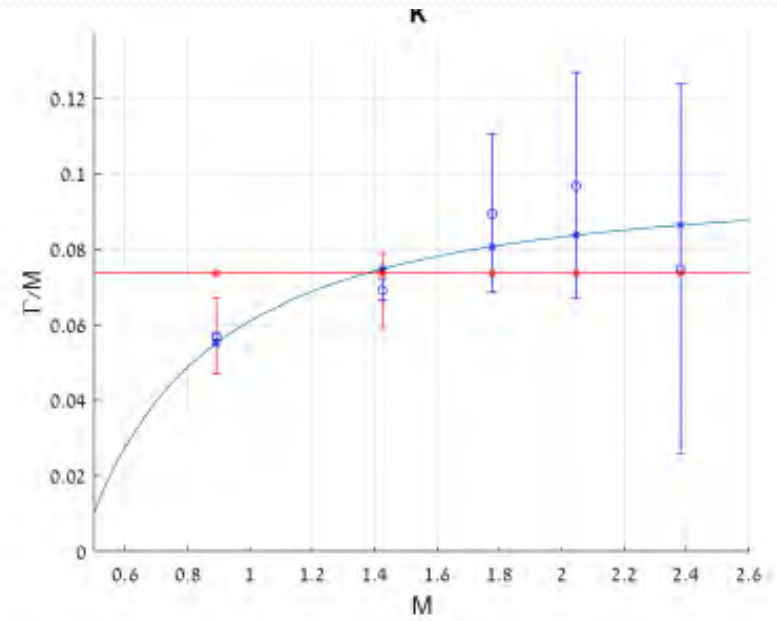
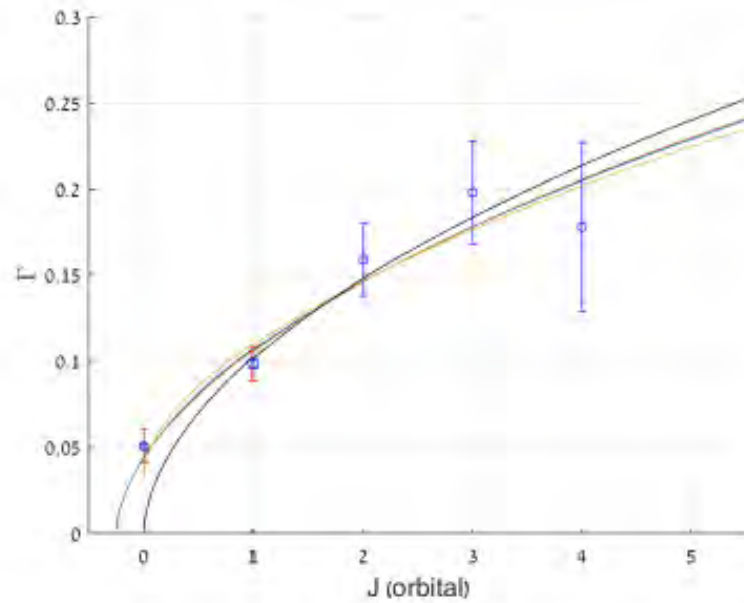
$$\Phi(M, M_1, M_2) \equiv 2 \frac{|p_f|}{M} = \sqrt{\left(1 - \left(\frac{M_1 + M_2}{M}\right)^2\right) \left(1 - \left(\frac{M_1 - M_2}{M}\right)^2\right)}$$

A test case: The K

- We compare our model to the decays of K^* trajectory

State	J^P	Mass	Width	Γ/M	Decay modes ⁴
$K^*(892)$	1^-	891.66 ± 0.26	50.8 ± 0.9	$(5.7 \pm 0.1)\%$	$K\pi$ (100%)
$K_2^*(1430)$	2^+	1425.6 ± 1.5	98.5 ± 2.7	$(6.9 \pm 0.2)\%$	$K\pi$ (50%), $K^*\pi$ (25%), $K^*\pi\pi$ (13%), $K\rho$ (9%), ...
$K_3^*(1780)$	3^-	1776 ± 7	159 ± 21	$(9.0 \pm 1.1)\%$	$K\rho$ (31%), $K^*\pi$ (20%), $K\pi$ (19%), $K\eta$ ($\sim 30\%$), ...
$K_4^*(2045)$	4^+	2045 ± 9	198 ± 30	$(9.7 \pm 1.5)\%$	$K\pi$ (10%), $K^*\pi\pi$ (9%), 5 more modes (7% or less), ...
$K_5^*(2380)$	5^-	2382 ± 24	178 ± 50	$(7.5 \pm 2.1)\%$	$K\pi$ (6%), no other measured modes.

test case: The K

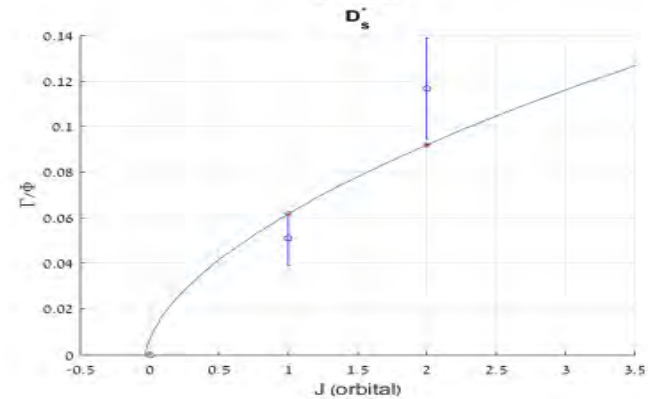
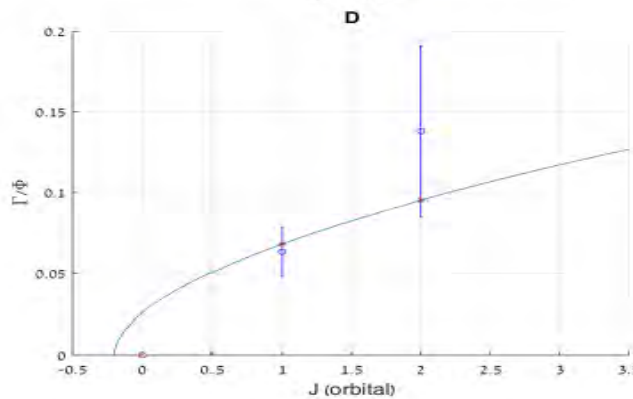
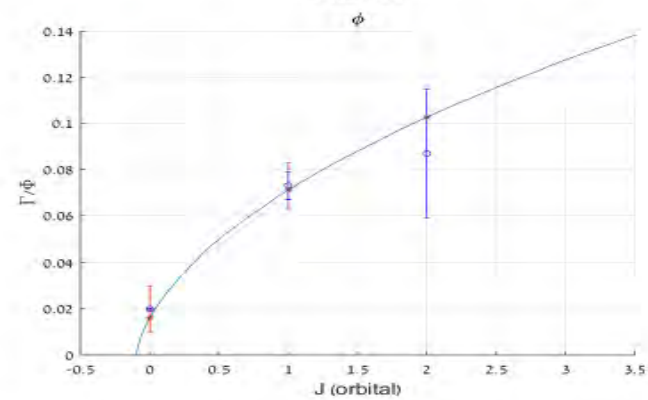
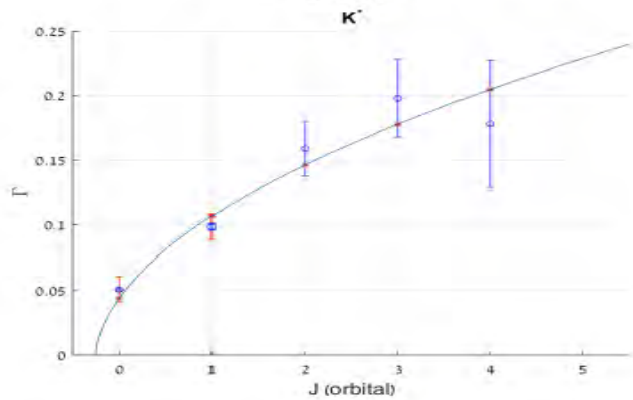
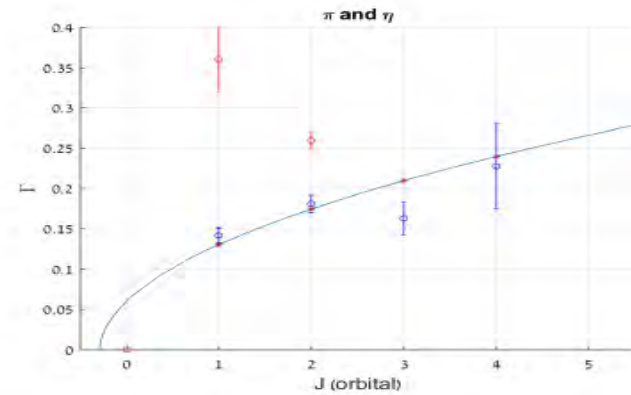
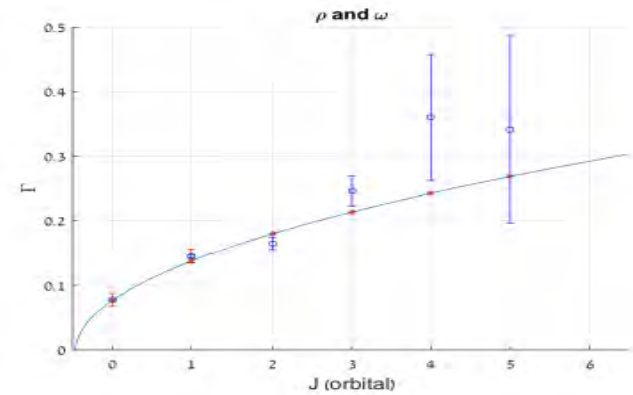


Fit results: the meson trajectories

● Meson fits

Trajectory (No. of states)	a (from spectrum)	A (fitted value)	$\sqrt{\chi^2/DOF}$	
ρ	5 ^[a]	-0.46	0.097	1.76
ω	5 ^[a]	-0.40	0.120	2.31
ρ and ω (avg.)	6	-0.46	0.108	1.14
π	3 ^[a]	-0.34	0.100	1.66
η	3 ^[a]	-0.29	0.108	1.56
π and η (avg.)	4	-0.29	0.109	1.52
K^*	5	-0.25	0.098	0.77
ϕ	3	-0.10	0.074	0.50
D	2	-0.20	0.072	0.87
D_s^*	2	-0.03	0.076	1.44

Fit results: the meson trajectories



The decay width of baryons

- For baryons the linearity with L is somewhat modified.

Trajectory (No. of states)		a (from spectrum)	A (fitted value)	$\sqrt{\chi^2/DC}$
N (even)	2	-0.77	0.080	3.33
N (odd)	3	-1.11	0.082	2.43
Δ (even)	3	-1.37	0.101	1.90
Λ	4	-0.46	0.041	2.33
Σ ($S = 1/2$)	2	-0.95	0.052	0.96
Σ ($S = 3/2$)	3	-1.22	0.100	1.57

Exponential suppression of pair creation

- The **ratio of the decay width** to a strange pair versus to a light quark pair is

$$\lambda_s = \exp\left(-2\pi C(m_s^2 - m_{u/d}^2)/T_{\text{eff}}\right) \approx 0.3$$

Hadron	J^P	Light channel	$s\bar{s}$ channel	Ratio	λ_s
$\rho_3(1690)$	3^-	$\omega\pi$ 16±6%	$K\bar{K}\pi$ 3.8±1.2%	0.24±0.12	0.30±0.15
$K_4^*(2045)$	4^+	$K^*\pi\pi\pi$ 7±5%	ϕK^* 1.4±0.7%	0.20±0.17	0.32±0.28

- In **radiative decays**

$$\frac{\Gamma(J/\Psi \rightarrow \gamma f_2'(1525))}{\Gamma(J/\Psi \rightarrow \gamma f_2(1270))} = 0.31 \pm 0.06, \quad \frac{\Gamma(\Upsilon \rightarrow \gamma f_2'(1525))}{\Gamma(\Upsilon \rightarrow \gamma f_2(1270))} = 0.38 \pm 0.10$$

Zweig suppressed decays and the string length

- The probability of a meson to decay via **annihilation of the quark and antiquark**

$$\Gamma = \Gamma_Z \exp(-T_Z L^2 / 2)$$

- The decays of upsilon

State	Full width [keV]	$B(ggg)$	$B(\gamma gg)$	Partial width [keV]	Best fit [keV]
$\Upsilon(1S)$	54.02 ± 1.25	$81.7 \pm 0.7\%$	$2.2 \pm 0.6\%$	45.3 ± 1.3	45.2
$\Upsilon(2S)$	31.98 ± 2.63	$58.8 \pm 1.2\%$	$1.87 \pm 0.28\%$	19.4 ± 1.7	20.6
$\Upsilon(3S)$	20.32 ± 1.85	$35.7 \pm 2.6\%$	$0.97 \pm 0.18\%$	7.5 ± 0.9	7.1

Summary

- In spite of five decades of research, the story of the strong decays of mesons and baryons has yet not been fully deciphered. **One does not know who to determine the decay width from QCD.**
- We believe, though not in the same strength as for the spectrum, that the decays of hadronic states tell us that indeed **hadrons are strings.**
- This is based on three ingredients:
 - (i) The **linearity relation** between the decay width and the length of the string
 - (ii) The **exponential suppression** factor associated with the creation of a pair that accompanies the breaking of the string into two strings.
 - (iii) The constraints due to **approximated symmetries** like isospin baryon number and flavor $SU(3)$ which are realized in the stringy description

Summary

- In this work we have used two string frameworks
(i) Strings of a **holographic confining** background in critical dimensions (ii) **HISH model** of strings in at four space-time dimensions.
- We saw that the effect of the intercept can be thought of as a **repulsive Casimir force, giving it non-zero length,** and mass and width, even when it is not rotating.
- We found that the **decay coefficient is universal**

$$A = 0.095 \pm 0.015 .$$

- Open questions: **creation mechanisms** of the hadronic states, **Jet formation, scattering amplitudes, weak interactions,** incorporating **leptons.**

Open questions

- Our model assumes **chargeless massive endpoint** particles. The endpoint of a string on a **flavor brane carries a charge** associated with the symmetry group of the flavor branes. Thus it is natural to add an interaction, for instance **EM interaction**, between the two string endpoints.
- It is easy to check that this change will introduce a **classical modification of the intercept**. One can use it to determine the **difference between m_D and m_U**
- **Magnetic moment** and other EM properties can be computed.

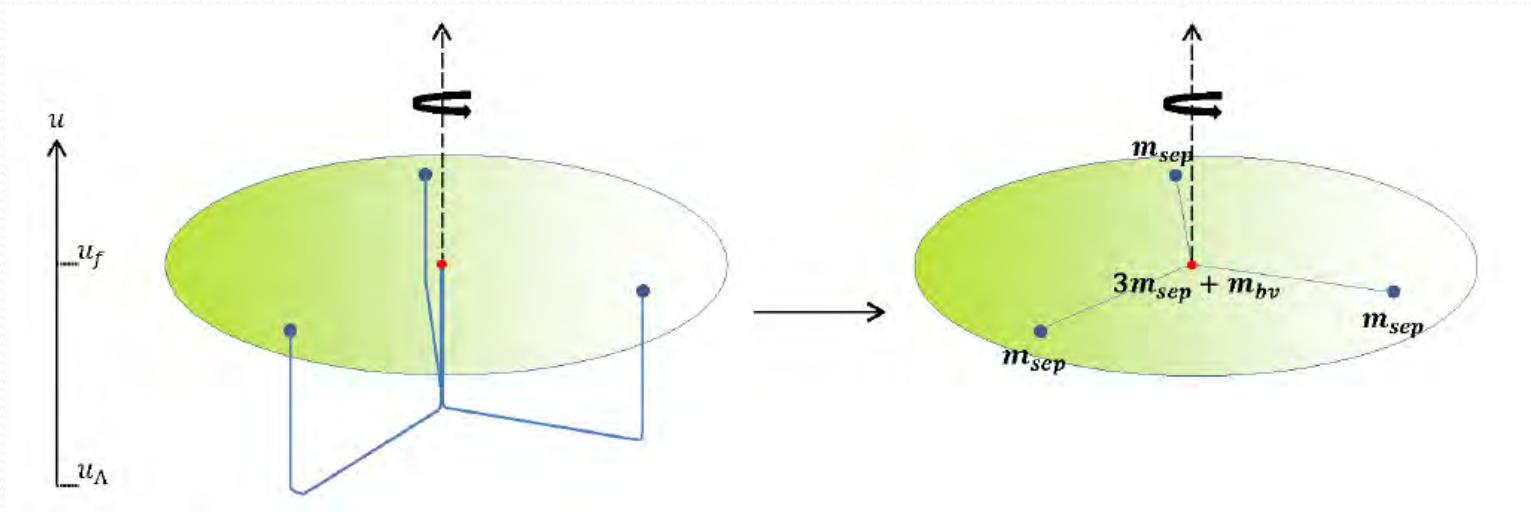
Open Questions

- As was discussed in the introduction, the models we are using are **not the outcome of a full quantization of the system**.
- The quantization of the rotating string without massive endpoints was analyzed. **The quantum Regge trajectories associated with strings with massive endpoints** require determining the contributions to the intercept to order J^0 from both the “Casimir” term and the **Polchinski-Strominger term**.
- Once a determination of the **intercept** as a function of m^2/T is made, an improved **fit** and a re-examination of the **deviations** from a universal model should be made.

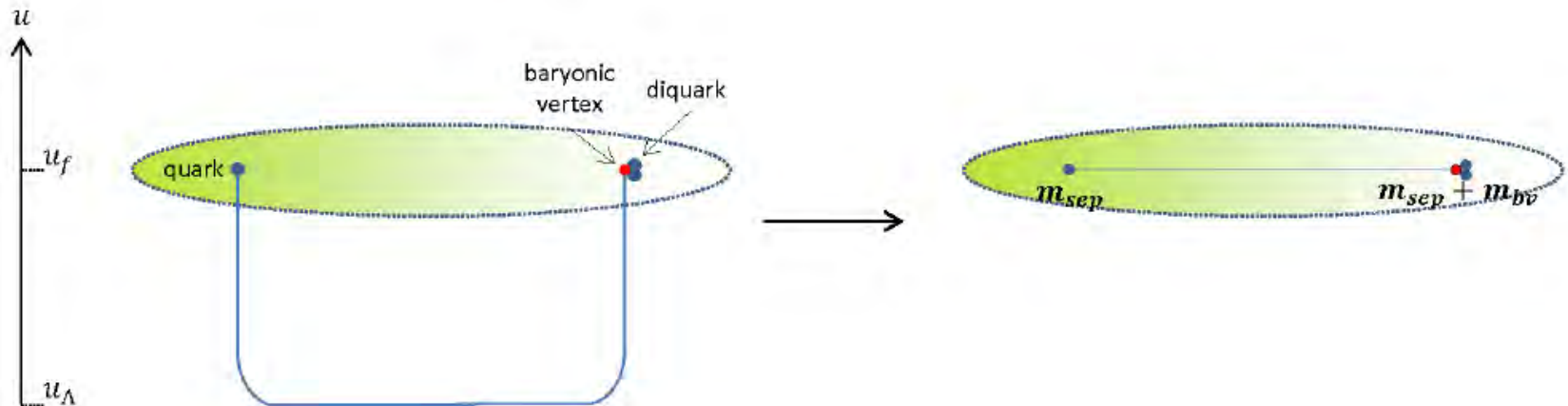
(c) The Λ^0 baryon and its
stability

From holographic to HISH baryons

• The symmetric configuration

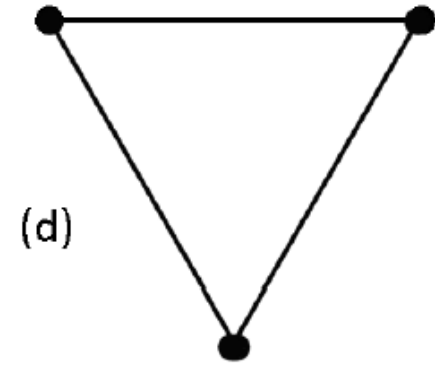
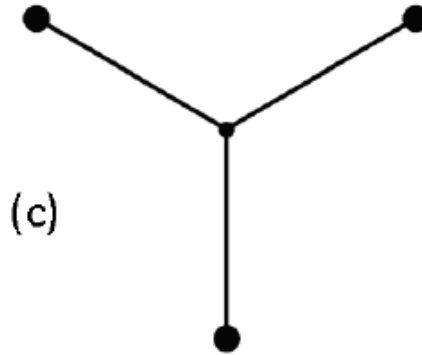
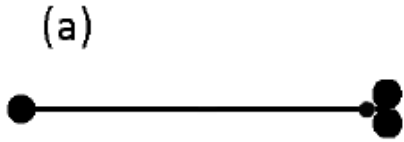


• The asymmetric configuration



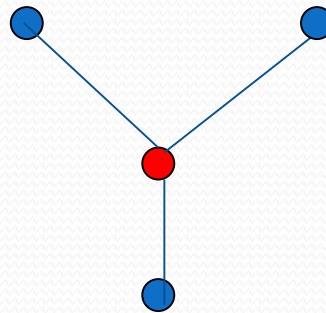
Possible baryon $c=3$ configurations

- A priori for $N_c=3$ there are several possible configurations



From large N_c to three colors

- Naturally the analog at $N_c=3$ of the symmetric configuration with a central baryonic vertex is the old **Y shape baryon**



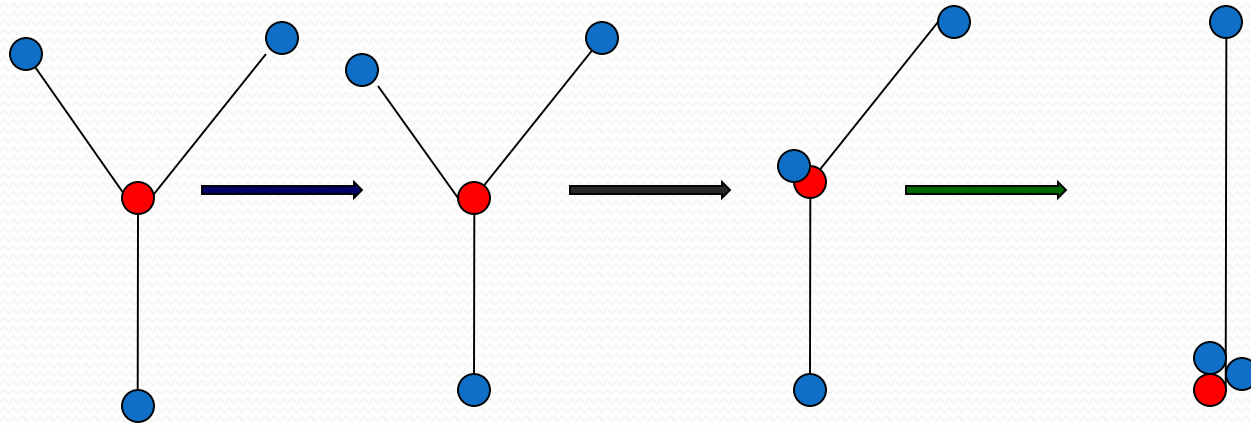
- The analog of the asymmetric setup with one quark on one end and N_c-1 on the other is a **straight string** with quark and a di-quark on its ends.



Stability of an excited baryon

- It was shown that the classical Y shape three string configuration is **unstable**. An arm that is slightly shortened will eventually shrink to zero size.
- We have examined Y shape strings with **massive endpoints** and with a massive **baryonic vertex** in the middle.
- The analysis included **numerical simulations** of the motions of mesons and Y shape baryons under the influence of symmetric and asymmetric disturbance.
- We indeed detected the **instability**
- We also performed a **perturbative analysis** where the instability **does not show up**.

Baryonic instability



The **conclusion** from both the **simulations** and the **qualitative analysis** is that indeed the Y shape string configuration is **unstable** to **asymmetric** deformations.

Thus an excited baryon is an **unbalanced single string** with a **quark** on one side and a **di-quark** and the **baryonic vertex** on the other side.

(d) The #9574 Glueball

The HISH Glueball

- The **map** of the **classical folded rotating closed string** in holographic background to a similar string in four dimensions is simple.
- Unlike the case of the open string here there are no vertical segments involved and correspondingly no **msep**.
- It is just the **string tension** dependence on the **holographic background**
- However, as will be seen in later, the form of the quantum string yields another significant difference
- The relation between the **energy and angular momentum** is modied from the linear Regge trajectory

$$J = \alpha'_{closed}(E - m_0)^2$$

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