



Kolymbari, 5 July 2009

# On mass hierarchies in orientifolds

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# Plan of the talk C

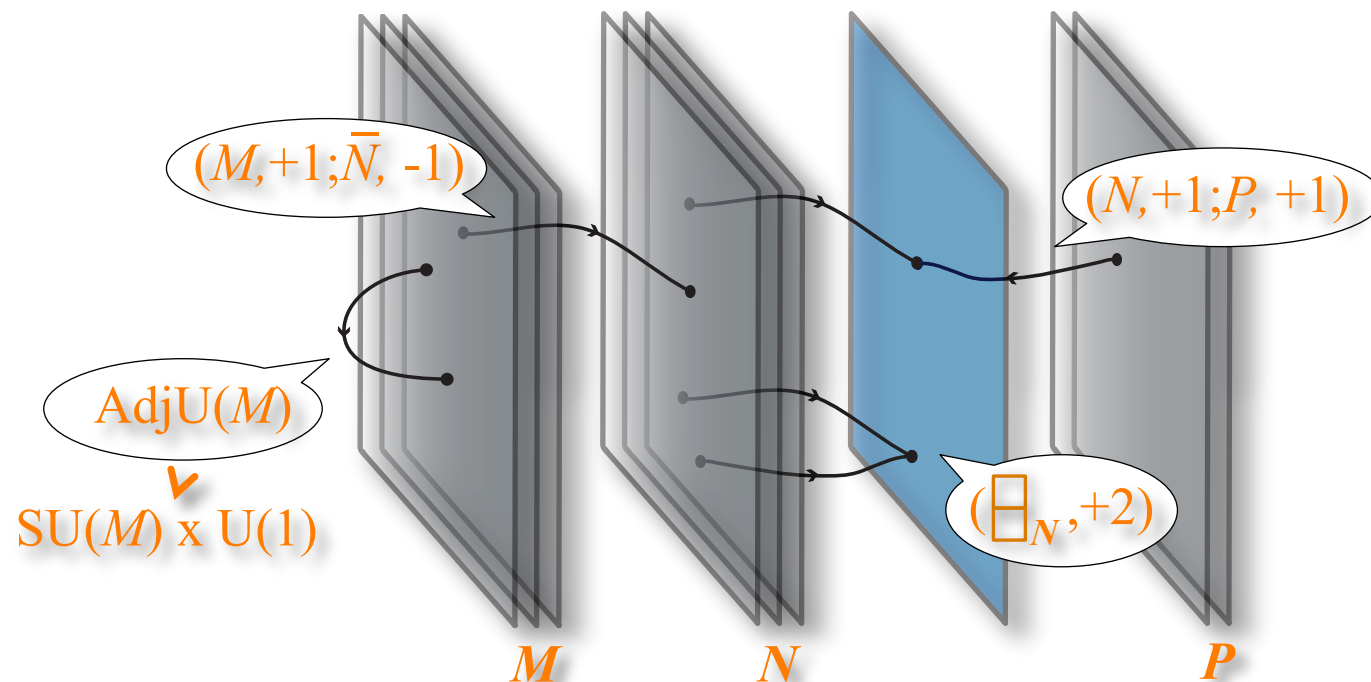
- Introduction and motivation
- D-brane realizations of the Standard Model
- Mass matrix general forms
- An interesting example
- Hierarchies
- Conclusions

# Introduction and Motivation

- One of the **biggest puzzles** of the Standard Model is the **origin** and **hierarchy** of masses and mixings.
  - The **range** of masses between the t-quark and the lightest neutrino spans **15 orders of magnitude!**
  - **Several mechanism** have been proposed to explain (parts of) the mass hierarchy in SM.
- Talk of Leontaris**
- In this talk we want to:
    - investigate the mechanism for the **mass hierarchy** in **open string models** (aka **orientifolds**).
    - To establish the **kind** of the SM embeddings that can accommodate such mechanism.

# Toolkit for Model Building

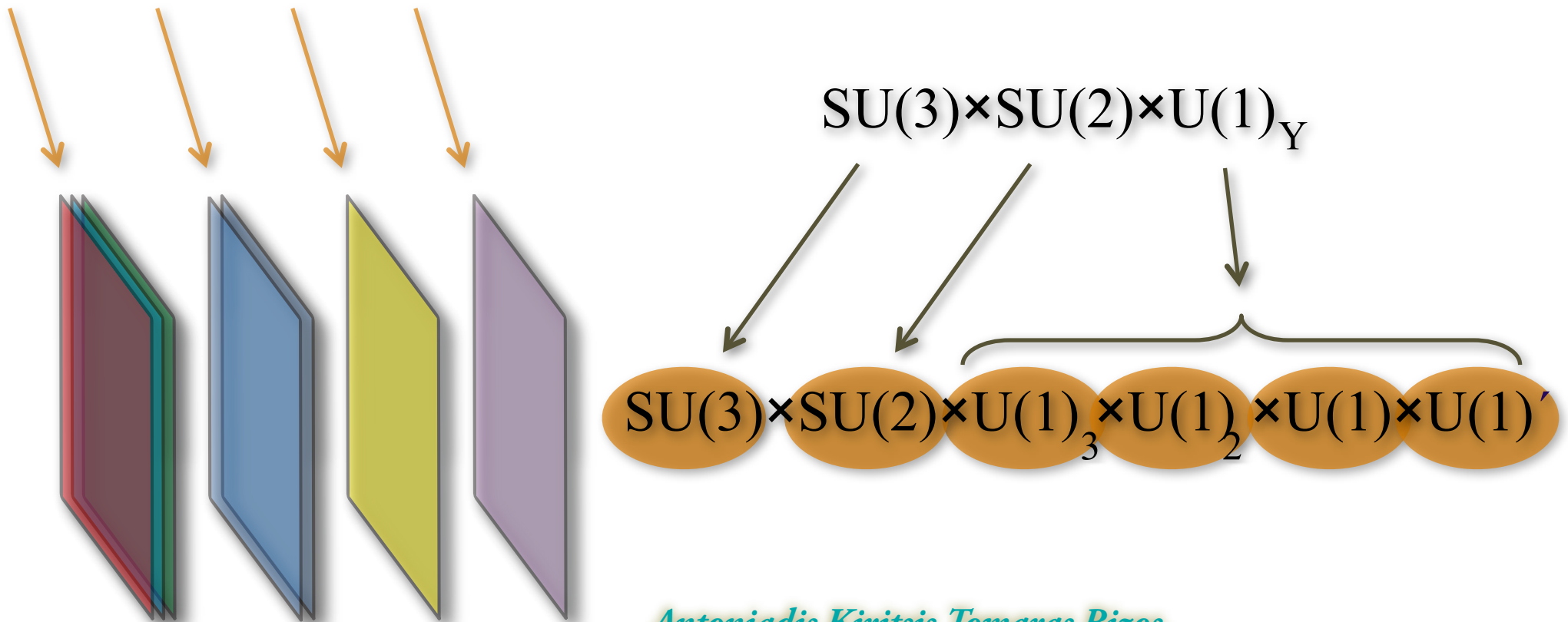
- Gauge Groups and Representations in **Orientifold vacua**:



- By these simple rules we can proceed and try to embed the SM in **open string vacua**.

# D-brane Standard Models

- In open string vacua the **Standard Model** is located on some stacks of branes (intersecting or not):



*Antoniadis Kiritsis Tomaras Rizos,  
Aldazabal Ibanez Marchesano Quevedo Rabadan Uranga,  
Cvetic Shiu Blumenhagen Honecker Kors Lust Ott,  
Anastasopoulos Schellekens Dijkstra Huiszoon et al..*

# Example: The Madrid Model

- All SM particles for  $Y = \frac{1}{6}Q_3 + \frac{1}{2}Q_1 + \frac{1}{2}Q'_1$ :

$$Q : (1, -1, 0, 0) \text{ or } (1, +1, 0, 0)$$

$$U : (-1, 0, -1, 0) \text{ or } (-1, 0, 0, -1)$$

$$D : (-1, 0, +1, 0) \text{ or } (-1, 0, 0, +1)$$

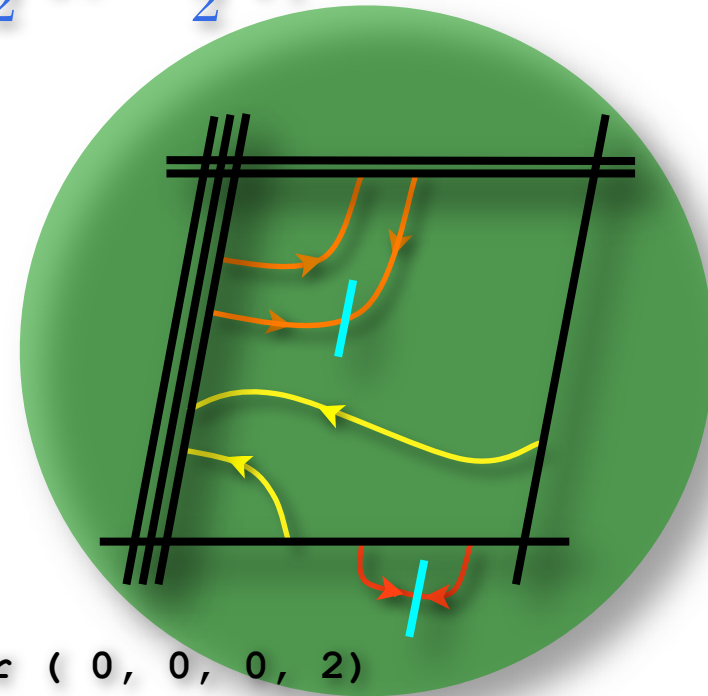
$$L : (0, -1, -1, 0) \text{ or } (0, -1, 0, -1) \\ (0, +1, -1, 0) \text{ or } (0, +1, 0, -1)$$

$$E : (0, 0, 1, 1) \text{ or } (0, 0, 2, 0) \text{ or } (0, 0, 0, 2)$$

$$N^c : (0, 2, 0, 0) \text{ or } (0, 0, 1, -1) \text{ or } (0, 0, -1, 1)$$

$$H_u : (0, -1, +1, 0) \text{ or } (0, -1, 0, +1) \\ (0, +1, +1, 0) \text{ or } (0, +1, 0, +1)$$

$$H_d : (0, -1, -1, 0) \text{ or } (0, -1, 0, -1) \\ (0, +1, -1, 0) \text{ or } (0, +1, 0, -1)$$



*Anastasopoulos Dijkstra  
Kiritsis Schellekens*

- Particles of different families can have different charges.

# Model building

- In the last years, there are **several approaches** towards the search for the Standard Model in String theory.
- However, **non** of them successfully describes **all features** of the SM or MSSM... We are working on this...
- Today, several **new techniques** have been established and can be applied in this task.
- Instead of a blind search, a **better technique** would be to focus in string vacua with some acceptable **phenomenological criteria**.
- In this talk, we will focus on the **mass-terms** and **hierarchy** in such models.

# Masses in D-brane models

- How do fermions get **masses** in D-brane models?
- The usual  $SU(3) \times SU(2) \times U(1)_Y$  is **embedded in** (for example):

$$SU(3) \times SU(2) \times U(1)_3 \times U(1)_2 \times U(1) \times U(1)'$$

- The “mass-terms” in this case should respect **more conditions**.
- This **forbids** several Yukawa terms.
- Could these different terms give an answer to **hierarchy**?

*Leontaris*

*Anastasopoulos Kiritsis Lionetto*

*Cvetic Halverson Richter*



# Yukawa-like terms

- Consider some SM particles to be:

$$Q : (1, -1, 0, 0)$$

$$D_1 : (-1, 0, +1, 0)$$

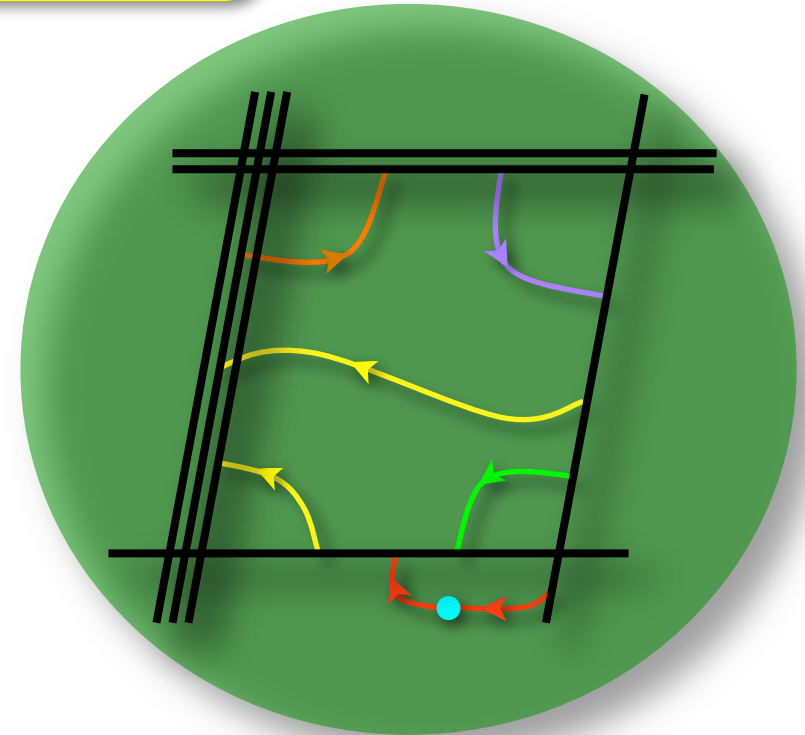
$$D_{2,3} : (-1, 0, 0, +1)$$

$$H_d : (0, 1, -1, 0)$$

$$\phi_1 : (0, 0, 1, -1)$$

$$\phi_2 : (0, 0, -1, 1)$$

$$E_1 : (0, 0, 1, -1)$$



- Yukawa terms:

$$g_i Q D H_d$$

- Higher order terms:

$$g_i Q D H_d \frac{\phi}{M_s}$$

- Instantonic contributions:

$$g_i Q D H_d \times e^{-Vol_{II}}$$

# Yukawa-like terms $\Leftrightarrow$ Textures

- The mass terms can *a priori* be generated by:
  - Yukawa terms:  $g_i Q U H_u \sim \langle H_u \rangle$
  - Higher order terms:  $g_i Q U H_u \frac{\phi}{M_s} \sim \langle H_u \rangle \frac{\langle \phi \rangle}{M_s}$
  - Instantons:  $g_i Q U H_u \times e^{-V^{ol_I I}} \sim \langle H_u \rangle e^{-V^{ol_I I}}$
- Such terms depend on **selection rules** based on the U(1) charges.
- All terms with the **same charges** under the U(1)'s will have the same mass generating terms.

**Talk of Leontaris**
- Therefore, we can make a list of all possible “**orientifold textures**”.

# Quark Textures

- All D-brane realizations of the SM have either:
  - $Q_1 = Q_2 = Q_3$  or  $Q_1 \neq Q_2 = Q_3$
  - $U_1 = U_2 = U_3$  or  $U_1 \neq U_2 = U_3$
  - $D_1 = D_2 = D_3$  or  $D_1 \neq D_2 = D_3$  or  $D_1 \neq D_2 \neq D_3$
- The form of the mass matrix will be:

$$M_1 = \begin{pmatrix} \chi & \chi & \chi \\ \chi & \chi & \chi \\ \chi & \chi & \chi \end{pmatrix}$$

*Anastasopoulos Kiritsis Lionetto*

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  - $U_1 = U_2 = U_3$  or  $U_1 \neq U_2 = U_3$
  - $D_1 = D_2 = D_3$  or  $D_1 \neq D_2 = D_3$  or  $D_1 \neq D_2 \neq D_3$
- The form of the mass matrix will be:

$$M_2 = \left( \begin{array}{c|cc} \mathcal{X} & \mathcal{Y} & \mathcal{Y} \\ \mathcal{X} & \mathcal{Y} & \mathcal{Y} \\ \mathcal{X} & \mathcal{Y} & \mathcal{Y} \end{array} \right) \sim \left( \begin{array}{ccc} \mathcal{X} & \mathcal{X} & \mathcal{X} \\ \mathcal{Y} & \mathcal{Y} & \mathcal{Y} \\ \mathcal{Y} & \mathcal{Y} & \mathcal{Y} \end{array} \right)$$

*Anastasopoulos Kiritsis Lionetto*

# Quark Textures

- All D-brane realizations of the SM have either:
  - $Q_1 = Q_2 = Q_3$  or  $Q_1 \neq Q_2 = Q_3$
  - $U_1 = U_2 = U_3$  or  $U_1 \neq U_2 = U_3$
  - $D_1 = D_2 = D_3$  or  $D_1 \neq D_2 = D_3$  or  $D_1 \neq D_2 \neq D_3$
- The form of the mass matrix will be:

$$M_3 = \left( \begin{array}{c|cc} \mathcal{X} & \mathcal{Y} & \mathcal{Y} \\ \hline \mathcal{Z} & \mathcal{U} & \mathcal{U} \\ \mathcal{Z} & \mathcal{U} & \mathcal{U} \end{array} \right)$$

*Anastasopoulos Kiritsis Lionetto*

# Quark Textures

- All D-brane realizations of the SM have either:
  - $Q_1 = Q_2 = Q_3$  or  $Q_1 \neq Q_2 = Q_3$
  - $U_1 = U_2 = U_3$  or  $U_1 \neq U_2 = U_3$
  - $D_1 = D_2 = D_3$  or  $D_1 \neq D_2 = D_3$  or  $D_1 \neq D_2 \neq D_3$
- The form of the mass matrix will be:

$$M_4 = \left( \begin{array}{c|c|c} \mathcal{X} & \mathcal{Y} & \mathcal{Z} \\ \hline \mathcal{X} & \mathcal{Y} & \mathcal{Z} \\ \hline \mathcal{X} & \mathcal{Y} & \mathcal{Z} \end{array} \right)$$

*Anastasopoulos Kiritsis Lionetto*

# Quark Textures

- All D-brane realizations of the SM have either:

- $Q_1 = Q_2 = Q_3$  or  $Q_1 \neq Q_2 = Q_3$

- $U_1 = U_2 = U_3$  or  $U_1 \neq U_2 = U_3$

- $D_1 = D_2 = D_3$  or  $D_1 \neq D_2 = D_3$  or  $D_1 \neq D_2 \neq D_3$

- The form of the mass matrix will be:

$$M_5 = \begin{pmatrix} x & y & z \\ u & v & w \\ u & v & w \end{pmatrix}$$

*Anastasopoulos Kiritsis Lionetto*

# Lepton Textures

- Similar textures also for the **Lepton** mass matrix:

$$M_1 = \begin{pmatrix} \mathcal{X} & \mathcal{X} & \mathcal{X} \\ \mathcal{X} & \mathcal{X} & \mathcal{X} \\ \mathcal{X} & \mathcal{X} & \mathcal{X} \end{pmatrix}$$

$$M_2 = \begin{pmatrix} \mathcal{X} & \mathcal{Y} & \mathcal{Y} \\ \mathcal{X} & \mathcal{Y} & \mathcal{Y} \\ \mathcal{X} & \mathcal{Y} & \mathcal{Y} \end{pmatrix} \sim \begin{pmatrix} \mathcal{X} & \mathcal{X} & \mathcal{X} \\ \mathcal{Y} & \mathcal{Y} & \mathcal{Y} \\ \mathcal{Y} & \mathcal{Y} & \mathcal{Y} \end{pmatrix}$$

$$M_3 = \begin{pmatrix} \mathcal{X} & \mathcal{Y} & \mathcal{Y} \\ \mathcal{Z} & \mathcal{U} & \mathcal{U} \\ \mathcal{Z} & \mathcal{U} & \mathcal{U} \end{pmatrix}$$

- In this case, there is an extra possibility:

$$M_4 = \begin{pmatrix} \mathcal{X} & \mathcal{Y} & \mathcal{Z} \\ \mathcal{X} & \mathcal{Y} & \mathcal{Z} \\ \mathcal{X} & \mathcal{Y} & \mathcal{Z} \end{pmatrix}$$

$$M_6 = \begin{pmatrix} \mathcal{X} & \mathcal{Y} & \mathcal{Z} \\ \mathcal{U} & \mathcal{V} & \mathcal{W} \\ \mathcal{R} & \mathcal{S} & \mathcal{T} \end{pmatrix}$$

$$M_5 = \begin{pmatrix} \mathcal{X} & \mathcal{Y} & \mathcal{Z} \\ \mathcal{U} & \mathcal{V} & \mathcal{W} \\ \mathcal{U} & \mathcal{V} & \mathcal{W} \end{pmatrix}$$

for  $L_1 \neq L_2 \neq L_3$ ,  $E_1 \neq E_2 \neq E_3$ .



## 8 Madrid type models

- We are interested in bottom-up configurations where in **all mass matrices** appear **Yukawas-** and **Higher-** and **Instantonic-**terms.
- This pluralism might allow for solutions where the **three masses** from each matrix will be in **1-1 correspondence** with the **Yukawas-**, **Higher-** and **Instantonic-**terms.
- Even if that is **not general**, it provides however a general first assessment of D-brane vacua as to their ability to **generate multiple scales** for **masses** and **mixings**.
- Within the “Madrid” class of models we have found **8** charge assignments with a single  $H_u$  and a single  $H_d$ , free of anomalies **with the above property**.

- The MSSM Particles:

$$Q_1 : ( 1, -1, 0, 0 )$$

$$Q_{2,3} : ( 1, +1, 0, 0 )$$

$$U_1 : ( -1, 0, -1, 0 )$$

$$U_{2,3} : ( -1, 0, 0, -1 )$$

$$D_1 : ( -1, 0, 1, 0 )$$

$$D_{2,3} : ( -1, 0, 0, +1 )$$

$$L_{1,2,3} : ( 0, -1, -1, 0 )$$

$$E_1 : ( 0, 0, 2, 0 )$$

$$E_2 : ( 0, 0, 1, 1 )$$

$$E_3 : ( 0, 0, 1, 1 )$$

$$N^c_{1,2,3} : ( 0, 2, 0, 0 )$$

$$H_u : ( 0, 1, 1, 0 )$$

$$H_d : ( 0, 1, -1, 0 )$$

$$\phi_1 : ( 0, 0, -1, +1 )$$

$$\phi_2 : ( 0, 0, +1, -1 )$$

$$E_1 : ( 0, -2, 0, 0 )$$

- The U-quark mass matrix:

$$M_U = V_u \begin{pmatrix} g_1 & g_2 v_{\phi_1} & g_3 v_{\phi_1} \\ g_4 E_1 & g_5 E_2 & g_6 E_2 \\ g_7 E_1 & g_8 E_2 & g_9 E_2 \end{pmatrix}$$

where

$$V_u = \langle H_u \rangle, v_{\phi_i} = \langle \phi_i \rangle / M_s, E_i = e^{-S_i}$$

- The MSSM Particles:

$$Q_1 : ( 1, -1, 0, 0 )$$

$$Q_{2,3} : ( 1, +1, 0, 0 )$$

$$U_1 : ( -1, 0, -1, 0 )$$

$$U_{2,3} : ( -1, 0, 0, -1 )$$

$$D_1 : ( -1, 0, 1, 0 )$$

$$D_{2,3} : ( -1, 0, 0, +1 )$$

$$L_{1,2,3} : ( 0, -1, -1, 0 )$$

$$E_1 : ( 0, 0, 2, 0 )$$

$$E_2 : ( 0, 0, 1, 1 )$$

$$E_3 : ( 0, 0, 1, 1 )$$

$$N_{1,2,3}^c : ( 0, 2, 0, 0 )$$

$$H_u : ( 0, 1, 1, 0 )$$

$$H_d : ( 0, 1, -1, 0 )$$

$$\phi_1 : ( 0, 0, -1, +1 )$$

$$\phi_2 : ( 0, 0, +1, -1 )$$

$$E_1 : ( 0, -2, 0, 0 )$$

- The U-quark mass matrix:

$$M_U = V_u \begin{pmatrix} g_1 & g_2 v_{\phi_1} & g_3 v_{\phi_1} \\ g_4 E_1 & g_5 E_2 & g_6 E_2 \\ g_7 E_1 & g_8 E_2 & g_9 E_2 \end{pmatrix}$$

where

$$V_u = \langle H_u \rangle, v_{\phi_i} = \langle \phi_i \rangle / M_s, E_i = e^{-S_i}$$

- The MSSM Particles:

$$Q_1 : ( 1, -1, 0, 0)$$

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$$U_1 : (-1, 0, -1, 0)$$

$$U_{2,3} : (-1, 0, 0, -1)$$

$$D_1 : (-1, 0, 1, 0)$$

$$D_{2,3} : (-1, 0, 0, +1)$$

$$L_{1,2,3} : ( 0, -1, -1, 0)$$

$$E_1 : ( 0, 0, 2, 0)$$

$$E_2 : ( 0, 0, 1, 1)$$

$$E_3 : ( 0, 0, 1, 1)$$

$$N^c_{1,2,3} : ( 0, 2, 0, 0)$$

$$H_u : ( 0, 1, 1, 0)$$

$$H_d : ( 0, 1, -1, 0)$$

$$\phi_1 : ( 0, 0, -1, +1)$$

$$\phi_2 : ( 0, 0, +1, -1)$$

$$E_1 : ( 0, -2, 0, 0)$$

- The U-quark mass matrix:

$$M_U = V_u \begin{pmatrix} g_1 & g_2 v_{\phi_1} & g_3 v_{\phi_1} \\ g_4 E_1 & g_5 E_2 & g_6 E_2 \\ g_7 E_1 & g_8 E_2 & g_9 E_2 \end{pmatrix}$$

where

$$V_u = \langle H_u \rangle, v_{\phi_i} = \langle \phi_i \rangle / M_s, E_i = e^{-S_i}$$

# All Mass Matrices

- The U-quark, D-quark, Lepton and Neutrino mass matrices:

$$M_U = V_u \begin{pmatrix} g_1 & g_2 v_{\phi_1} & g_3 v_{\phi_1} \\ g_4 E_1 & g_5 E_2 & g_6 E_2 \\ g_7 E_1 & g_8 E_2 & g_9 E_2 \end{pmatrix} \quad M_D = V_d \begin{pmatrix} q_1 & q_2 v_{\phi_2} & q_3 v_{\phi_2} \\ q_4 E_1 & q_5 E_3 & q_6 E_3 \\ q_7 E_1 & q_8 E_3 & q_9 E_3 \end{pmatrix}$$

$$M_L = V_d \begin{pmatrix} l_1 E_4 & l_2 v_{\phi_1} & l_3 \\ l_4 E_4 & l_5 v_{\phi_1} & l_6 \\ l_7 E_4 & l_8 v_{\phi_1} & l_9 \end{pmatrix}$$

$$M_N \sim \begin{pmatrix} 0 & 0 & 0 & V_u E_1 & V_u E_1 & V_u E_1 \\ 0 & 0 & 0 & V_u E_1 & V_u E_1 & V_u E_1 \\ 0 & 0 & 0 & V_u E_1 & V_u E_1 & V_u E_1 \\ V_u E_1 & V_u E_1 & V_u E_1 & M_s E_5 & M_s E_5 & M_s E_5 \\ V_u E_1 & V_u E_1 & V_u E_1 & M_s E_5 & M_s E_5 & M_s E_5 \\ V_u E_1 & V_u E_1 & V_u E_1 & M_s E_5 & M_s E_5 & M_s E_5 \end{pmatrix}$$

# Solving for the Unknowns

- The U-quark mass matrix is:

$$M_U = V_u \begin{pmatrix} g_1 & g_2 v_{\phi_1} & g_3 v_{\phi_1} \\ g_4 E_1 & g_5 E_2 & g_6 E_2 \\ g_7 E_1 & g_8 E_2 & g_9 E_2 \end{pmatrix}$$

- We are looking for solutions where:

$$\begin{aligned} \lambda_1^U &\sim V_u v_{\phi_1} = m_u \\ \lambda_2^U &\sim V_u E_2 = m_c \\ \lambda_3^U &\sim V_u = m_t \end{aligned}$$

in the perturbative regime  $|g_i| \in [0.1 - 0.5]$ .

- This type of solutions could naturally explain the hierarchy in the  $u$ ,  $c$ ,  $t$  quark masses.

# Solutions for all the Unknowns

- An interesting solution for **all** scales (1 TeV,  $10^{15}$  MeV,  $\Lambda_{\text{GUT}}$ ):

$$\begin{array}{ll} V_u \sim m_t, & V_d \sim m_b \\ E_1 \sim E_2 \sim m_c/m_t & E_3 \sim E_4 \sim m_s/m_b \\ v_{\phi_1} \sim m_u/m_t & v_{\phi_2} \sim m_d/m_b \end{array}$$

- The last instanton related to the **Majorana term**:

$$\begin{array}{ll} 1 \text{ TeV scale} & : \quad E_5 \sim 0.654 \\ 10^{15} \text{ MeV scale} & : \quad E_5 \sim 0.754 \\ \Lambda_{\text{GUT}} \text{ scale} & : \quad E_5 \sim 2.5 \times 10^{-7} \end{array}$$

- The **last instanton** appears always as  $E_5 \times M_s$  and initiates the seesaw mechanism.

- The CKM matrix:

$$\text{CKM}(1\text{TeV}) = \begin{pmatrix} 0.970 & 0.240 & 0.007 \\ 0.240 & 0.970 & 0.013 \\ 0.010 & 0.011 & 0.999 \end{pmatrix}$$

$$\begin{array}{ll} V_u \sim m_t, & V_d \sim m_b \\ E_1 \sim E_2 \sim m_c/m_t & E_3 \sim E_4 \sim m_s/m_b \\ v_{\phi_1} \sim m_u/m_t & v_{\phi_2} \sim m_d/m_b \end{array}$$

$$\begin{array}{ll} 1 \text{ TeV scale} & : E_5 \sim 0.654 \\ 10^{15} \text{ MeV scale} & : E_5 \sim 0.754 \\ \Lambda_{\text{GUT}} \text{ scale} & : E_5 \sim 2.5 \times 10^{-7} \end{array}$$

- The mixing-neutrino matrix:

$$U_N = \begin{pmatrix} -0.42 - 0.23i & -0.53 + 0.38i & -0.19 - 0.54i \\ 0.69 - 0.21i & -0.34 + 0.10i & -0.55 + 0.17i \\ 0.20 - 0.44i & 0.65 & -0.16 - 0.55i \end{pmatrix}$$

- Comparing with Data:

$$\text{CKM}(\text{Data}) = \begin{pmatrix} 0.97419 \pm 0.00022 & 0.2257 \pm 0.0010 & 0.00359 \pm 0.00016 \\ 0.2256 \pm 0.0010 & 0.97334 \pm 0.00023 & 0.0415 \pm 0.001 \\ 0.00874^{+0.00026}_{-0.00037} & 0.0407 \pm 0.0010 & 0.999133^{+0.000044}_{-0.000043} \end{pmatrix}$$

- This model could give a natural explanation of the **hierarchy**.



# More/Less D-brane stacks

- The **smaller** is the number of different Yukawa-type terms  $\Rightarrow$   
the **more related** are the mass matrices  $\Rightarrow$   
the **more difficult** is to find the previous hierarchical solutions.
- Therefore, it is easy to show that in:
  - **3-stacks models**: **No** such solutions.
  - **4-stacks models**: Only **few** such solutions (Madrid).
  - **5-stacks (or more) models**: **More** solutions are expected/found...

# “Bad” terms

- A bonus: undesired terms could be absent due to the extended symmetries.
- So, apart from the mass terms, some extra terms could be present:

$H_u H_d$ ,  $QDL$ ,  $DDU$ ,  $LEL$ ,  $H_u H_d \nu$ ,  $H_d E H_d$ ,  $\nu\nu\nu$

- However, now they can be present due to instantonic effect.
- There are non-dangerous and dangerous terms (for small  $M_s$ ).
- All 8 bottom-up models have no dangerous terms.

# Conclusions

- **Open string textures** are different from the traditional ones.
- **Yukawa-, Higher- and Instantonic-**terms can generate the full hierarchy of the Standard Model: From the **t-quark** down to **neutrinos**.
- **Undesired terms** can be **eliminated** without problems due to the extended additional  $U(1)$  symmetries.
- Search for **optimal embeddings** in consistent orientifolds (with cancelled tadpoles) is very interesting (and in progress).