

# New susy type II $\text{AdS}_4$ vacua

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*Κολυμπάρι, Κρήτη*

# Outline

- 1 Introduction
  - Motivation
  - The result
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- 2 General Description of  $\text{AdS}_4 \times_w \mathcal{M}_6$ 
  - $\text{SU}(3)$  structure
  - $\text{SU}(3) \times \text{SU}(3)$  structure
- 3 New  $\text{AdS}_4$  vacua
  - Overview
  - Type IIA
  - Type IIB
- 4 Conclusions
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# Motivation

## AdS<sub>4</sub>/CFT<sub>3</sub> duality

- Nonperturbative definition of String Theory
- Multiple M2 branes

## Deviation from CY-ness

- Flux  $\neq 0 \implies \text{AdS}_4 \times_w \mathcal{M}_6$

## Flux Vacua

- Moduli stabilization
- Starting point for de Sitter
- Susy breaking, ...

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# The result

- New  $\mathcal{N} = 2$  IIA and  $\mathcal{N} = 1$  IIB pure-flux vacua

## Ten-dimensional spacetime

$\text{AdS}_4 \times_w \mathcal{M}_6$  with:

$$ds^2(\mathcal{M}_6) = dt^2 + ds_t^2(\mathcal{M}_5)$$

where  $\mathcal{M}_5$  admits a Sasaki-Einstein structure

$$ds_t^2(\mathcal{M}_5) = e^{2B(t)} ds_{KE}^2 + \xi^2(t)(d\psi + A)^2$$



Lüst, DT, JHEP 0904



Lüst, DT, arXiv:0906

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Lüst, DT, JHEP 0904



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# Outline

- $\text{AdS}_4 \times \mathcal{M}_6$  vacua: generalities
- New explicit vacua

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# SU(3) structure

Flux = 0,  $\mathcal{M}_6 = \text{CY}$

- SUSY:  $\nabla\eta = 0$
- Bilinears:  $J_{mn} := \eta^\dagger \gamma_{mn} \eta$ ;  $\Omega_{mnp} := \eta \gamma_{mnp} \eta$
- Differential conditions:  $d\Omega = 0$ ;  $dJ = 0$

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# SU(3) structure

[hep-th]

$(\eta, g_{mn})$

# SU(3) structure

[math.DG]

$(J, \Omega)$

# SU(3) structure

## Definition

$$\Omega \wedge \bar{\Omega} = \frac{1}{3!} J^3$$

$$J \wedge \Omega = 0$$

$$Sp(6, \mathbb{R}) \cap SL(3, \mathbb{C}) = SU(3)$$

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# Spinor ansatz

## Two susy parameters

$$\epsilon_i = \zeta \otimes \theta_i + \text{c.c.}; \quad i = 1, 2$$

$$|\theta_1|^2 = |\theta_2|^2 \propto e^A$$

## Two unimodular spinors

$$\theta_1 = a \eta_1; \quad \theta_2 = \begin{cases} b \eta_2^* + c^* \eta_1^* & \text{IIA} \\ b \eta_2 + c \eta_1 & \text{IIB} \end{cases}$$

$$a^2 = b^2 + |c|^2$$

# $\text{SU}(3) \times \text{SU}(3)$ structure

## Local $\text{SU}(2) = \text{SU}(3) \cap \text{SU}(3)$ structure

$$\tilde{J} \wedge \omega = 0$$

$$2\tilde{J} \wedge \tilde{J} = \omega \wedge \omega^* \neq 0$$

$$\iota_K \tilde{J} = \iota_K \text{Re} \omega = \iota_K \text{Im} \omega = 0$$

## $\text{SU}(3) \times \text{SU}(3)$ structure

$$J^{(1)} = \frac{i}{2} K \wedge K^* + \tilde{J}; \quad J^{(2)} = \frac{i}{2} K \wedge K^* - \tilde{J}$$

$$\Omega^{(1)} = -i\omega \wedge K; \quad \Omega^{(2)} = i\omega^* \wedge K$$

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# The scalar ansatz

Provided certain conditions are obeyed by  $(K, \tilde{J}, \omega)$   
the scalar ansatz solves the **susy** equations of **IIA/IIB**

 Lüst, DT, JHEP 0904

# The scalar ansatz

## Metric

$$ds^2 = e^{2A} ds^2(AdS_4) + ds^2(\mathcal{M}_6)$$

## Three-form

$$H = \frac{1}{24} \left( h_1 \omega^* + h_2 \omega + 2h_3 \tilde{J} \right) \wedge K + \text{c.c.}$$

# The scalar ansatz

## RR fluxes IIA

$$e^\phi F_0 = f_0$$

$$e^\phi F_2 = \frac{1}{8} \left( f_2 \omega^* + f_3 \tilde{\mathbf{J}} + 2if_1 K \wedge K^* \right) + \text{c.c.}$$

$$e^\phi F_4 = \frac{1}{16} g_1 \tilde{\mathbf{J}} \wedge \tilde{\mathbf{J}} + \frac{i}{96} \left( g_2 \omega^* + g_2^* \omega + 2g_3 \tilde{\mathbf{J}} \right) \wedge K \wedge K^*$$

$$e^\phi F_6 = f \text{vol}_6$$

# The scalar ansatz

## RR fluxes IIB

$$e^\phi F_1 = g_1 K + \text{c.c.}$$

$$e^\phi F_3 = \frac{1}{24} \left( f_1 \omega^* + f_2 \omega + 2f_3 \tilde{J} \right) \wedge K + \text{c.c.}$$

$$e^\phi F_5 = g_2 \star_6 K + \text{c.c.}$$

# Equations of motion

- SUSY $\oplus$ (generalized) Bianchi ids  $\implies$  All EOM's
- Also in the presence of **calibrated** sources



Koerber, DT, JHEP 0708

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# Construction of vacua

## IIA Strict $\text{SU}(3)$

- Until recently all known (massive) vacua were of rigid- $\text{SU}(3)$  type
- All can be described in a unifying framework: left-invariant  $\text{SU}(3)$  structures on groups, cosets
- Many more should be possible!



Lüst, DT, JHEP 0502



Koerber, Lüst, DT, JHEP 0807

# Explicit vacua

## IIA Strict SU(3)

-  Nilsson, Pope, CQG 1984
-  Sorokin, Tkach, Volkov PLB 1985
-  Behrndt, Cvetič, NPB 2005
-  Lüst, DT, JHEP 0502
-  Graña, Minasian, Petrini, Tomasiello JHEP 0705
-  Aldazabal, Font, JHEP 0802
-  Tomasiello, hep-th 0712
-  Koerber, Lüst, DT, JHEP 0807

# Explicit vacua

## IIA $SU(3) \times SU(3)$



Gaiotto, Tomasiello, arXiv:0904



Petrini, Zaffaroni, arXiv:0904



Lüst, DT, arXiv:0906

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# New $\mathcal{N} = 2$ IIA vacua

$\mathcal{M}_5$  admits a S-E  $\text{SU}(2)$  structure

$$\iota_u \alpha = \iota_u \beta = \iota_u \gamma = 0$$

$$\alpha \wedge \beta = \beta \wedge \gamma = \gamma \wedge \alpha = 0$$

$$\alpha \wedge \alpha = \beta \wedge \beta = \gamma \wedge \gamma \neq 0$$

$$du = -2\gamma; \quad d(\alpha + i\beta) = -3iu \wedge (\alpha + i\beta); \quad d\gamma = 0$$

# 5d Sasaki-Einstein

## Killing spinor

$$\nabla_m \eta = \pm \frac{i}{2} \Gamma_m \eta$$

$$R_{mn} = 4g_{mn}$$

## The $\text{SU}(2)$ structure

$$u_m := (\eta^\dagger \Gamma_m \eta)$$

$$\alpha_{mn} + i\beta_{mn} := (\eta \Gamma_{mn} \eta)$$

$$\gamma_{mn} := i(\eta^\dagger \Gamma_{mn} \eta)$$

# New $\mathcal{N} = 2$ IIA vacua

## Local $\text{SU}(2)$ structure

$$K = e^{B(t)} (dt - i\xi(t)u)$$

$$\begin{pmatrix} \tilde{J} \\ \text{Re}\omega \\ \text{Im}\omega \end{pmatrix} = e^{2C(t)} \mathcal{R}(\theta(t), \chi(t)) \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}$$

## Metric on $\mathcal{M}_6$

$$ds^2(\mathcal{M}_6) = e^{2B} \left( \frac{3}{W} e^{2(C-B)} ds_{KE}^2 + \xi^2 u \otimes u + dt^2 \right)$$

- $\mathcal{M}_6$  is locally a smooth  $S^2$  bundle over 4D K-E base.

# New $\mathcal{N} = 2$ IIA vacua

- All conditions of the scalar ansatz are satisfied
- All BI's and EOM's are satisfied
- All fields are determined

## The solution

$$\tan \theta = \frac{\tan \varphi}{\sin \varepsilon} = \sqrt{2} \tan(\sqrt{2}t)$$

$$f = -3We^{-A} \cos \varepsilon \cos \varphi$$

$$f_0 = -We^{-A} (\cos \varphi \sin \varepsilon + \csc \varepsilon \sin \varphi \tan \varphi)$$

$$f_1 = -\cos \varepsilon \cos \varphi \left( We^{-A} + 4e^{-B} A' \cot \varphi \sin \varepsilon \right)$$

$$f_2 = -8e^{-B} A' \cos \varepsilon \cos \varphi$$

# New $\mathcal{N} = 2$ IIA vacua

- All conditions of the scalar ansatz are satisfied
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## The solution

$$g_1 = -8 (\cos \varphi \sin \varepsilon + \sin \varphi \csc \varepsilon \tan \varphi) \\ \left( We^{-A} - 4e^{-B} A' \cot \varphi \sin \varepsilon \right)$$

$$g_2 = 48 \sin \varphi \left( We^{-A} + e^{-B} A' \cot \varphi \sin \varepsilon \right)$$

$$h_1 = -6 \sin^2 \varphi \cot \varepsilon \left( We^{-A} - 2e^{-B} A' \sin \varepsilon \cot \varphi \right)$$

$$\frac{h_1}{h_3} = \frac{h_2}{h_3} = \frac{f_2}{f_3} = \frac{g_2}{g_3} = -\tan \theta .$$

# New $\mathcal{N} = 2$ IIA vacua

- All conditions of the scalar ansatz are satisfied
- All BI's and EOM's are satisfied
- All fields are determined

## The solution

$$e^{4A} = \frac{1}{\cos^2 \theta} \tan \varepsilon$$

$$e^{B-A} = -\frac{1}{2W} \cot \theta (\log \tan \varepsilon)'$$

$$e^{\phi-3A} = \cos \varphi \cos \varepsilon$$

$$\xi = \frac{3}{2W} e^{A-B} \sin \theta$$

# New $\mathcal{N} = 2$ IIA vacua

- All conditions of the scalar ansatz are satisfied
- All BI's and EOM's are satisfied
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## The solution

$$\begin{aligned}\zeta' &= \frac{1}{2W} e^{2(A-C)} \cos \theta \cot \varepsilon \sin^2 \varphi (\log \tan \varepsilon)' \\ \theta' &= \cot \theta \left( \frac{1}{2W} e^{2(A-C)} \sin^2 \theta - 1 \right) (\log \tan \varepsilon)' \\ C' &= -\frac{1}{4W} e^{2(A-C)} (\sin^2 \varphi + \cos^2 \theta) (\log \tan \varepsilon)'\end{aligned}$$

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# New susy IIB vacua

## Local SU(2) structure

$$K = e^{A(t)} (idt - 3u)$$

$$\begin{pmatrix} \tilde{J} \\ \text{Re}\omega \\ \text{Im}\omega \end{pmatrix} = e^{2A(t)} \mathcal{R}(\theta(t)) \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix}$$

## Metric on $\mathcal{M}_6$

$$ds_E^2 = ds^2(AdS_4) + \frac{6}{5W^2} ds_{KE}^2 + 9u \otimes u + dt^2$$

- $\mathcal{M}_6$  is the product of squashed 5D S-E and  $S^1$  or  $\mathbb{R}$ .

# New susy IIB vacua

- All conditions of the scalar ansatz are satisfied
- All BI's and EOM's are satisfied
- All fields are determined

## The solution

$$H = \frac{1}{2} W \text{Re} w \wedge dt - \left( 2A' \tilde{J} + c e^{-4A} \text{Re} w \right) \wedge u$$

$$e^\phi F_1 = -2c e^{-4A} dt$$

$$e^\phi F_3 = -\frac{1}{2} W \tilde{J} \wedge dt + \left( 2A' \text{Re} w - c e^{-4A} \tilde{J} \right) \wedge u$$

$$e^\phi F_5 = \frac{3}{2} W \tilde{J} \wedge \tilde{J} \wedge u$$

# New susy IIB vacua

- All conditions of the scalar ansatz are satisfied
- All BI's and EOM's are satisfied
- All fields are determined

## The solution

$$\phi = 4A$$

$$e^\phi = \begin{cases} \frac{2}{\sqrt{5}} \left| \frac{c}{W} \right| \cosh [\sqrt{5} W(t - t_0)] , & c \neq 0 \\ \exp [\sqrt{5} W(t - t_0)] , & c = 0 \end{cases}$$

$$\tan(\theta - \theta_0) = \begin{cases} \tanh \left[ \frac{\sqrt{5}}{2} W(t - t_0) \right] , & c \neq 0 \\ 0 , & c = 0 \end{cases}$$

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# Conclusions

## Summary

- Given any 5D S-E manifold we have constructed corresponding families of new explicit IIA/IIB  $\text{AdS}_4$  vacua
- Infinite number of families
- Pure flux
- Given any 4D K-E manifold we have constructed corresponding families of vacua

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# Conclusions

## Open problems

- Implications for  $\text{AdS}_4/\text{CFT}_3$   
(specific models)
- Many more vacua?  $\mathcal{N}=3$ ?  
(more  $\text{CFT}_3$ 's than  $\text{AdS}_4$ 's)
- General properties of flux vacua?
- Phenomenological applications

Thank You