

# Possible Imprints of the Overshoot Problem

Sunny Itzhaki

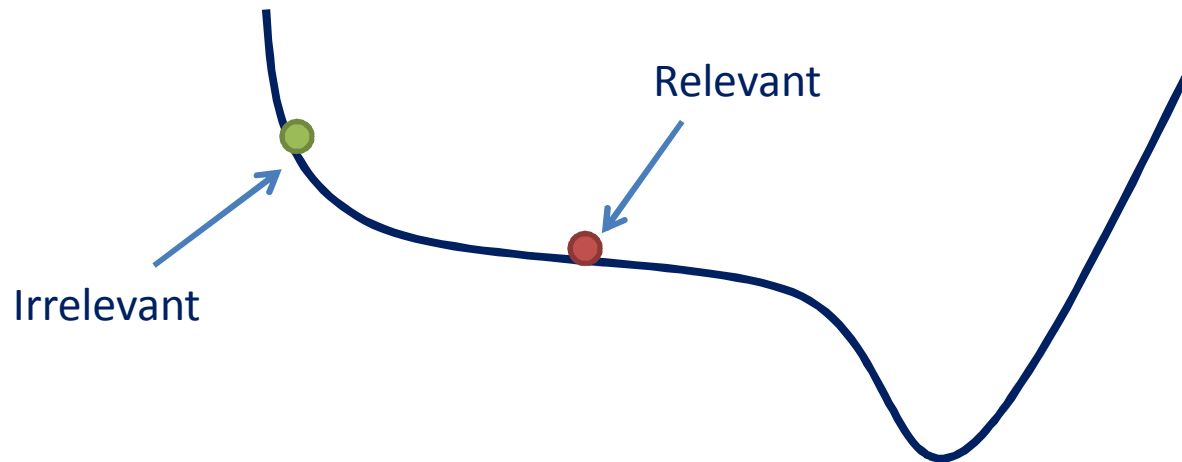
Based on:

0807.3216

A. Fialkov, N.I and E. Kovetz to appear

The basic feature of inflation is that it erases (exponentially fast) all details of the pre-inflationary period:

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The attractor mechanism makes sure that ● doesn't depend on ● .

This is the main reason why precise predictions can be made despite the fact that we don't know the initial state ● .

The parameter that controls how precise this statement is :

$$x = \exp(-\Delta N)$$

where

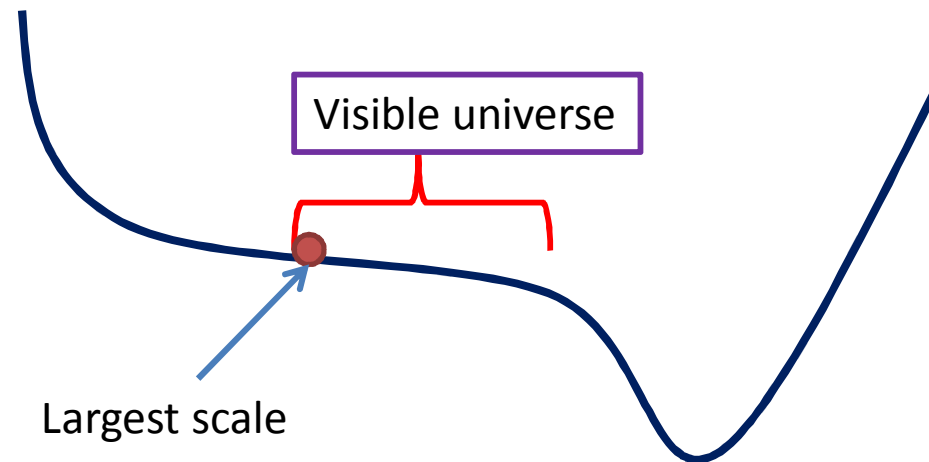
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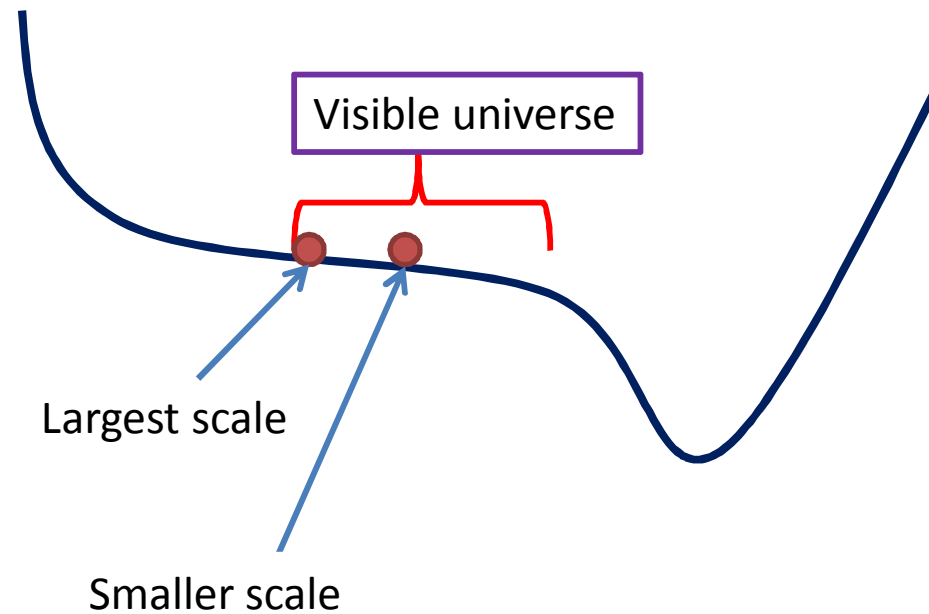


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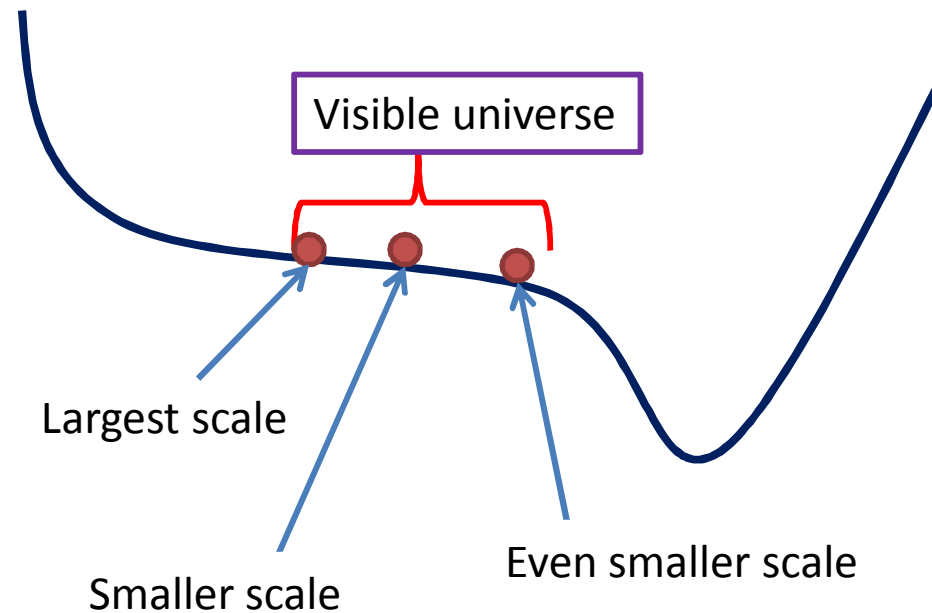


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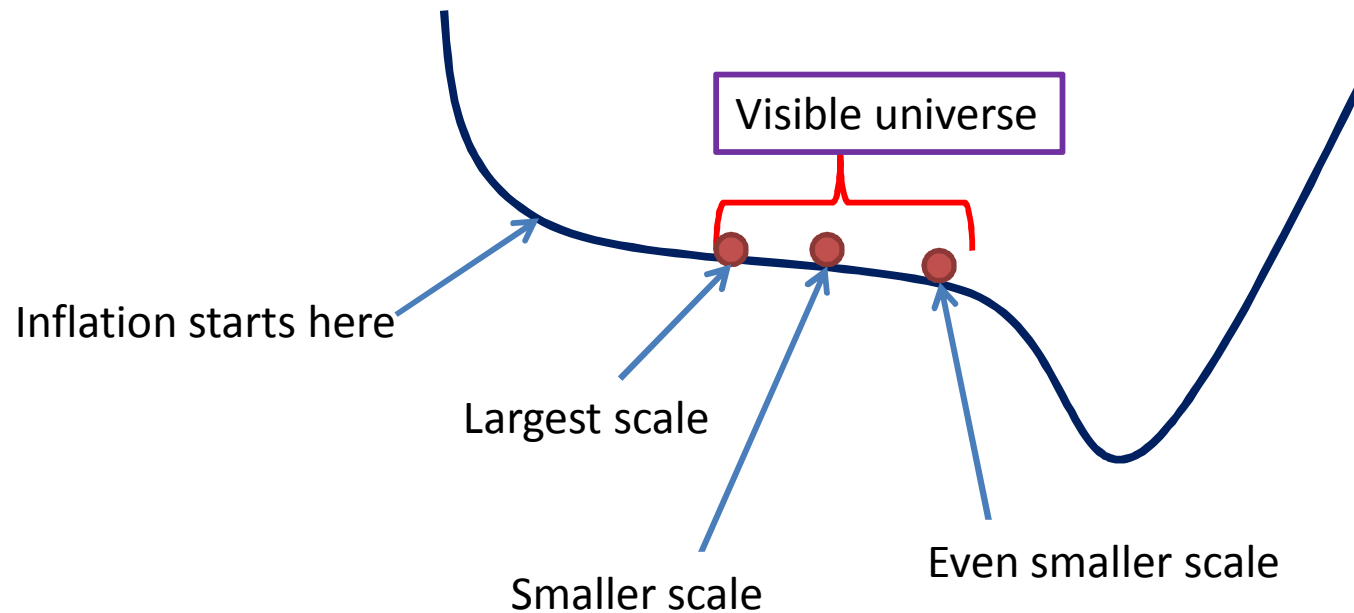


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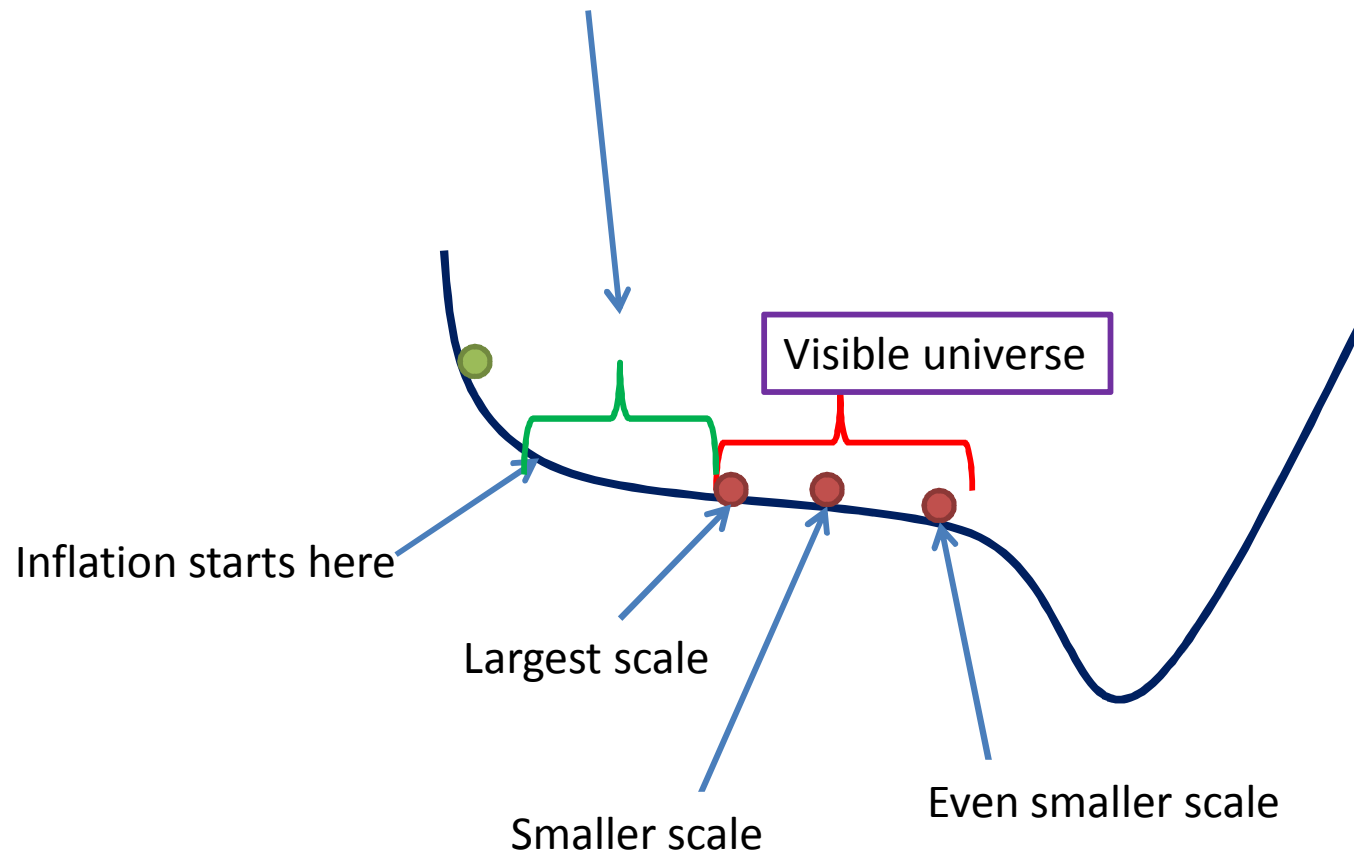


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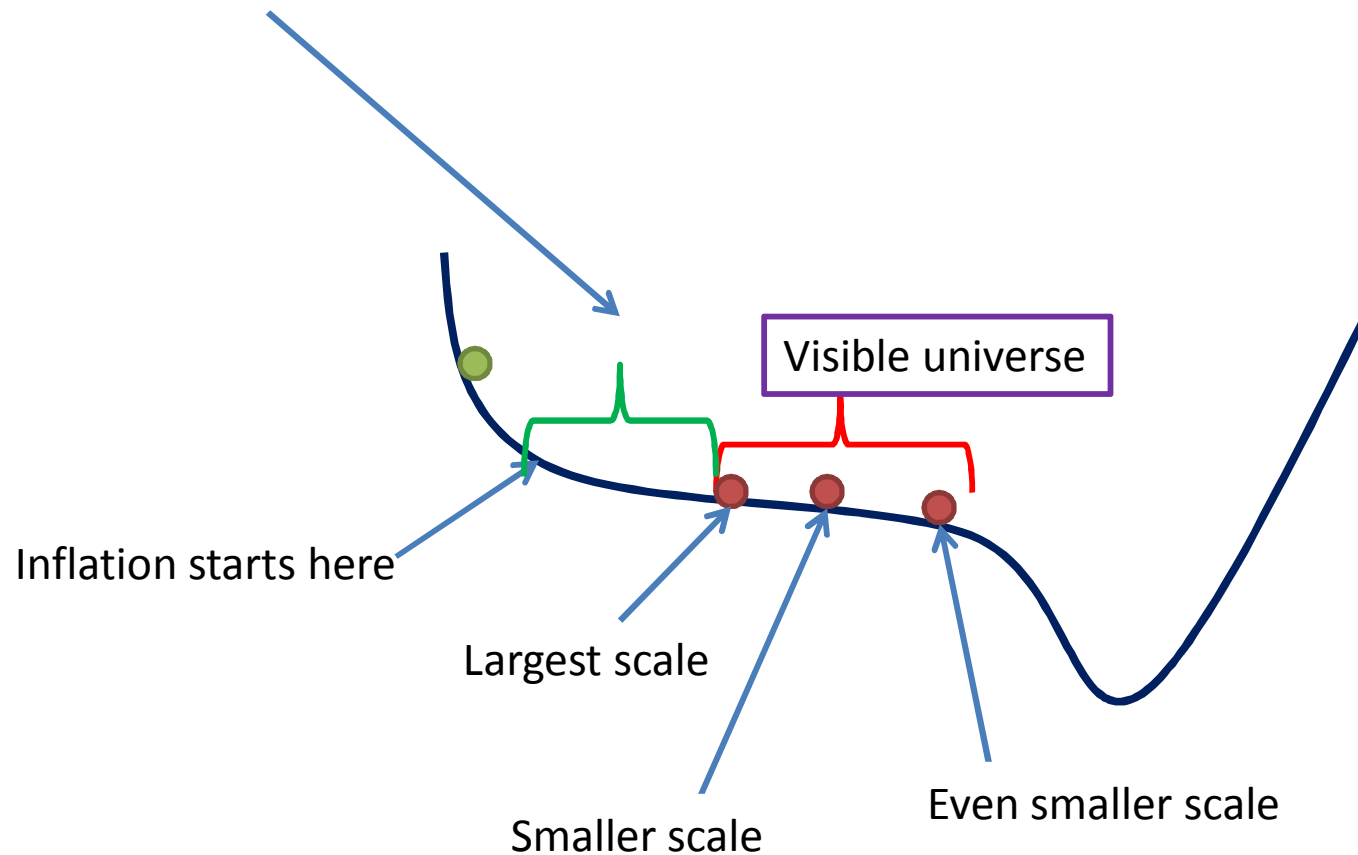
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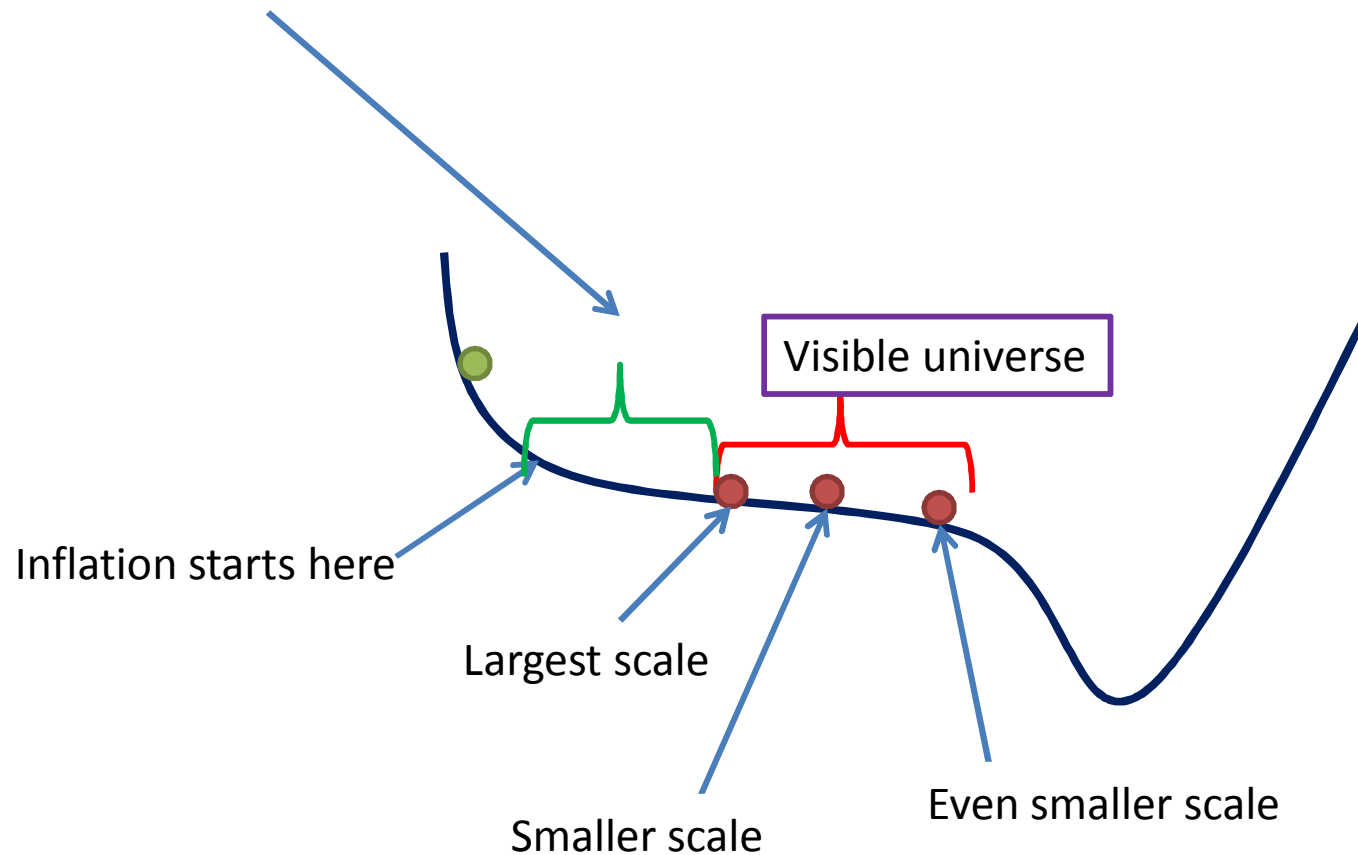
If  $\Delta N$  is large then the visible universe is not sensitive to the initial condition  $\bullet$ .

$$\Delta N = N^{total} - N^{visible}$$



If  $\Delta N$  is not that large then the largest scales in the visible universe depend on  $\bullet$ .

$$\Delta N = N^{total} - N^{visible}$$



I would like to argue that both **experimentally** and theoretically  
there are hints that  $\Delta N$  is not too large.

Experimentally, there are some  $2\sigma$  anomalies at the largest scales:

## Large peculiar velocity

(Watkins, Feldman, Hudson, 0809.4041; Kashlinsky, Atrio-Barandela, Kocevski, Ebeling, 0809.3734; Lavaux, Tully, Mohayaee, Colombi, 0810.3658)

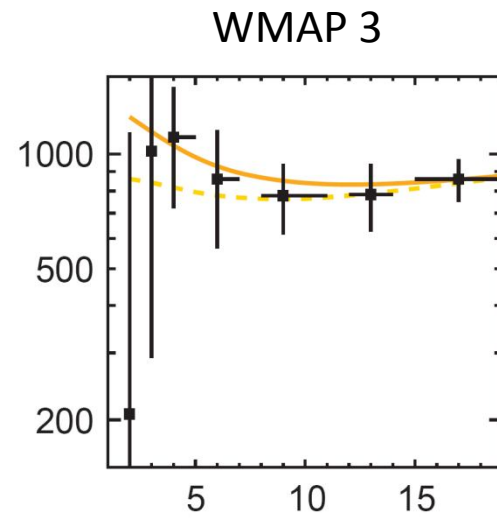
### Theory :

1. For  $\sim 100h^{-1}$  Mpc  
about  $\sim 110 \text{ km s}^{-1}$
2. Drops like  $1/r$

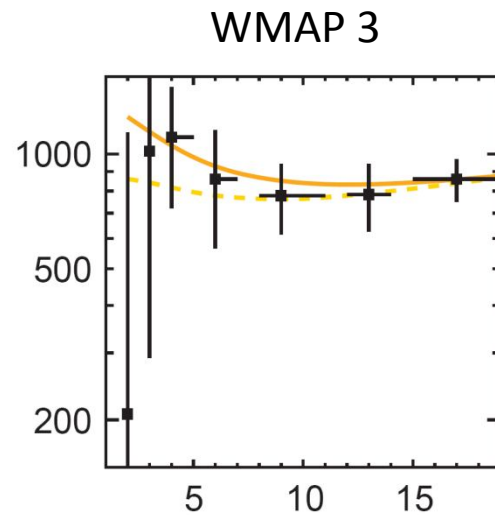
### Observation:

1. For  $\sim 100h^{-1}$  Mpc  
about  $407 \pm 81 \text{ km s}^{-1}$
2. Does not drop with distance.

CMB is anomalously small at large distances



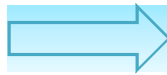
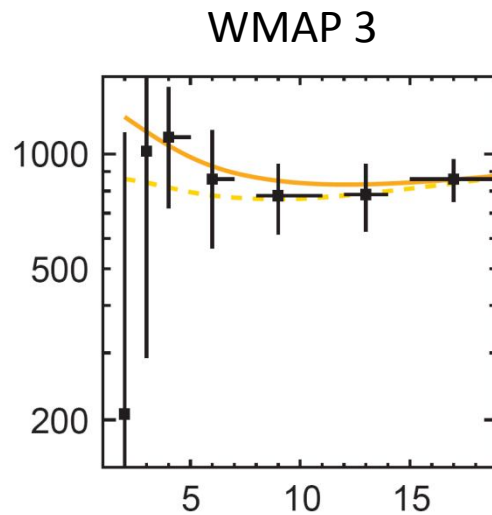
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Might be viewed as evidence  
for small  $\Delta N$  .



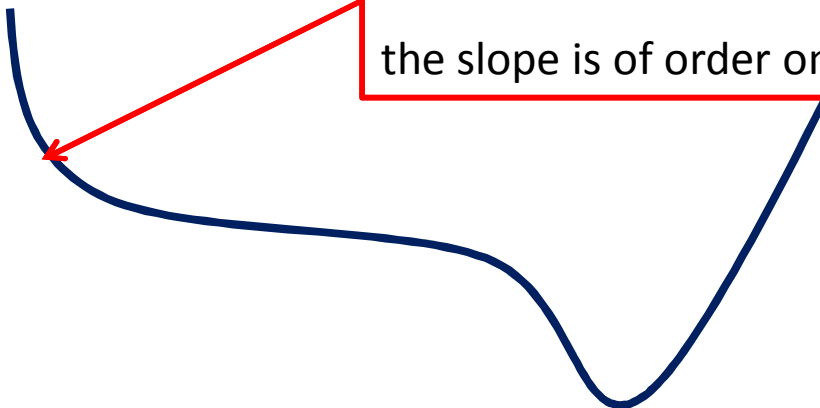
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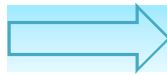
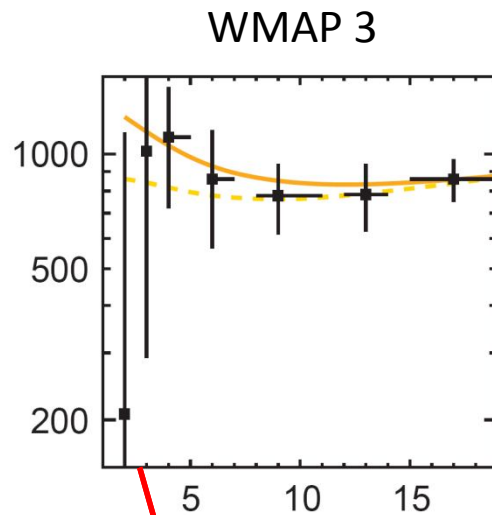
Might be viewed as evidence  
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The reason is that  $P \sim \frac{1}{V'}$

Inflation begins roughly where  
the slope is of order one



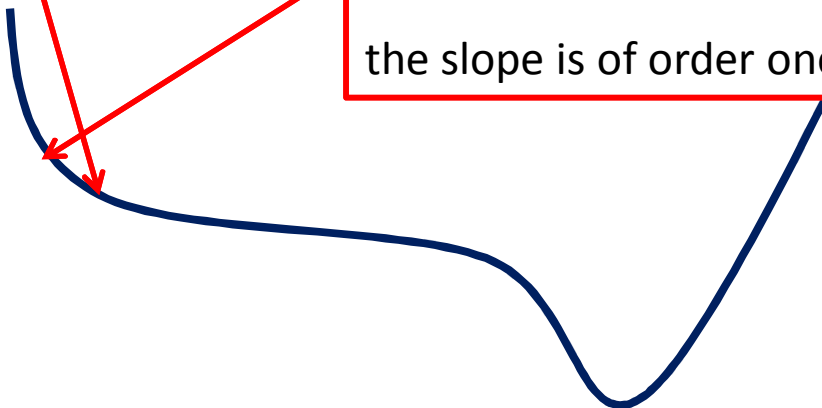
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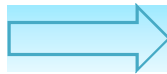
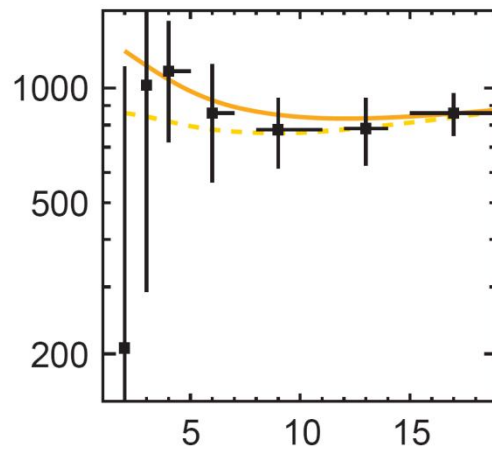
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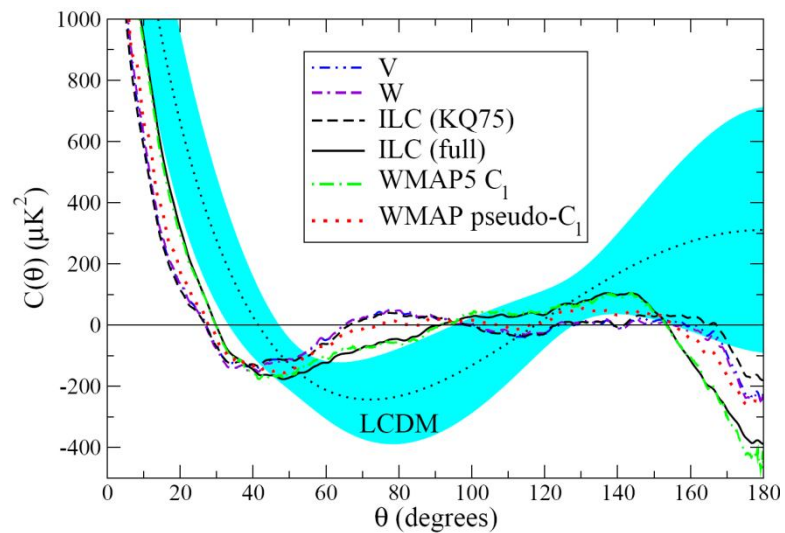
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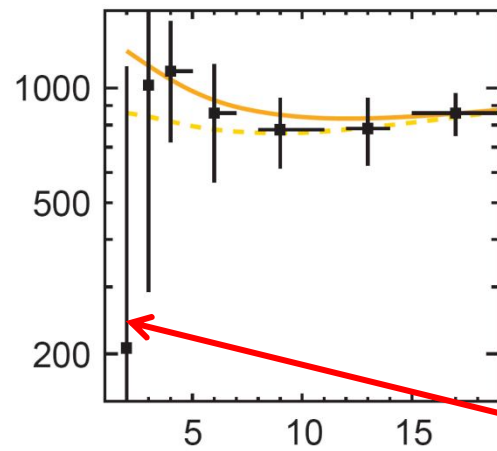
WMAP 3



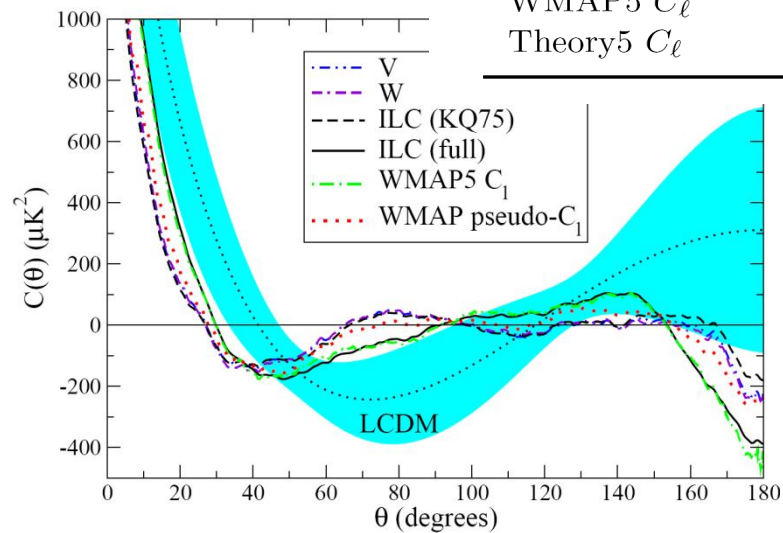
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Copi et.al 0808.3767

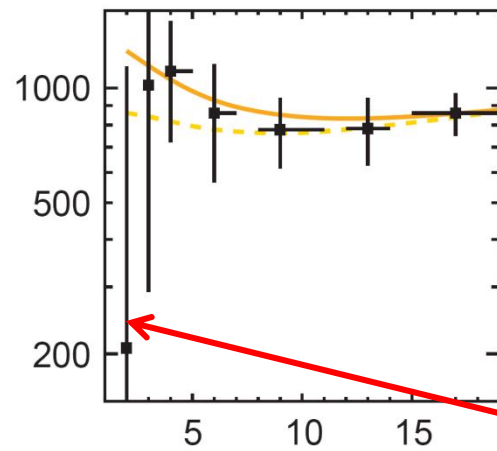




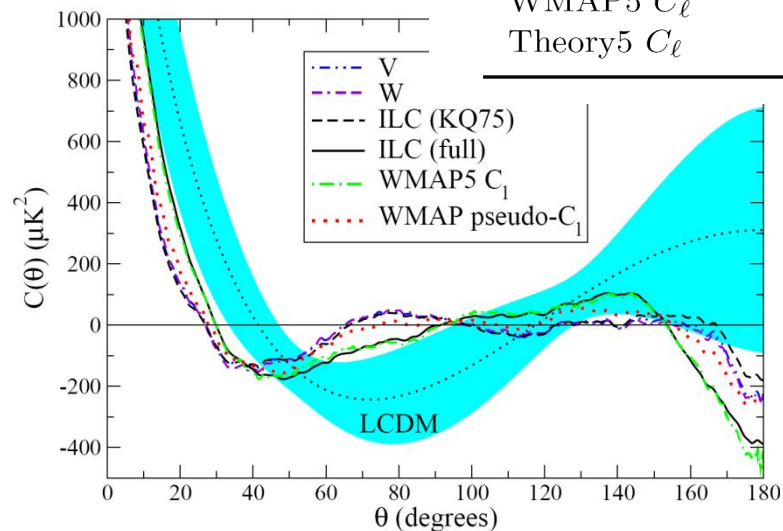
Data Source	$S_{1/2}$ ( $\mu\text{K}$ ) <sup>4</sup>	$P(S_{1/2})$ (per cent)	$6C_2/2\pi$ ( $\mu\text{K}$ ) <sup>2</sup>	$12C_3/2\pi$ ( $\mu\text{K}$ ) <sup>2</sup>	$20C_4/2\pi$ ( $\mu\text{K}$ ) <sup>2</sup>	$30C_5/2\pi$ ( $\mu\text{K}$ ) <sup>2</sup>
V3 (kp0, DQ)	1288	0.04	77	410	762	1254
W3 (kp0, DQ)	1322	0.04	68	450	771	1302
ILC3 (kp0, DQ)	1026	0.017	128	442	762	1180
ILC3 (kp0), $\mathcal{C}( > 60^\circ ) = 0$	0	—	84	394	875	1135
ILC3 (full, DQ)	8413	4.9	239	1051	756	1588
V5 (KQ75)	1346	0.042	60	339	745	1248
W5 (KQ75)	1330	0.038	47	379	752	1287
V5 (KQ75, DQ)	1304	0.037	77	340	746	1249
W5 (KQ75, DQ)	1284	0.034	59	379	753	1289
ILC5 (KQ75)	1146	0.025	81	320	769	1156
ILC5 (KQ75, DQ)	1152	0.025	95	320	768	1158
ILC5 (full, DQ)	8583	5.1	253	1052	730	1590
WMAP3 pseudo- $C_\ell$	2093	0.18	120	602	701	1346
WMAP3 MLE $C_\ell$	8334	4.2	211	1041	731	1521
Theory3 $C_\ell$	52857	43	1250	1143	1051	981
WMAP5 $C_\ell$	8833	4.6	213	1039	674	1527
Theory5 $C_\ell$	49096	41	1207	1114	1031	968



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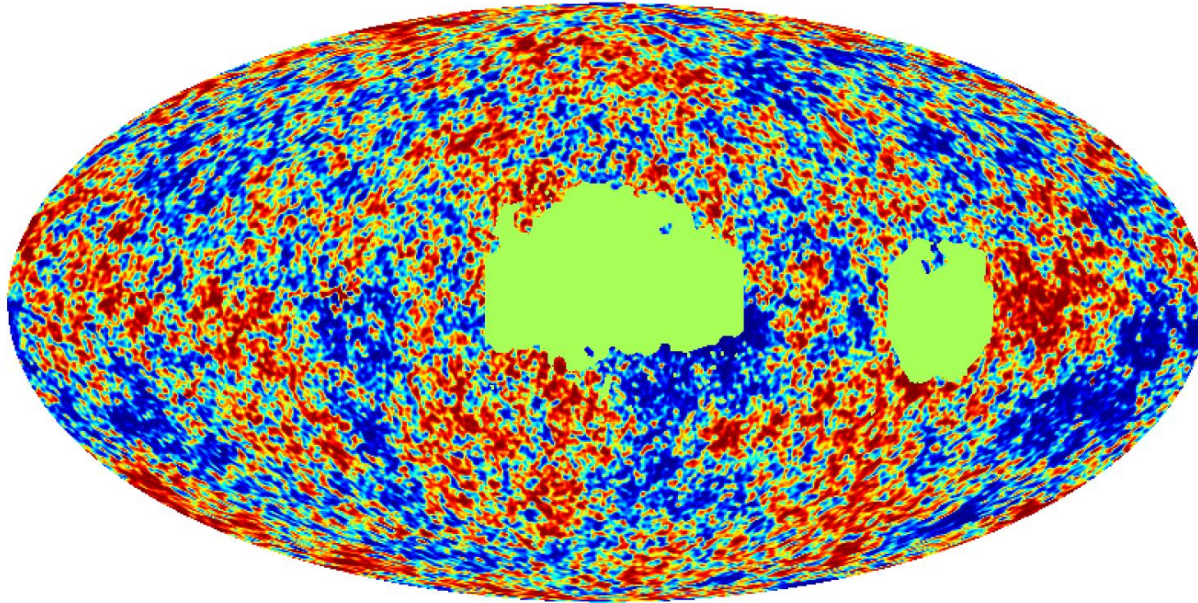
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Become much less probable when  
masking the galactic plane

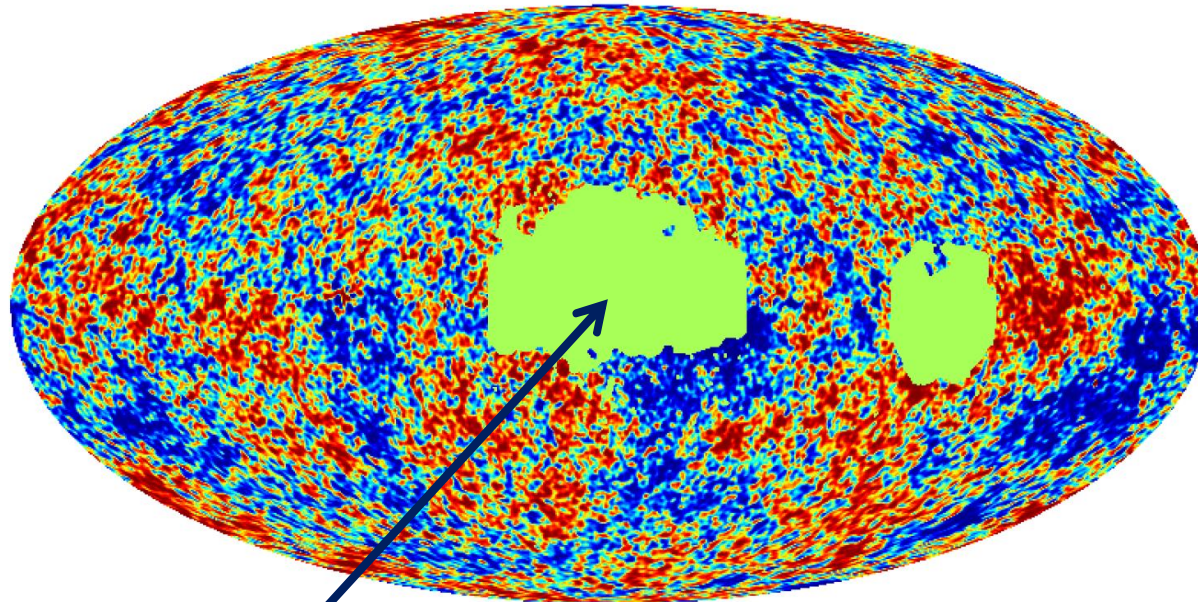
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In fact even within the galactic plane it is localized (Hajian 0702723)



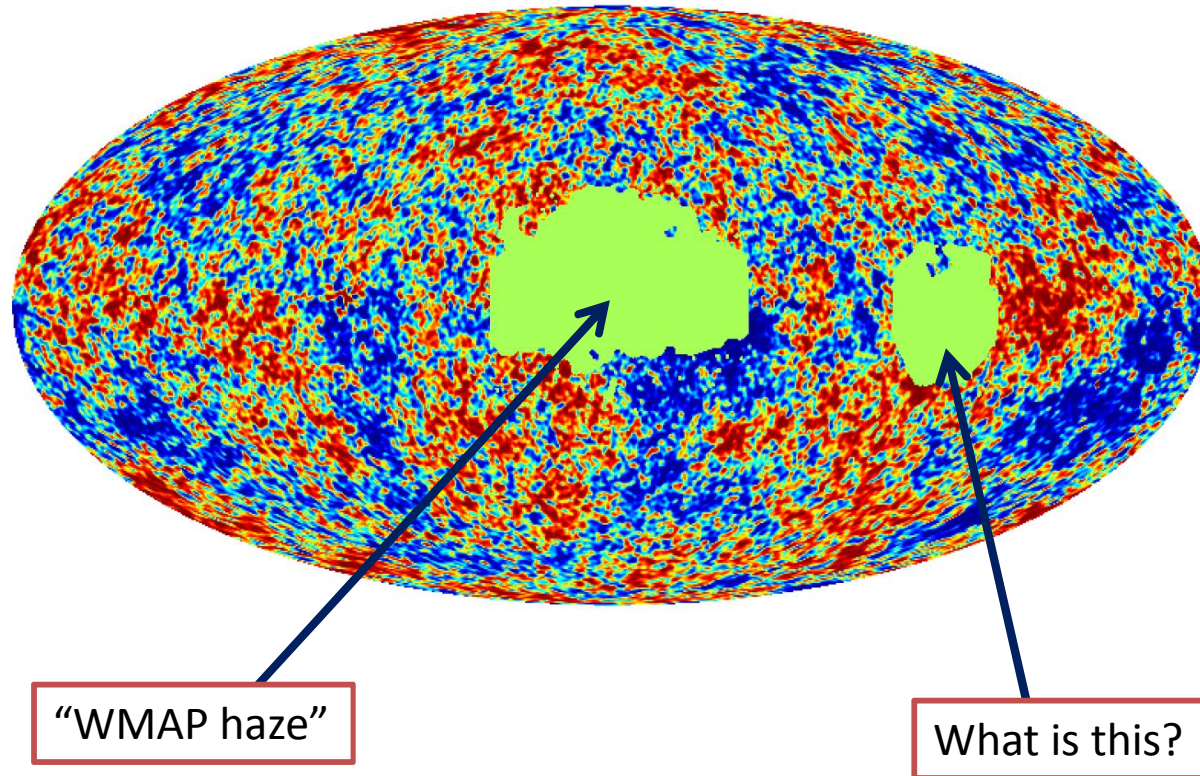


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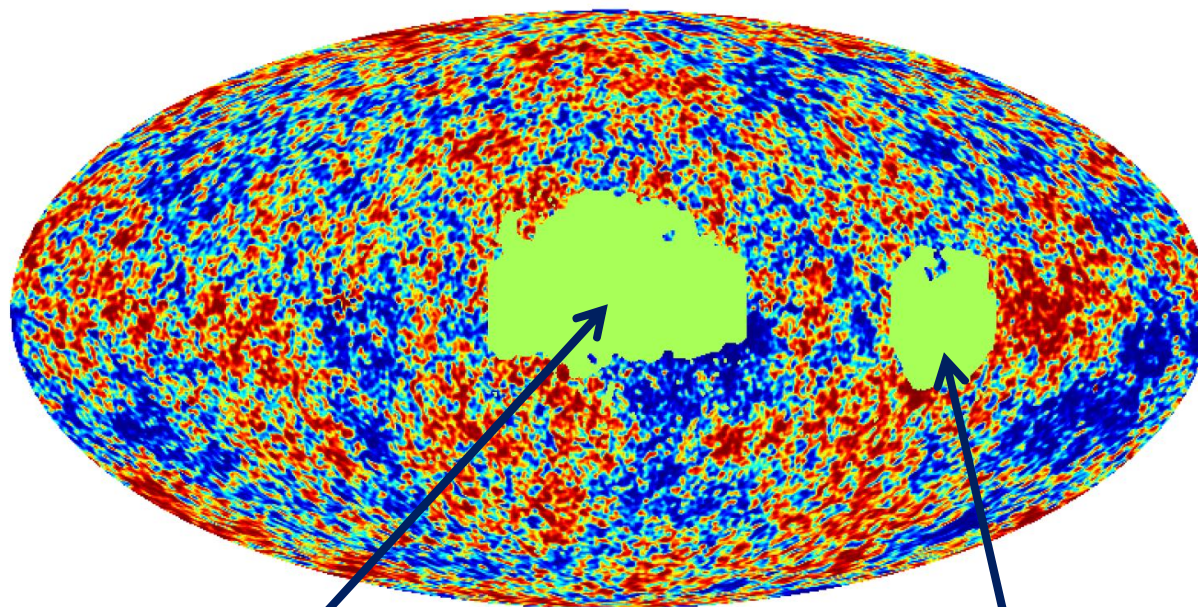
"WMAP haze"

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"WMAP haze"

What is this?

Don't know.

But it is interesting that roughly it is in the same direction as the peculiar velocity.

Theoretically, it is not easy to construct in string theory large field models of inflation.

Where  $\Delta N$  is always large.

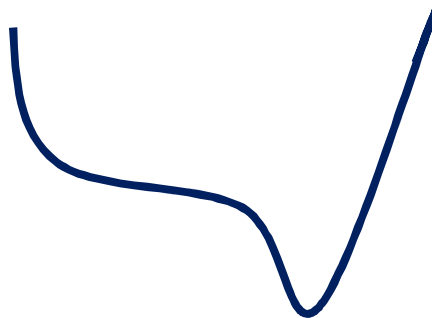
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Large field potential

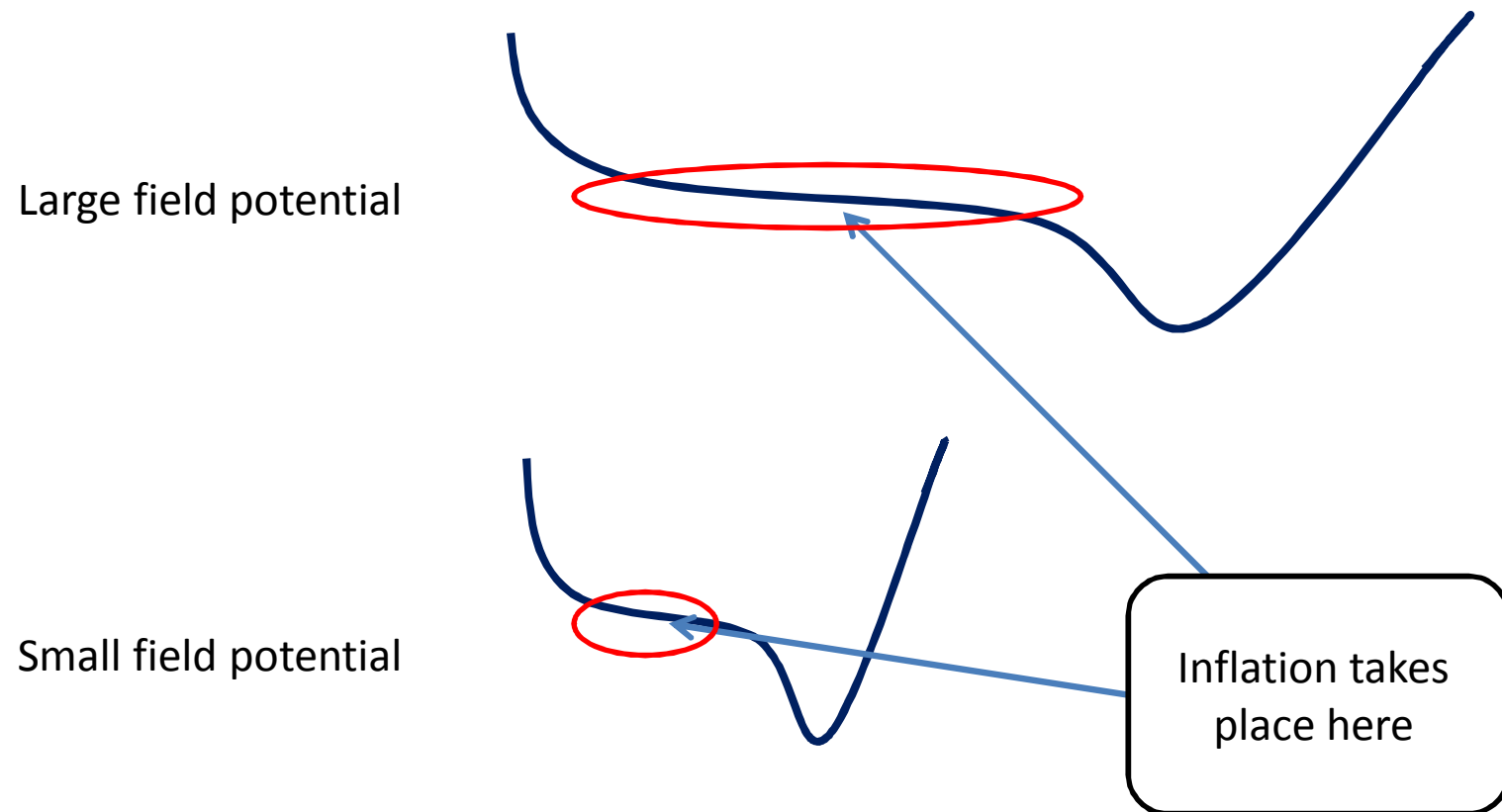


Small field potential



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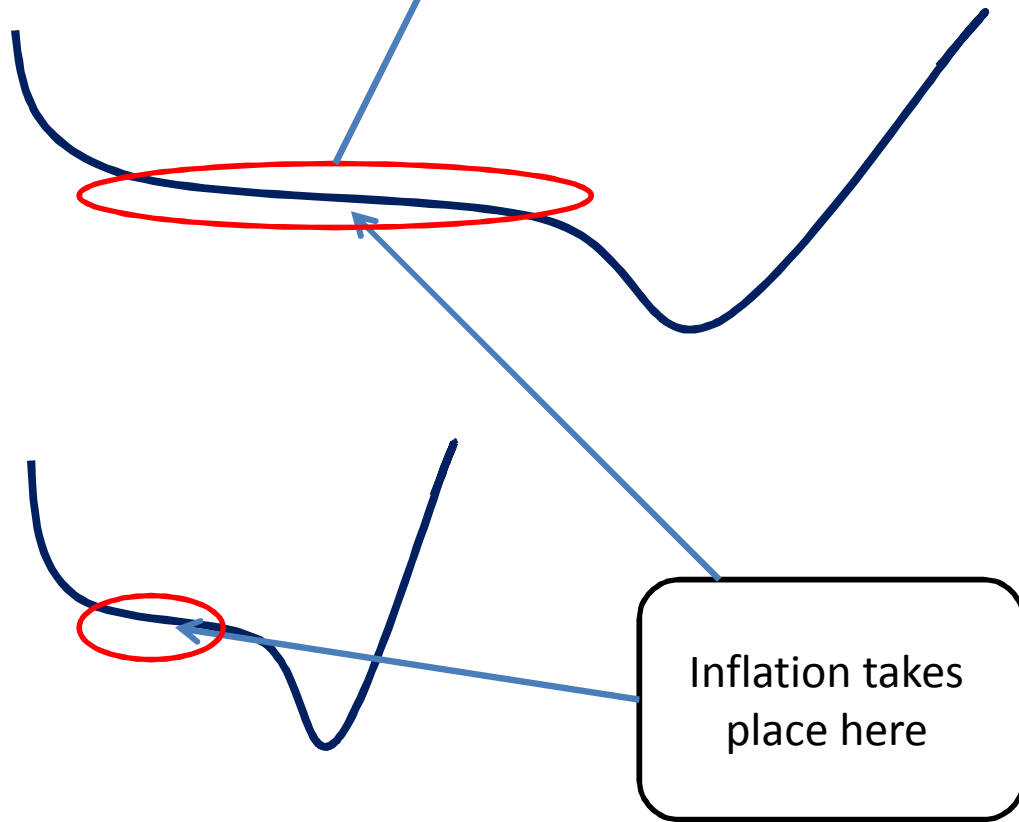


**N** is for sure much larger than 60.

Large field potential

Small field potential

Inflation takes  
place here



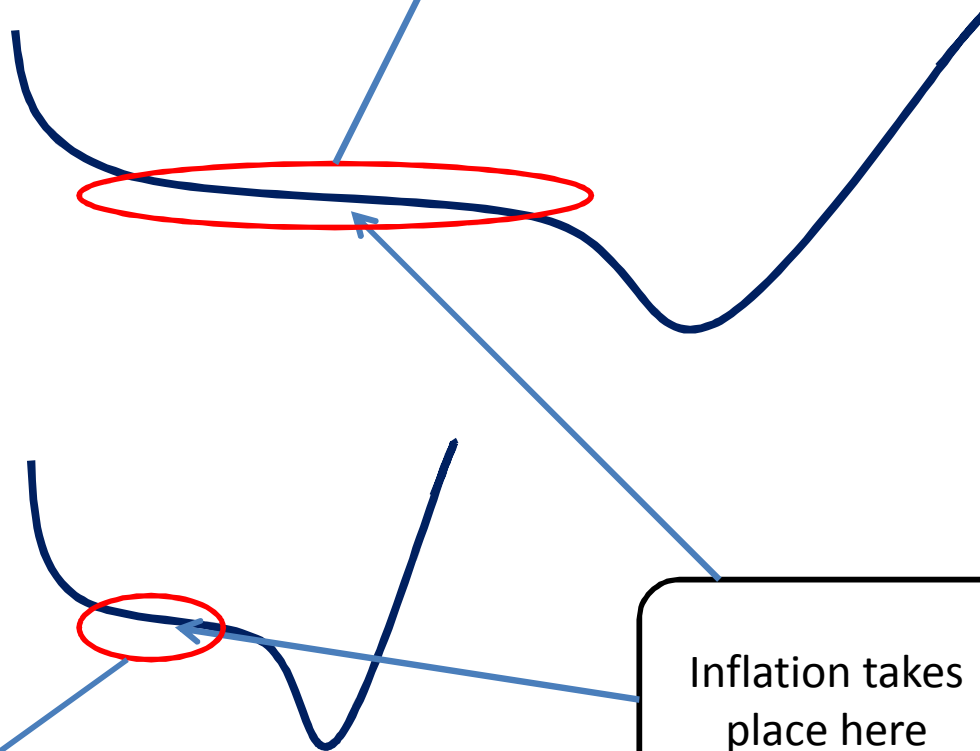
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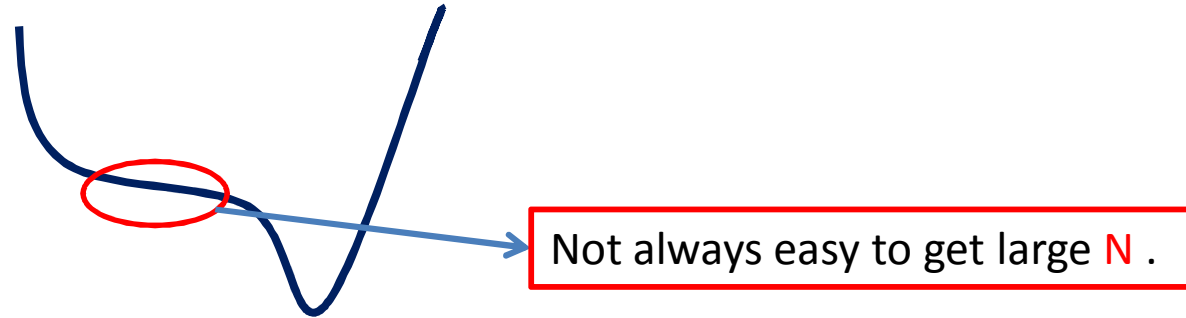
Large field potential

Small field potential

Inflation takes  
place here

Not always easy to get large  $N$ .





Moreover, often encounter the **overshoot problem** (Brustein, Steinhardt 92) :

The inflaton overshoots the slow roll region (where the universe inflates).

In the rest of the talk:

1. Discuss ways to overcome the overshoot problem.



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2. Show that in some cases the resolution has an experimental signature.
3. Possible connection with the  $2\sigma$  anomalies at the largest scales.

There aren't too many ways to address the overshoot problem.


The basic equation is

$$\ddot{\phi} + 3H\dot{\phi} + V_{,\phi} = 0$$


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A. Berendsen, T. Biswas and J. M. Cline;  
S. Cremonini, S. Watson; N. I., E. Kovetz

A - Increase **H** in a time dependent

fashion by adding particles.

B- Modify **V** in a time dependent fashion

by adding particles with mass that  
depend on the inflaton.

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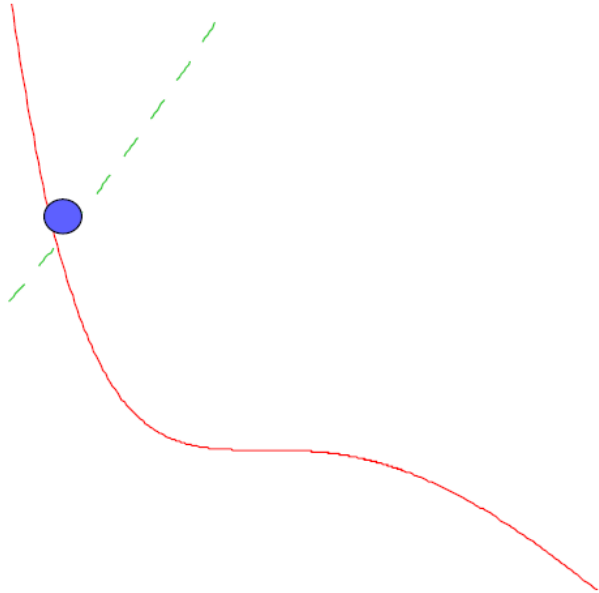
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depend on the inflaton.

$B$  is more efficient than  $A$  (by a factor of the slow-roll parameter)

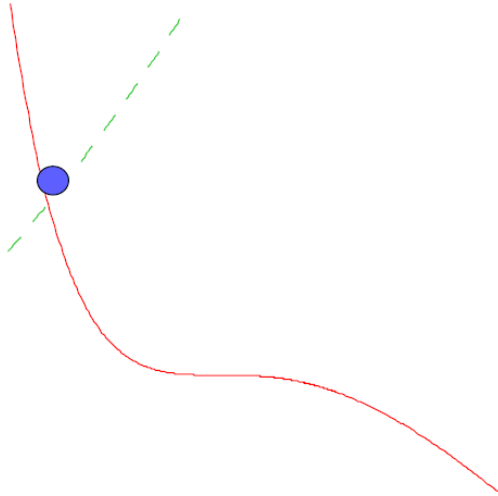
and has a stronger imprint (by a factor of the slow-roll parameter) .

A resolution to the overshoot problem (N.I. E. Kovetz [0708.2798](#))

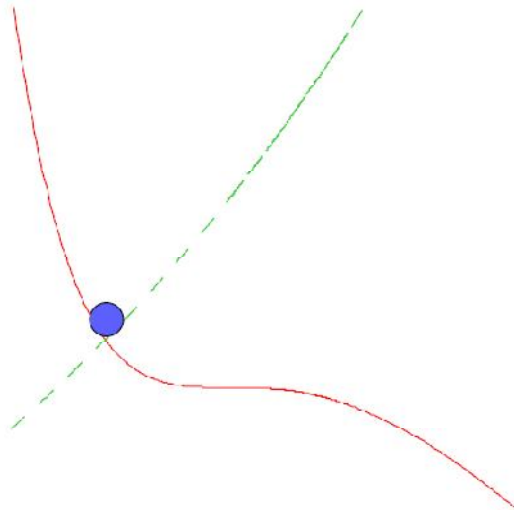


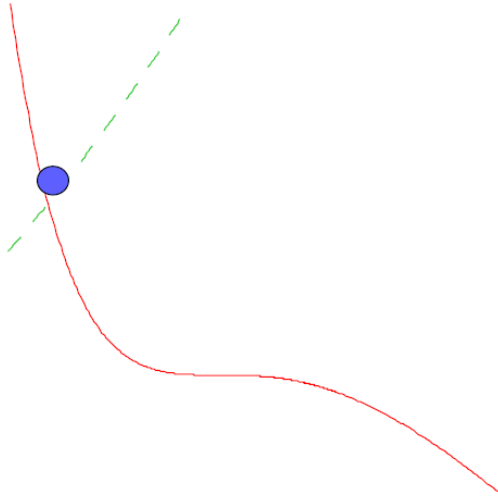
There are particles in the theory  
with mass that grows with the inflaton.  
These particles induce a time-dependent  
potential for the inflaton (green line).





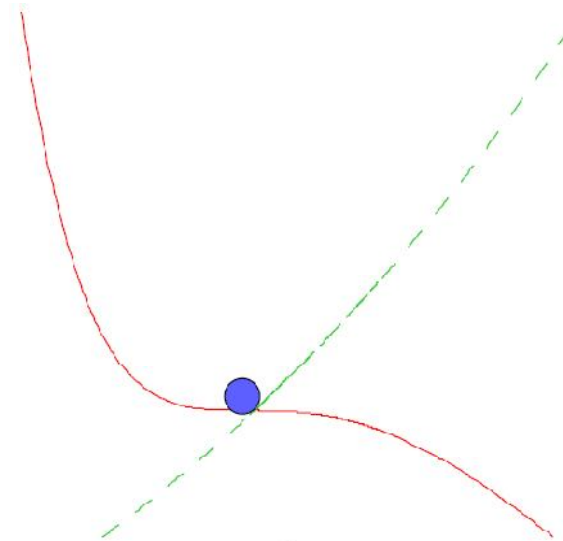
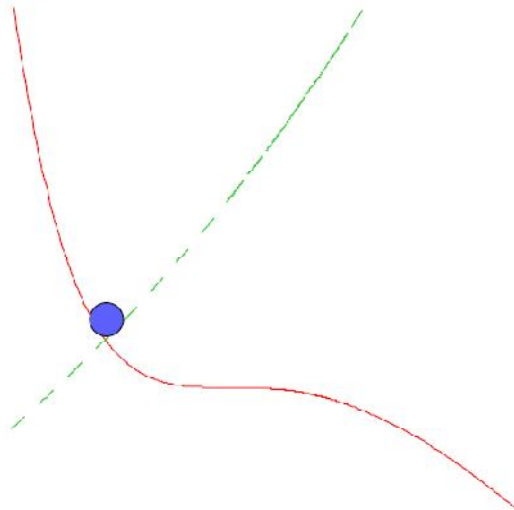
As the universe expands their density becomes smaller and the induced potential grows weaker.



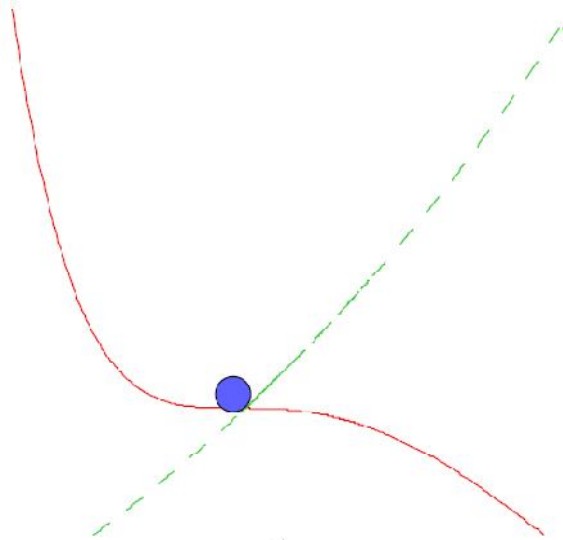


As the universe expands their density becomes smaller and the induced potential grows weaker.

And weaker.

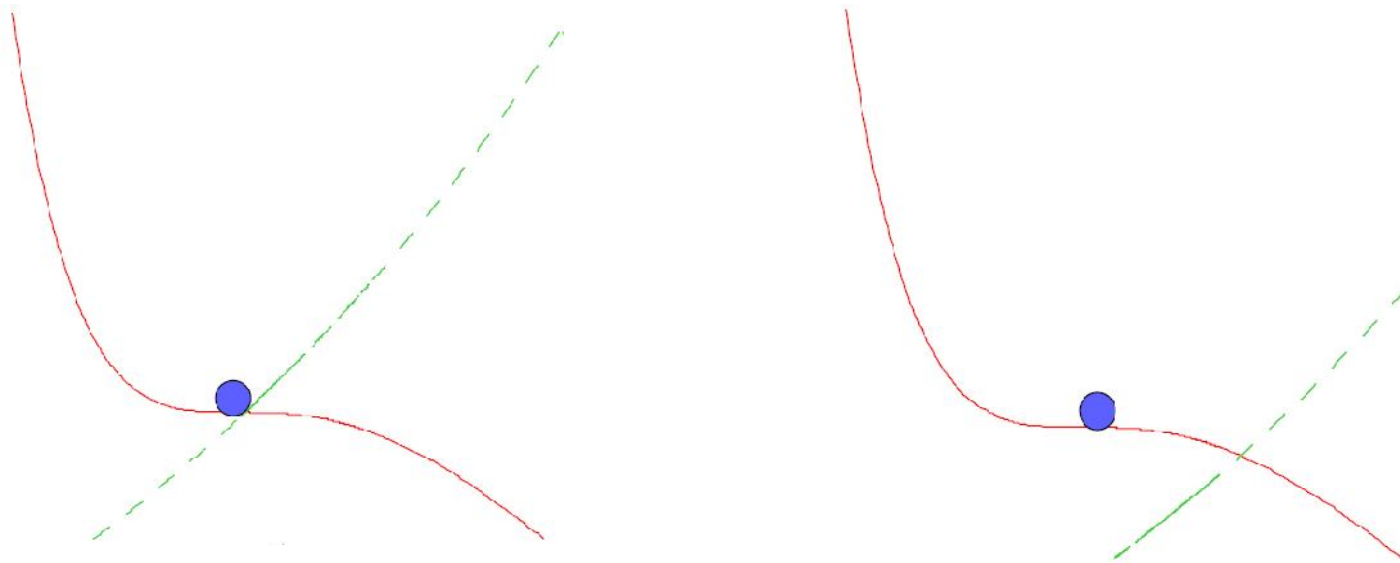


At this stage the particles are not “needed” to balance the inflaton.

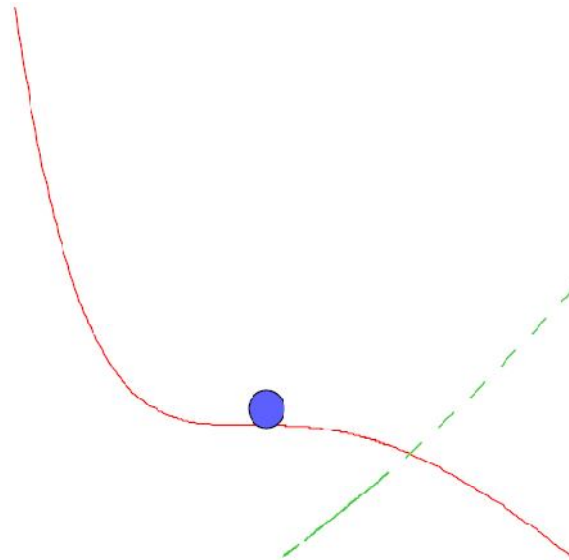


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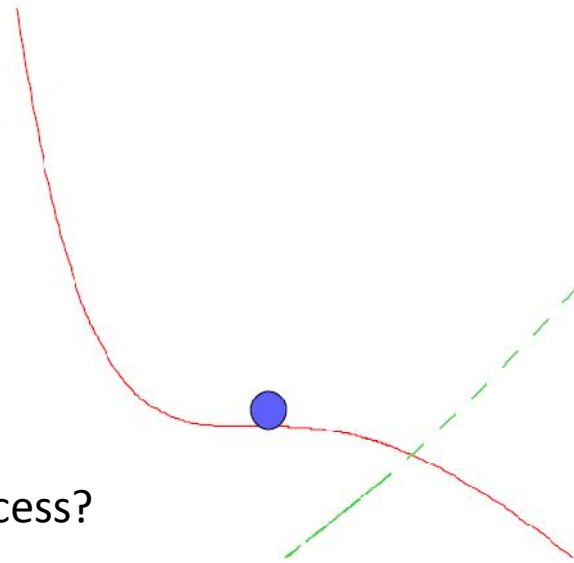
And they get diluted while the inflaton remains at the slow-roll region



Regardless of the initial condition  
we end up at the slow roll region.  
And inflation can begin.



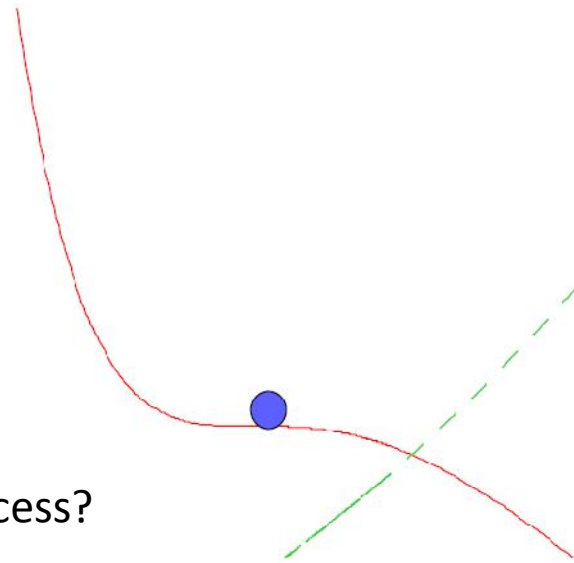
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Q: Is there any experimental signature to this process?

(any remnant of these particles?)

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Q: Is there any experimental signature to this process?

(any remnant of these particles?)

A: Yes.

Each particle creates a spherically symmetric giant structure.

If  $\Delta N$  is not too large some of them are in the visible universe.

We know that the shape of the inflaton during inflation is the seed for structure formation.



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A particle during inflation will have the following effect on the inflaton

$$\delta\ddot{\phi} + 3H\delta\dot{\phi} - \frac{1}{a(t)^2}\nabla^2\delta\phi + \frac{\delta^3(x)}{a^3}m_{eff} = 0$$

where

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The imprint of ordinary particles is suppress  
by the slow roll parameter

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The homogeneous solutions generate the usual quantum fluctuation which lead to the usual power spectrum.

On top we have the inhomogeneous solution which depends on the location of the particle(s).

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The particles push in  
the opposite direction

Each particle provide the seed  
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The shape of the overdense region is fixed by the inhomogeneous solution. In momentum space we find

$$\delta\phi_k = -\frac{Hm_{eff}}{\sqrt{32\pi}k^3}$$

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1. Scales like **H** (like the usual quantum effect)

  $m_{eff}$  should be large to be noticed.

The signal to noise ration is roughly  $m_{eff}$

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giant structure

Let's study the properties  
of this giant structure.

In 0807.3216 I considered the simplest


approximation to the transfer function:

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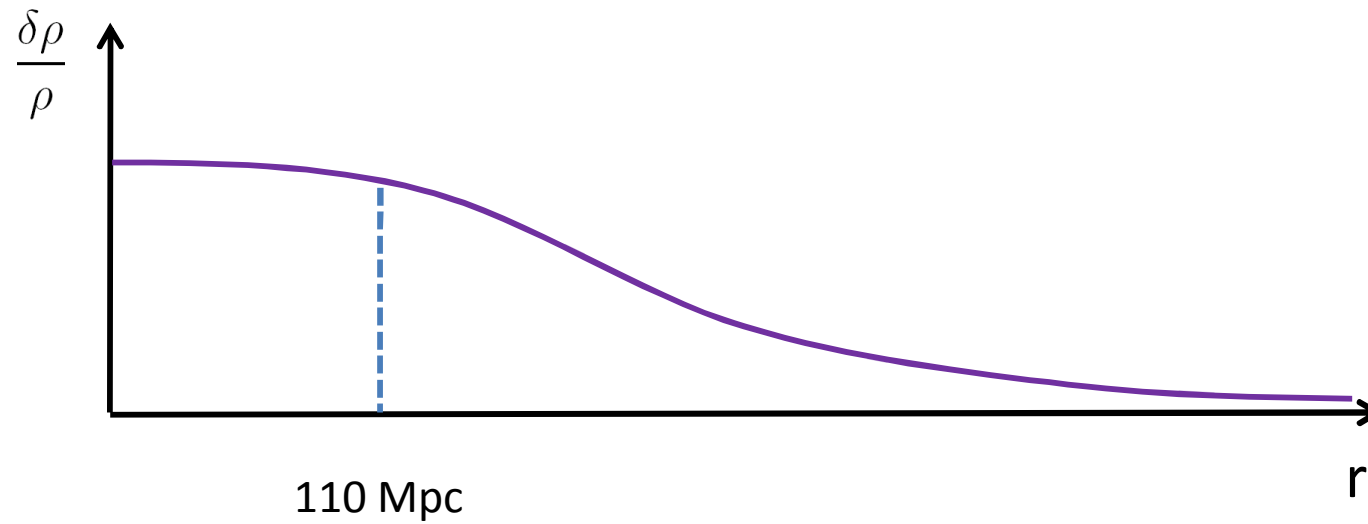


Linear with the scale factor  
during matter domination



No growth at all during  
radiation domination

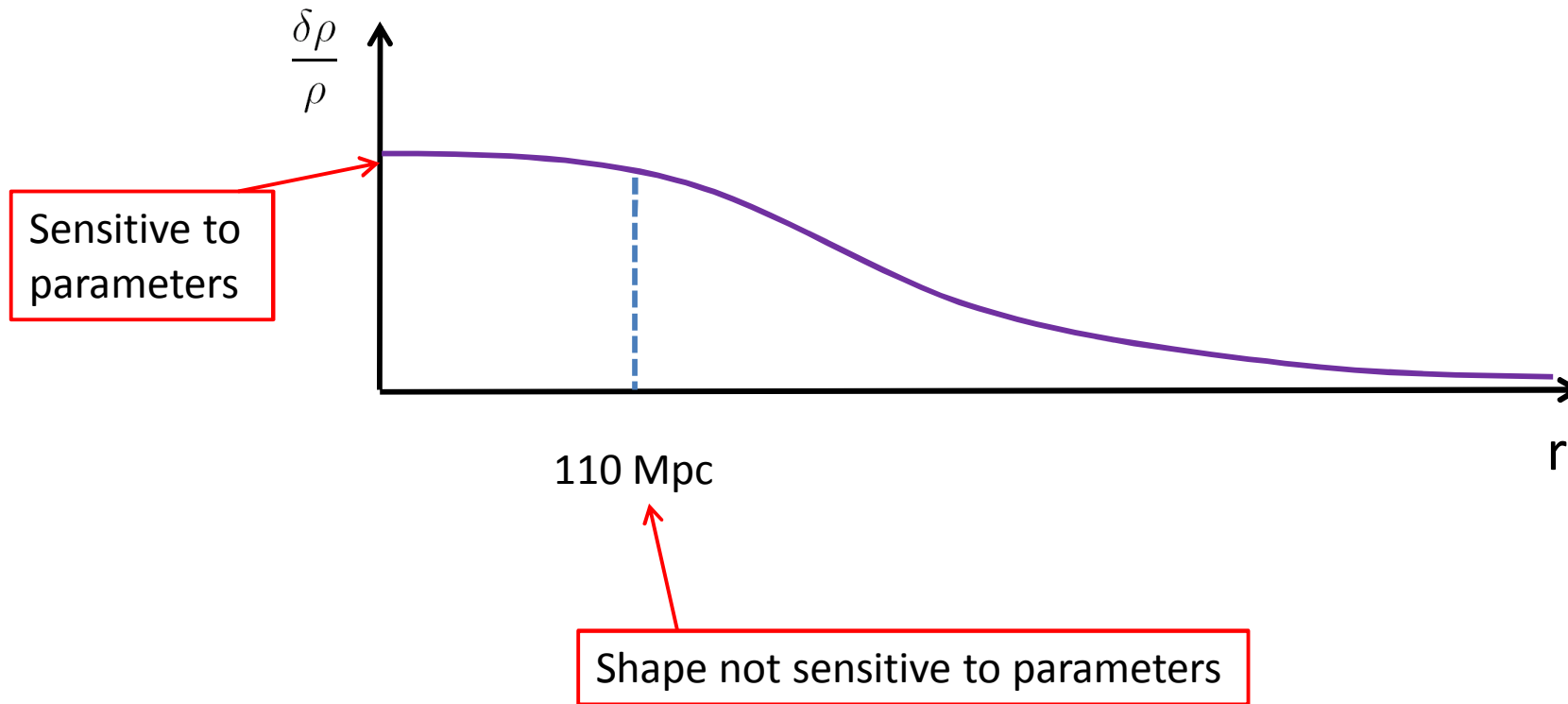
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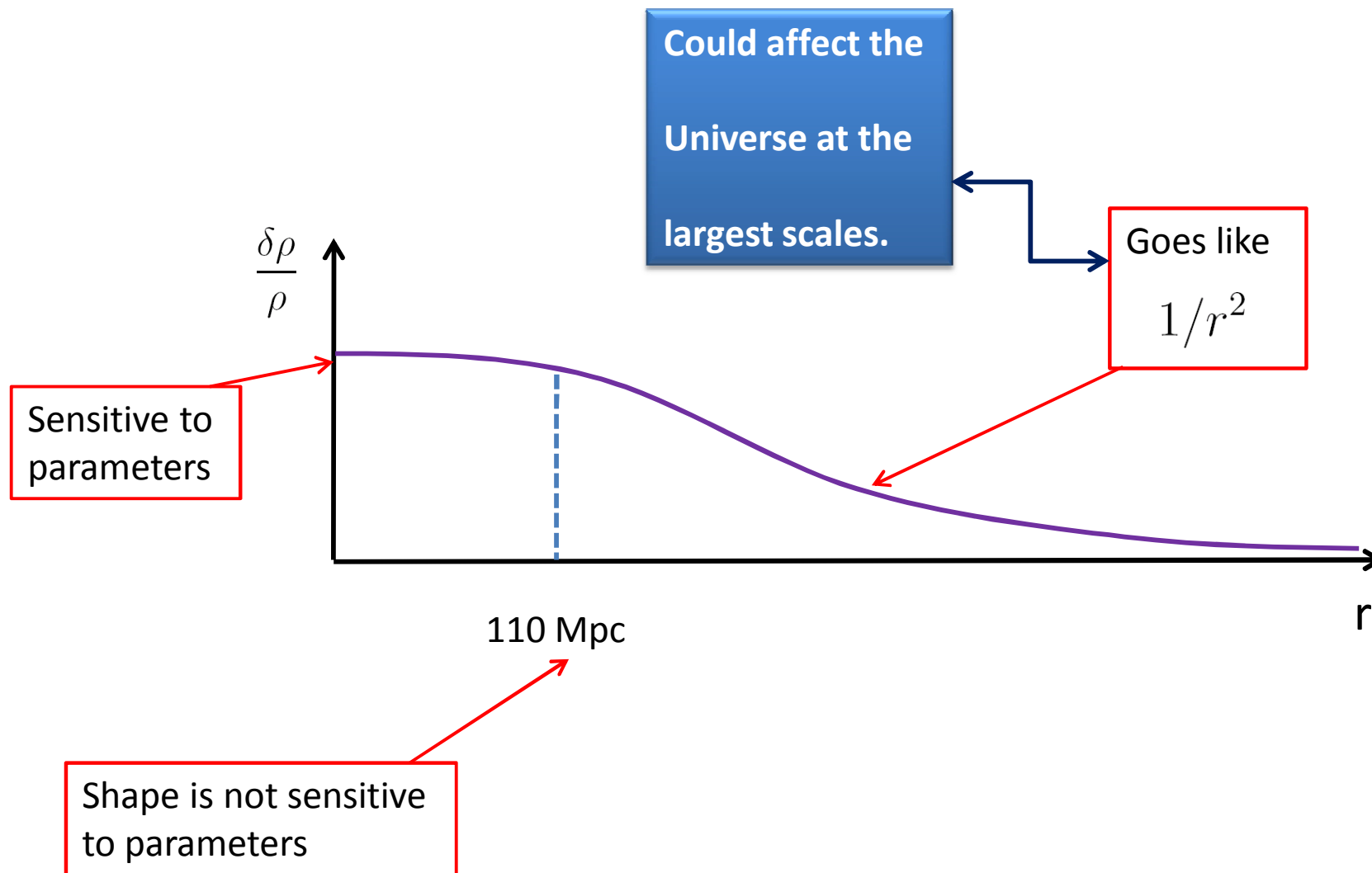


110 Mpc

Shape not sensitive to parameters

In this approximation





Right now with A. Fialkov and E. Kovetz we are looking in more detail into this option.

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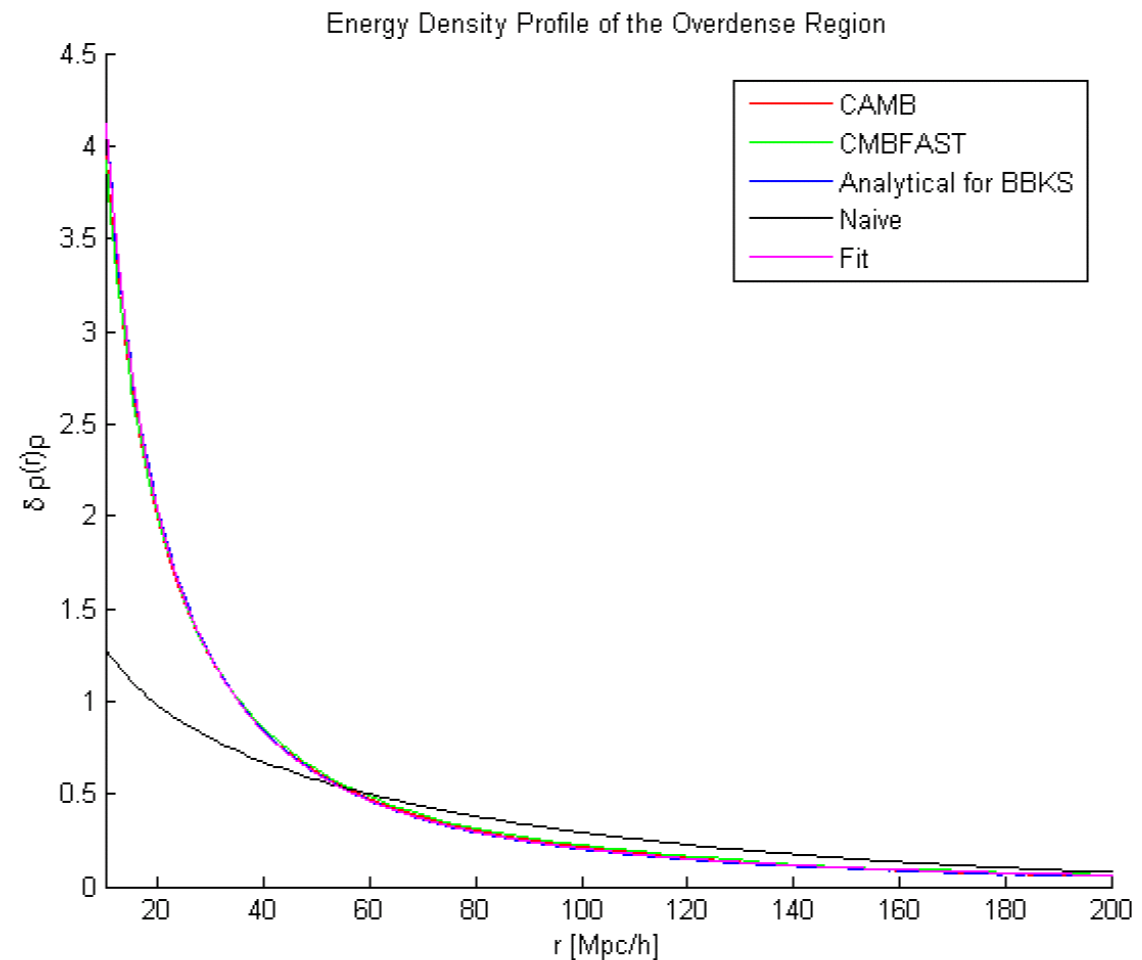
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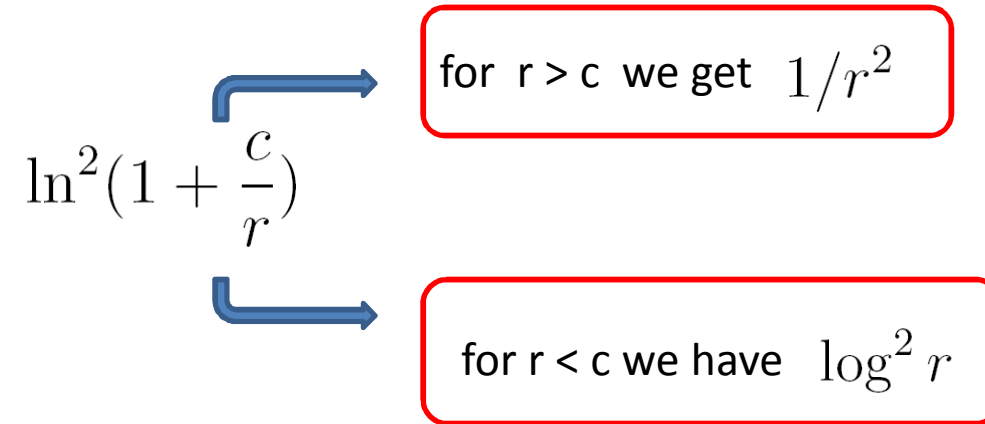
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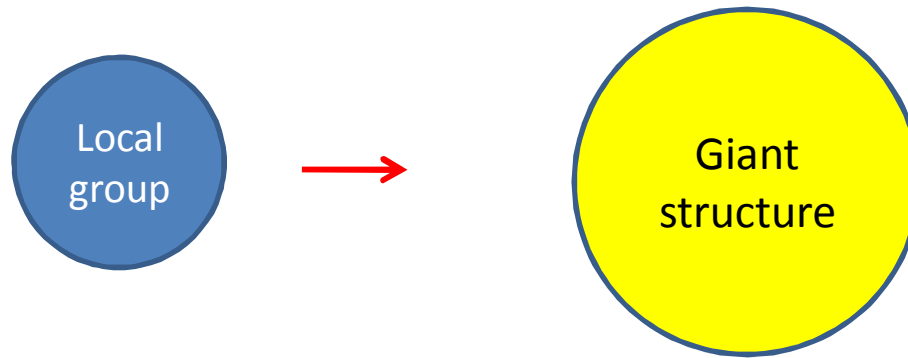
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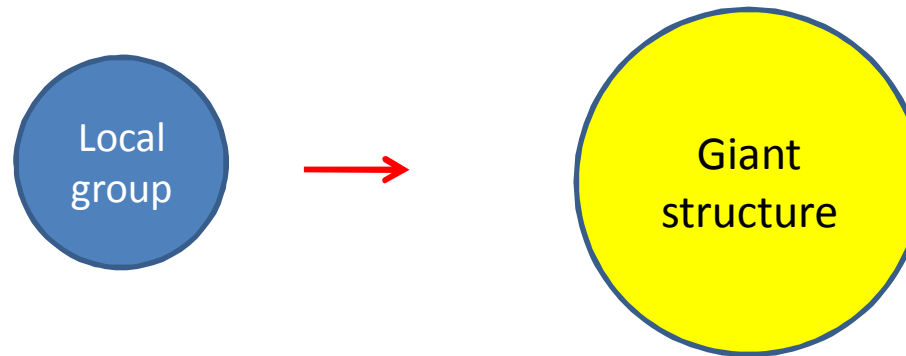
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If you know of a giant structure that roughly  
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Such a structure could easily explain the large peculiar velocity:

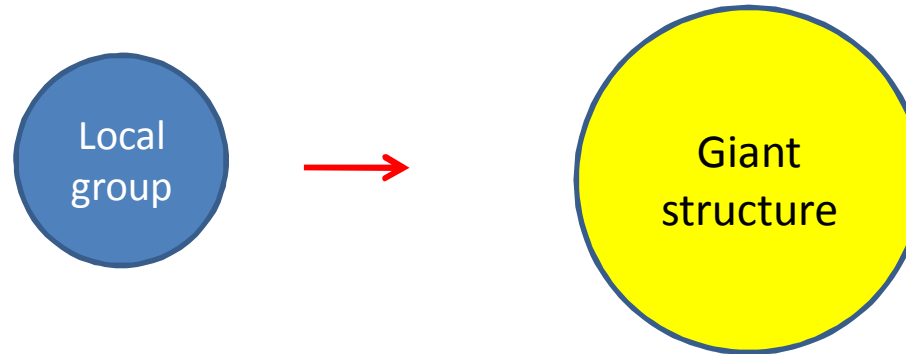


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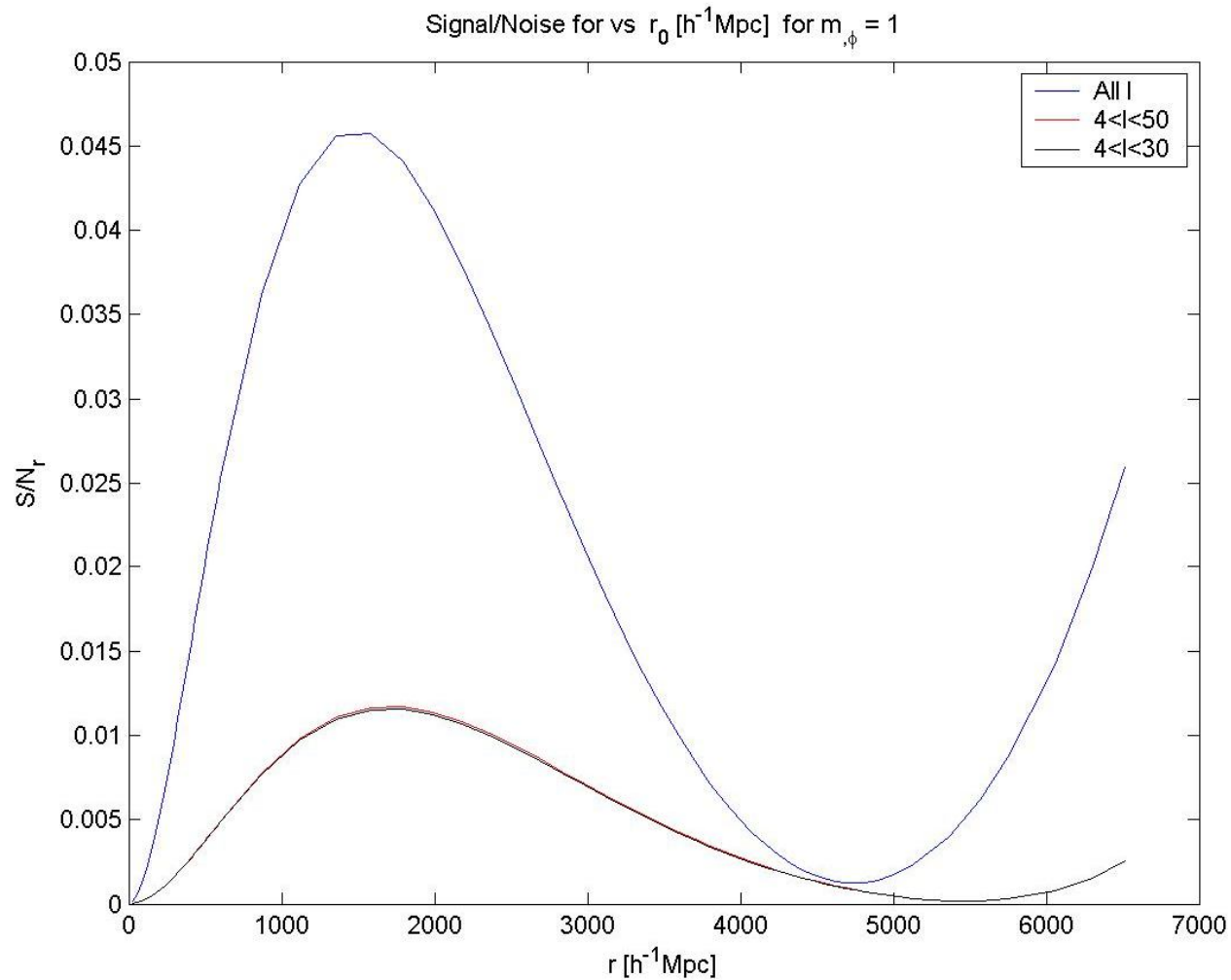
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As expected it affects mainly the low- $l$  modes.

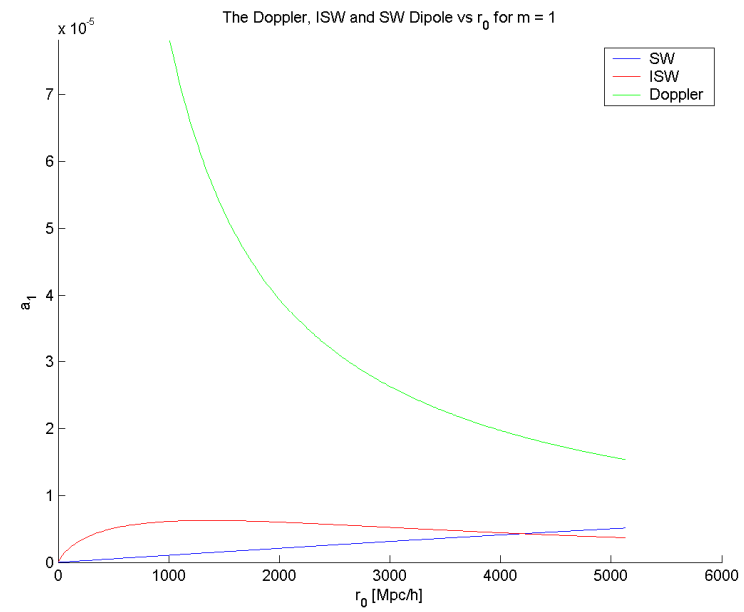
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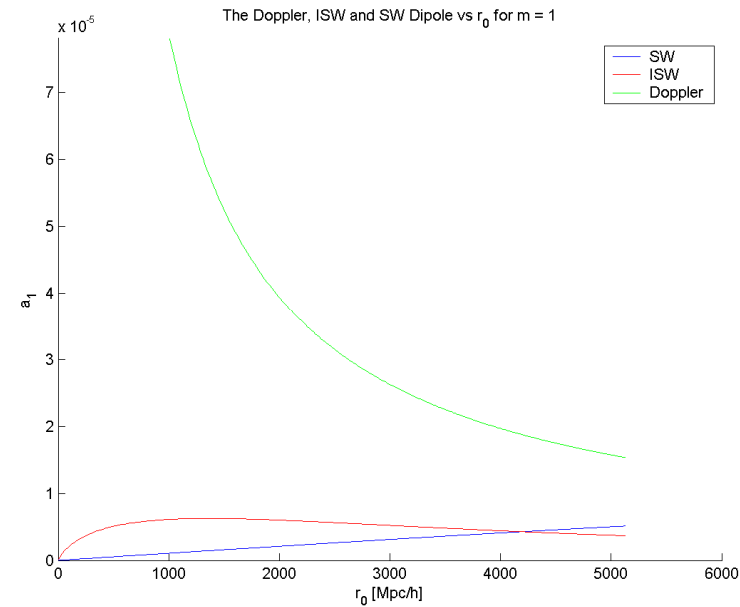




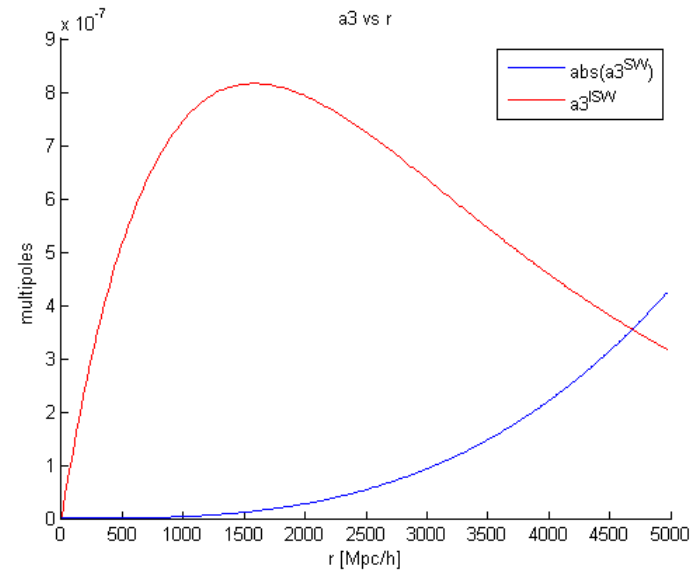
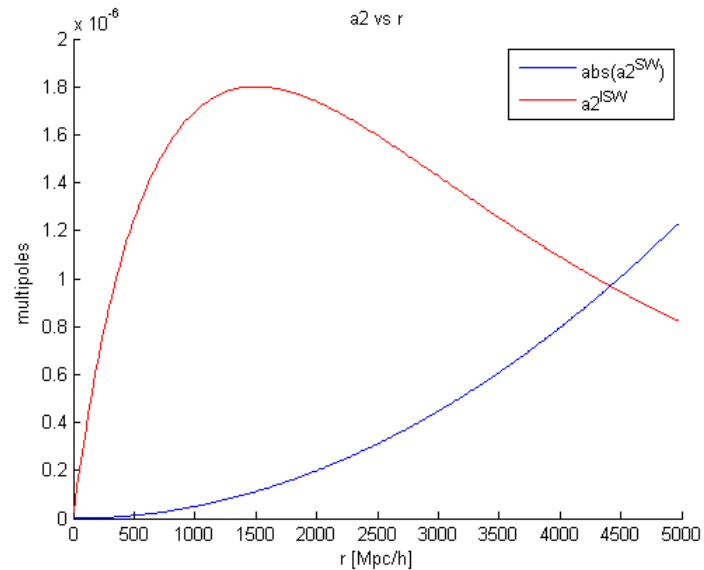
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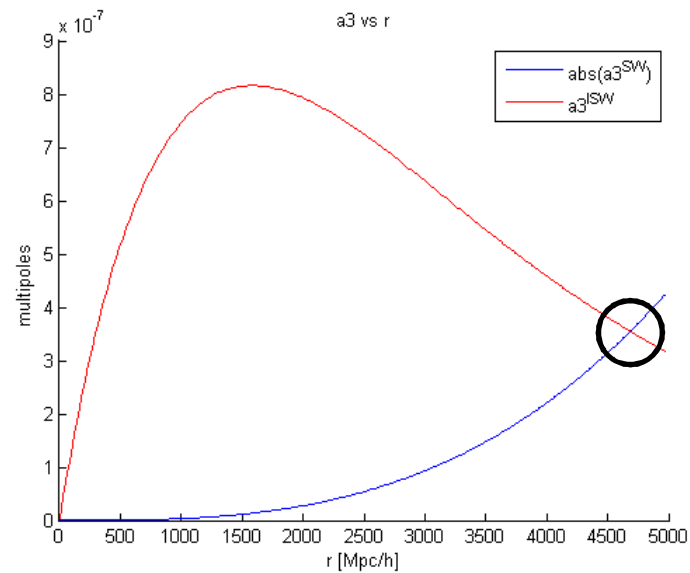
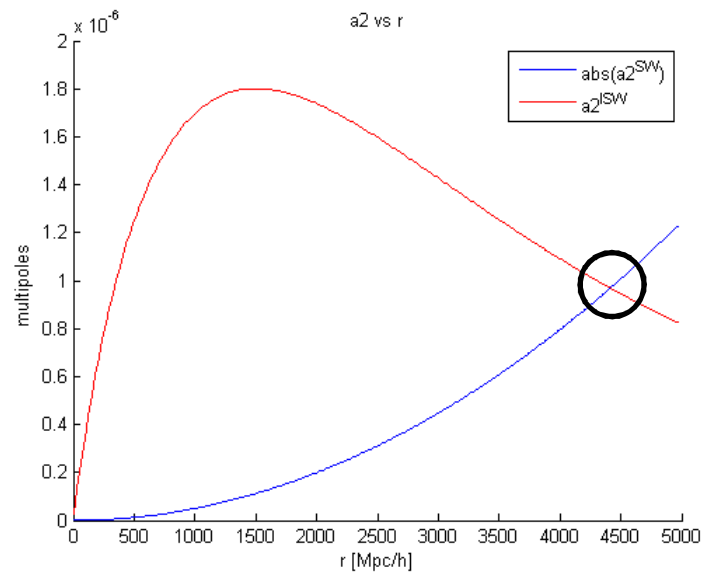
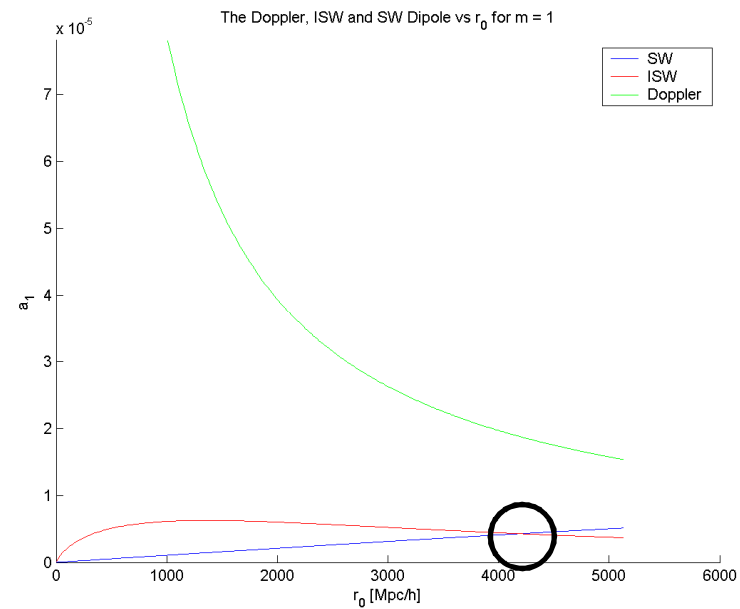
And two contributions to the rest (e.g. quadrupole & octopole):



Notice that for

$r \sim 4500/h$  Mpc

SW cancels ISW

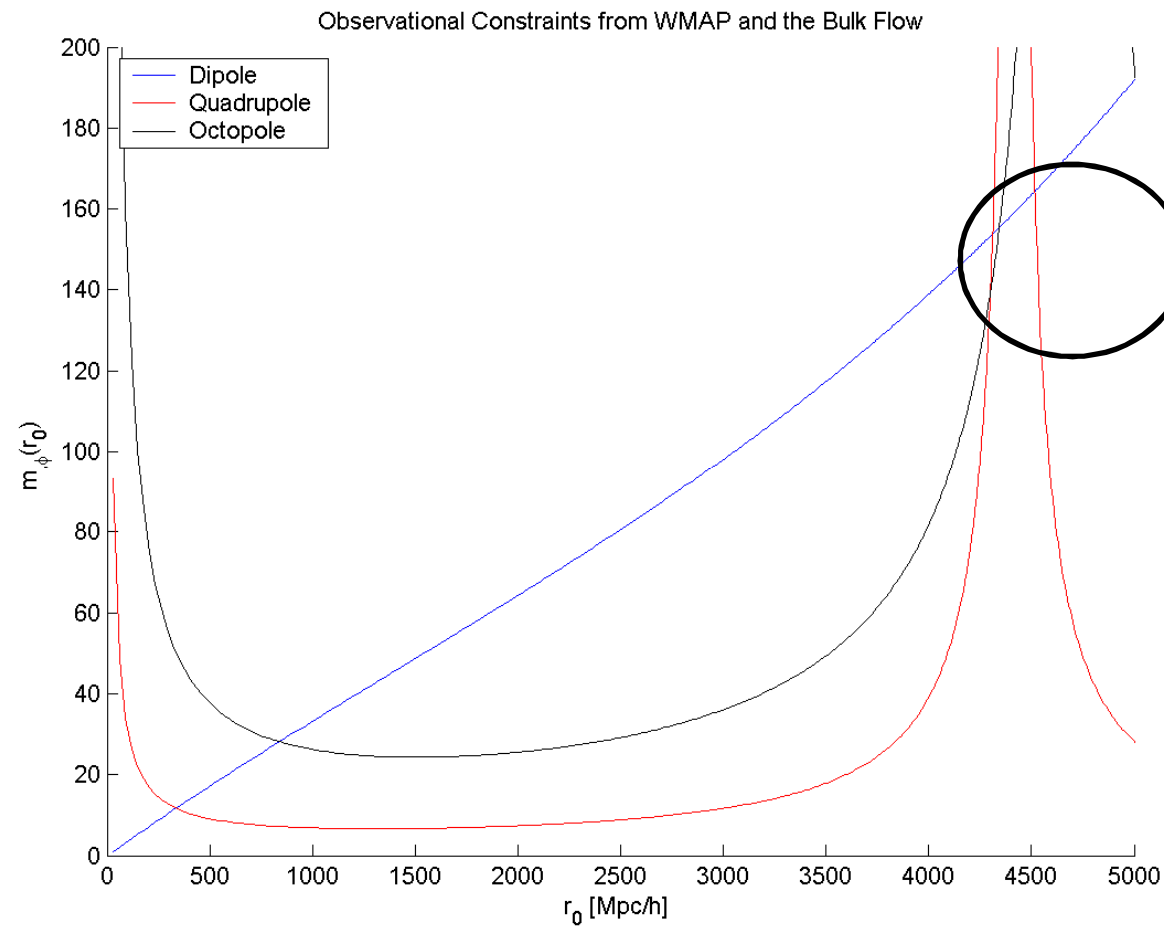




There is a region around  $4500/h \text{ Mpc}$  where we get a large peculiar velocity without affecting the CMB.



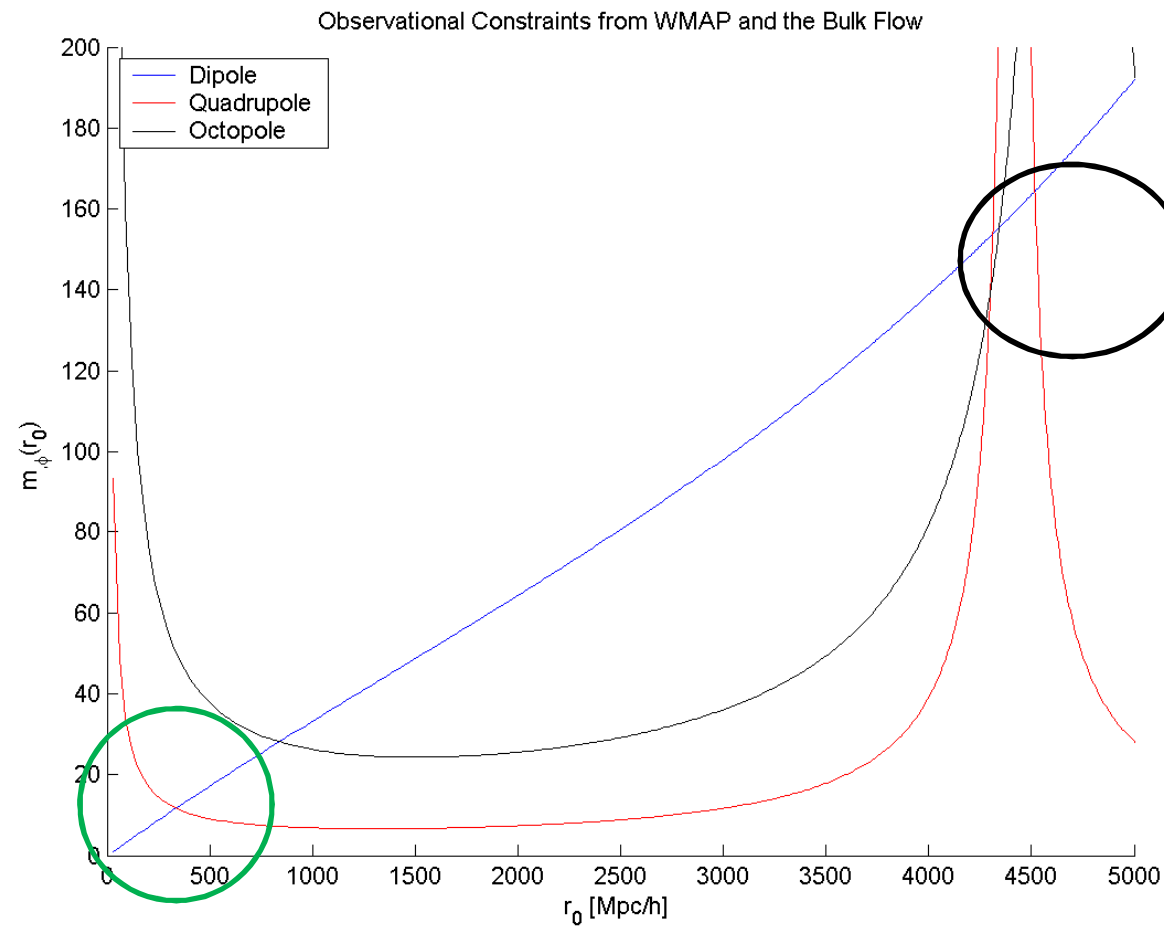
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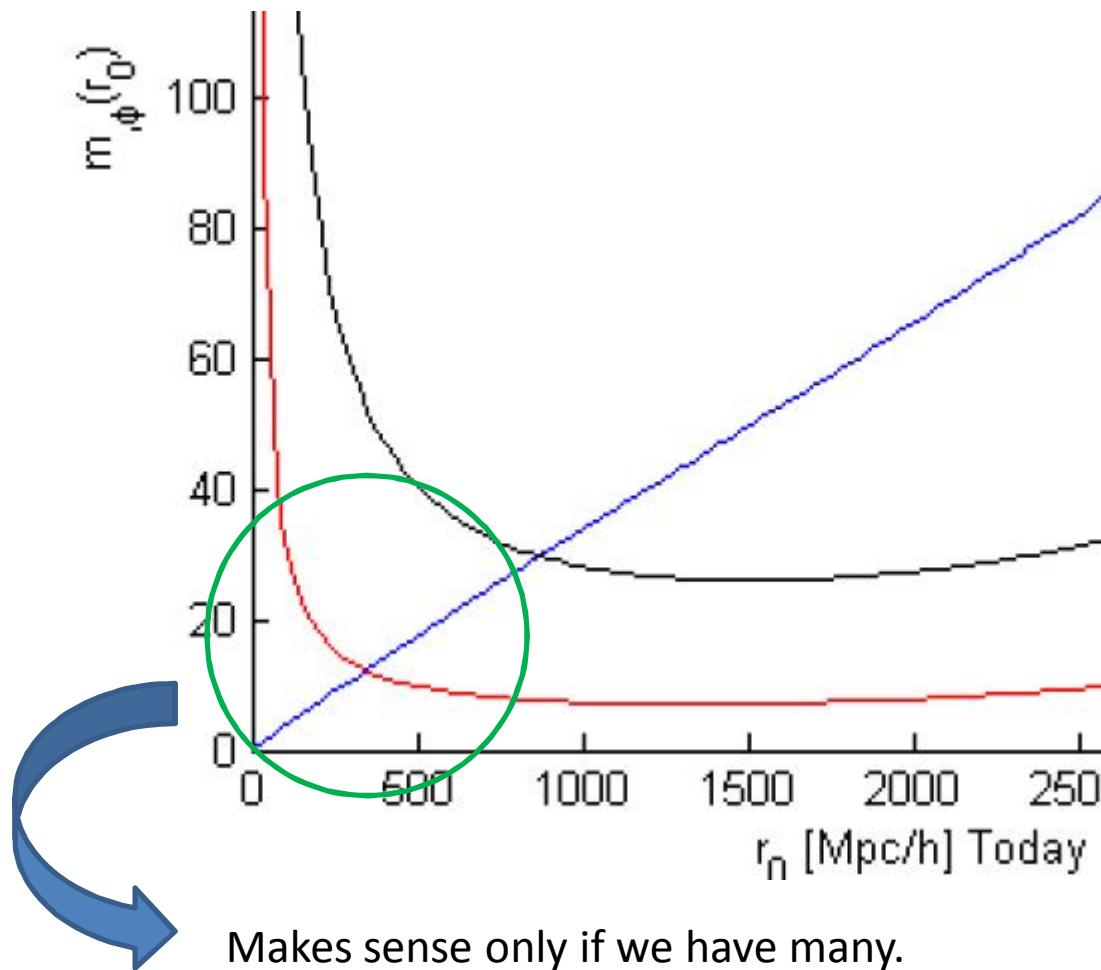


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$$P_{\Phi} = \frac{H^2}{9\epsilon k^3} \left( 1 + \frac{n\bar{m}^2}{16\pi k^3} \right)$$

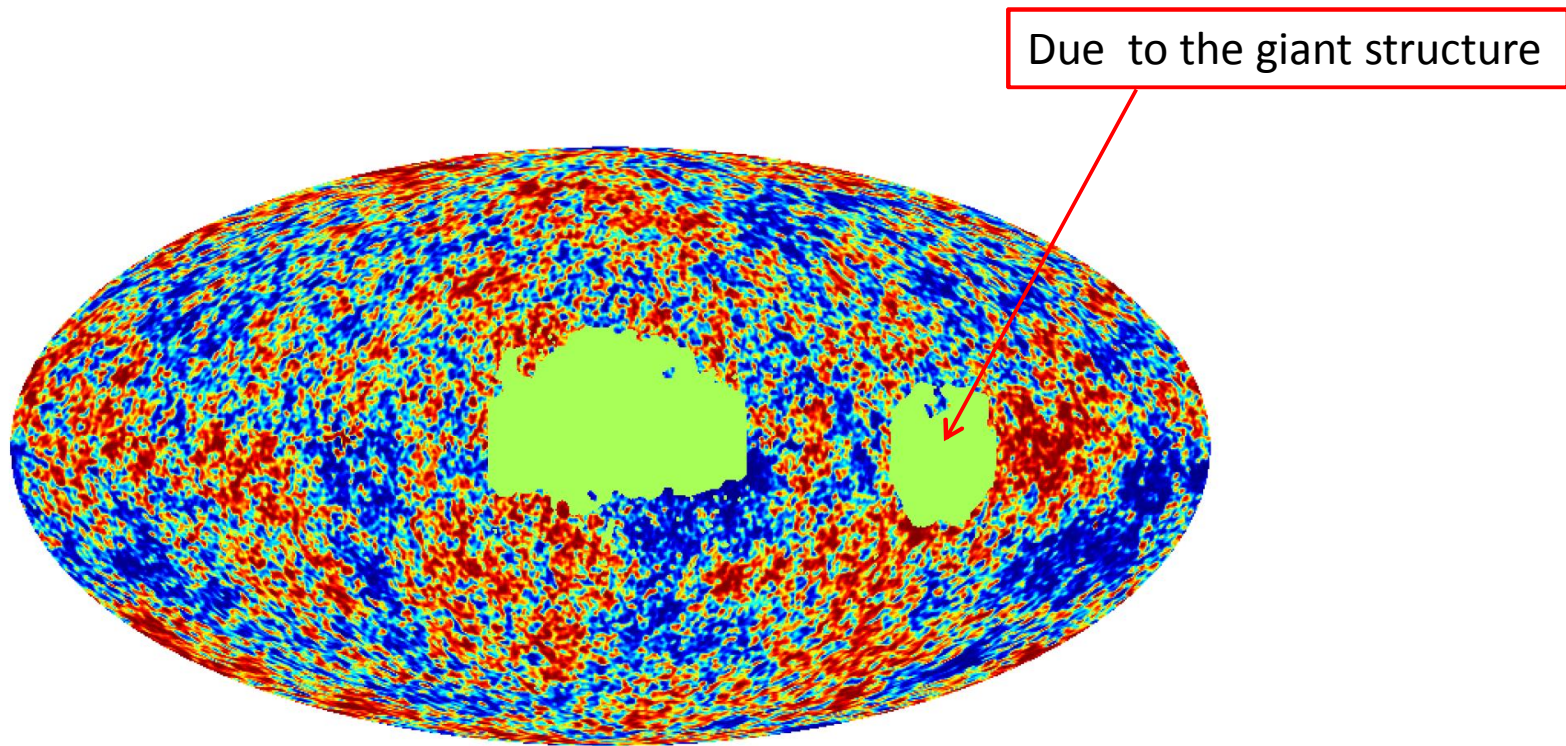
Important at the IR

Currently we are checking whether the low- $l$  CMB anomalies can be explained via this giant structure.



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Basic idea is simple:



## Weak Lensing

It turns out that this giant structure has also a distinct signature in weak lensing.

The density goes like  $1/r^2$  at large distances ( $r > 100$  Mpc).



A cosmological "Isothermal sphere" model.

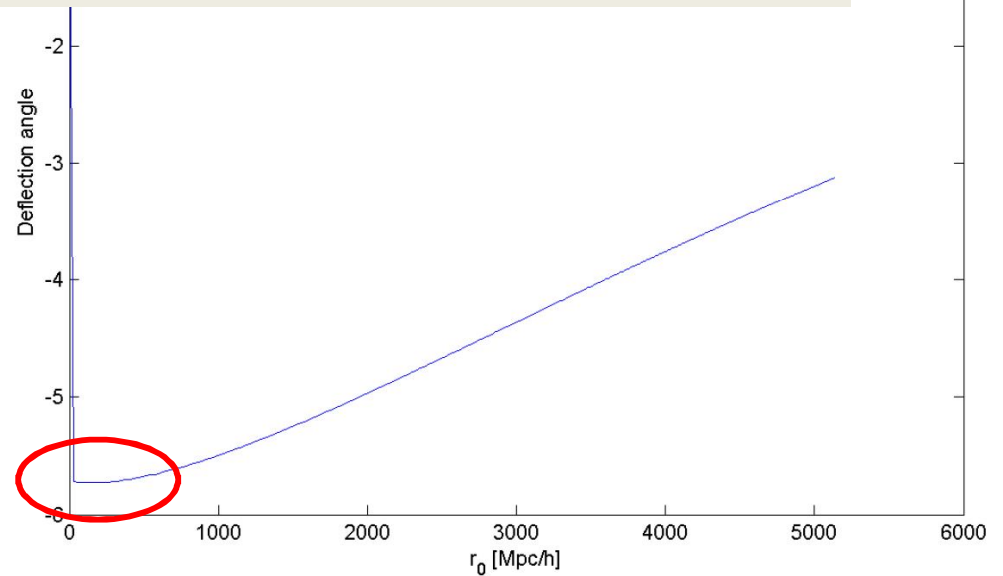
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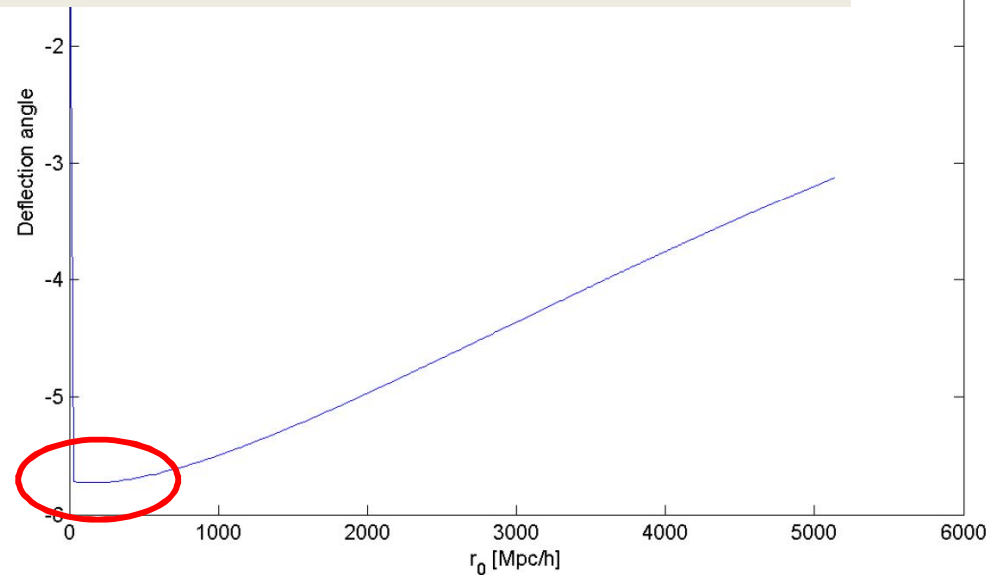
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Should have simple effects on CMB:

1. Polarization at low  $l$ .
2. Mixing between low- $l$  due to relative motion.



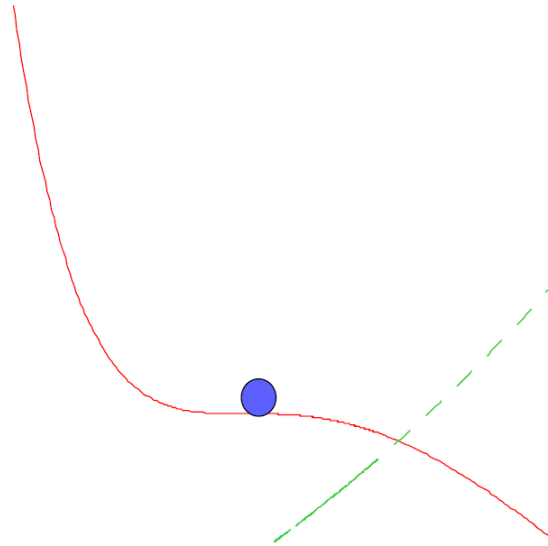
## Summary :

1. We proposed a concrete pre-inflationary remnant that is motivated by string theory.
2. We study some of its affects on the largest scale in the universe.
3. Argue that might be the way to explain some of the anomalies.





The particles become irrelevant



0807.3216:

Not quite irrelevant.

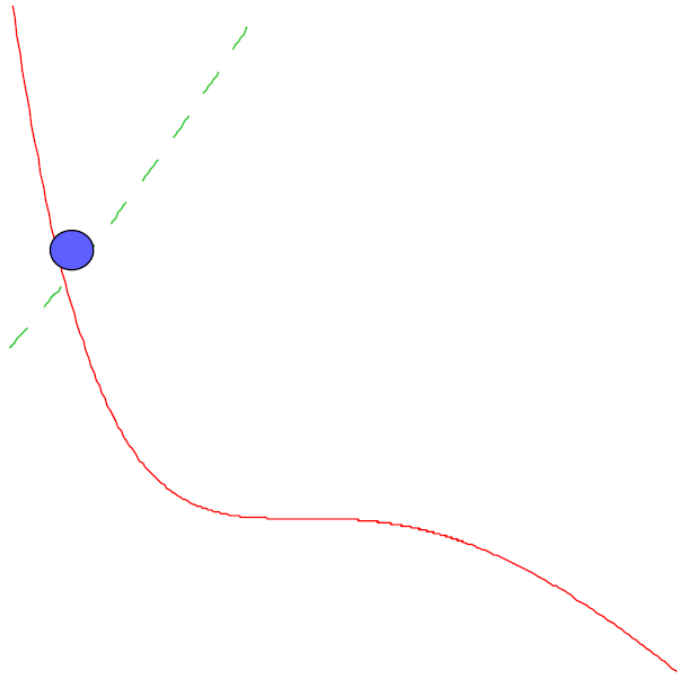
There is a possible **distinct** imprint in structure formation:

Creation of spherically symmetric overdense region(s) with radius of about 110 Mpc.

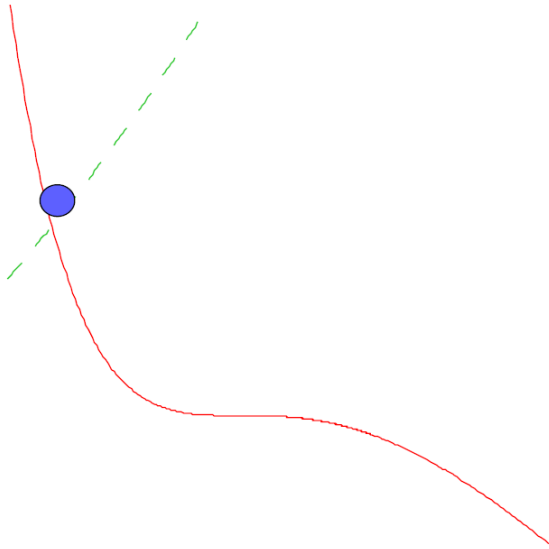


A resolution to the overshoot problem (N.I. E. Kovetz [0708.2798](#))

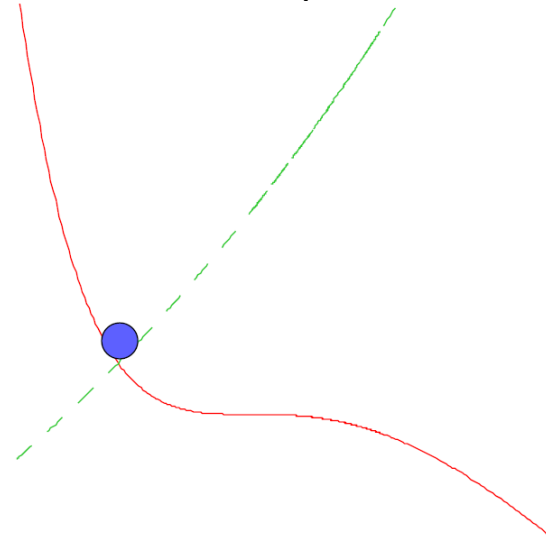
String theory often has non-perturbative particles with mass that grow with the value of the inflaton.



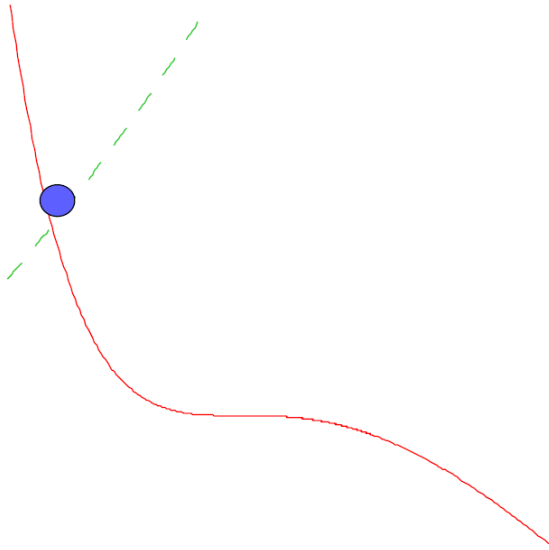
Minor effect at the beginning



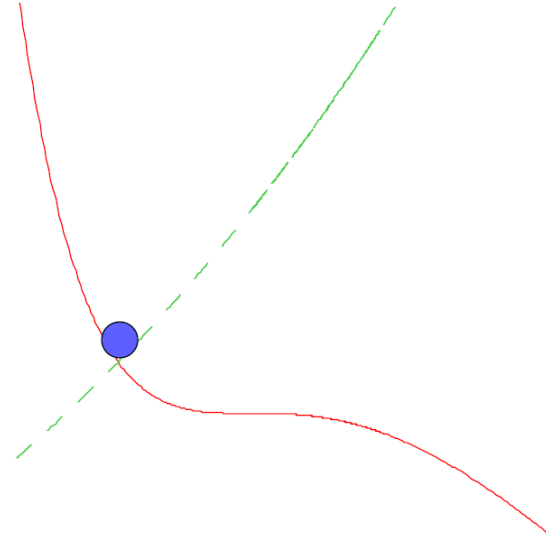
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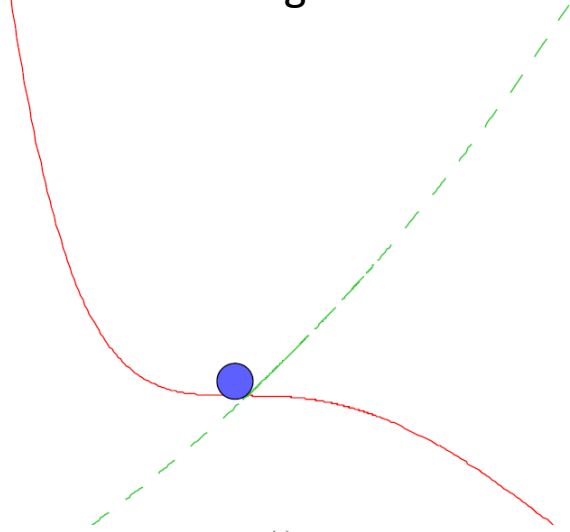
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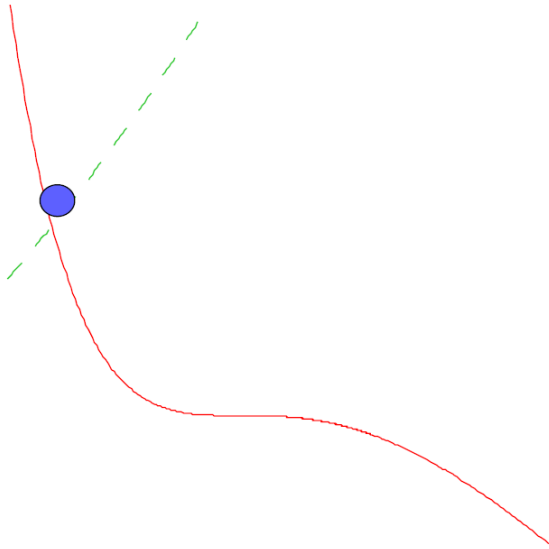
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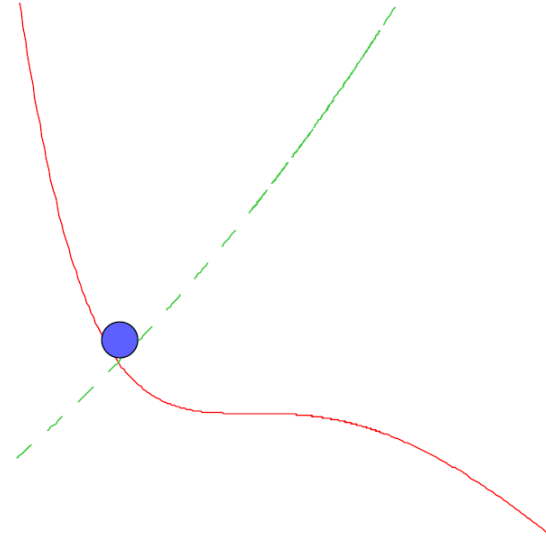
Inflaton moves slowly down at the slow-roll region



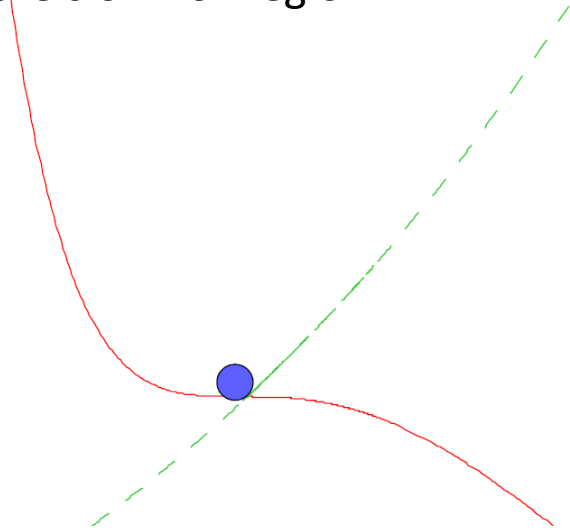
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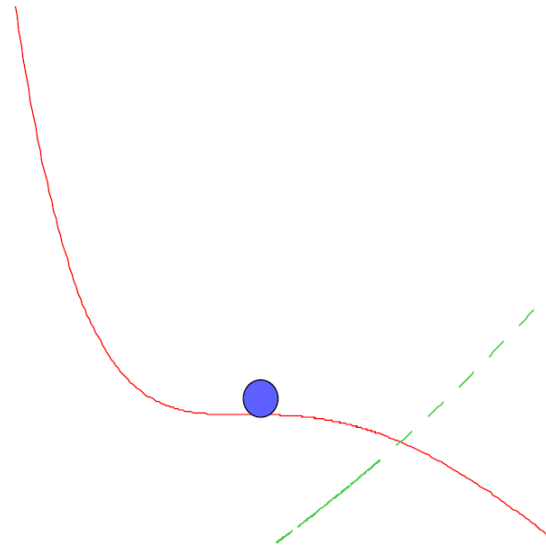
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